Tutorial 5

Analysis of propagation effects from GNSS observables based on laboratory exercises

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Slides associated to *gLAB* version 2.0.0

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OVERVIEW

- **Introduction**
- **The gLAB tool suite**
- **Examples of GNSS Data Processing using gLAB**
- **Laboratory session organization**

LABORATORY Session

- **Starting up your laptop**
- **Basic:** Introductory lab exercises: Iono & Posit, SF, storm,TIDs
- **Medium:** Laboratory Work Projects: LWP1 to LWP4
- **Advanced:** Homework

Introduction

- This tutorial is devoted to analysing and assessing different issues associated with GNSS signal propagation effects in the atmosphere.
- The laboratory exercises will be developed with actual GPS measurements, and processed with the **ESA/UPC GNSS-Lab Tool suite** (***gLAB***), which is an interactive software package for GNSS data processing and analysis.
- **All software tools** (including ***gLAB***) and associated files for the laboratory session are included in the USB stick delivered to those who attend the lecture.
- **The laboratory session** will consist of a set of exercises organized in three different levels of difficulty (Basic, Medium and Advanced). A set of introductory examples range from a first glance assessment of the ionosphere effects on single frequency positioning, and Zenith Tropospheric Delays estimate to showing different perturbation effects in the ionosphere (Solar Flair, Halloween storm, TIDs). Electron density profiles (Ne) retrieval, bending effects analysis (phase excess rate depicture), as well as in-depth analysis of the code-carrier ionosphere divergence on single-frequency smoothed codes and the second order ionospheric effects are analysed in detail in four Laboratory Work Projects. Other topics are given as homework.
- The target is to provide the participants with a **wide range of selected exercises to choose from,** according their interests and their level of knowledge of these topics.

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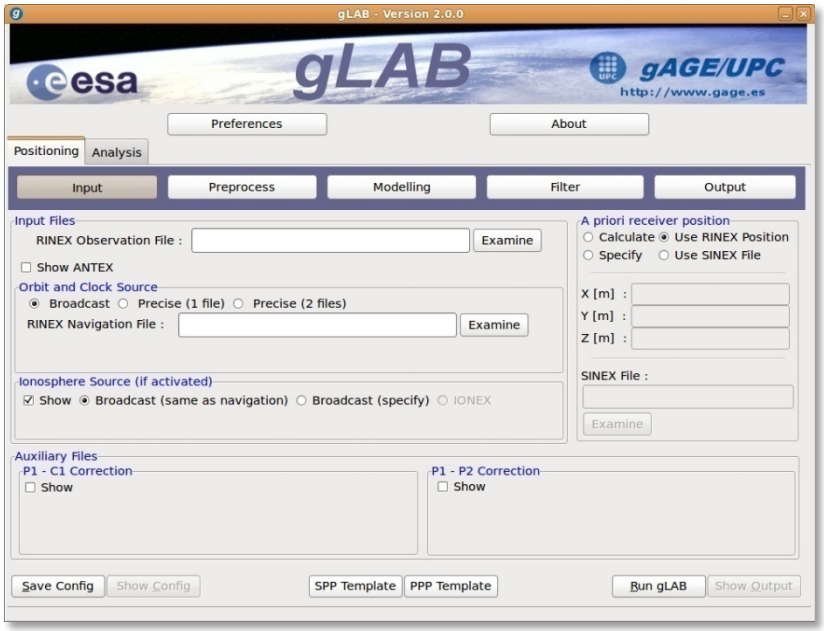
The gLAB Tool suite

- **The GNSS-Lab Tool suite (gLAB)** is an interactive multipurpose educational and professional package for GNSS Data Processing and Analysis.
- gLAB has been developed under the ESA Education Office contract N. P1081434.
- **Main features:**
  - High Accuracy Positioning capability.
  - Fully configurable.
  - Easy to use.
  - Access to internal computations.



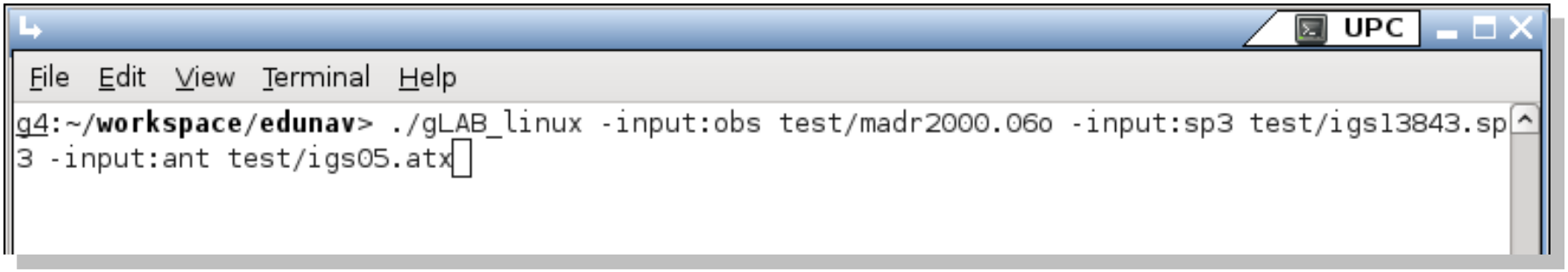
The gLAB Tool suite

Students/Newcomers:

- Easy to use: Intuitive GUI.
- Explanations: Tooltips over the different GUI options.
- Guidelines: Several error and warning messages. Templates for pre-configured processing.

Professionals/Experts:

- Powerful tool with High Accuracy Positioning capability.
- Fast to configure and use: Templates and carefully chosen defaults.
- Can be executed in command-line and **included in batch processing**.



The gLAB Tool suite

- **In order to widen the tool availability, gLAB Software has been designed to work in both Windows and Linux environments.**

- **The package contains:**
  - Windows binaries (with an installable file).
  - Linux .tgz file.
  - Source code (to compile it in both Linux and Windows OS) under an Apache 2.0 license.
  - Example data files.
  - Software User Manual.
  - HTML files describing the standard formats.

The gLAB Tool suite

- **Read files capability:**
  - RINEX observation v2.11 & v3.00
  - RINEX navigation message.
  - SP3 precise satellite clocks and orbits files
  - ANTEX Antenna information files.
  - Constellation status.
  - DCBs files.
  - GPS_Receiver_Type files.
  - SINEX position files.

- **Pre-processing module:**
  - Carrier-phase pre-alignment.
  - Carrier-phase / pseudo-range consistency check.
  - Cycle-slip detection (customizable parameters)
    - Melbourne-Wübbena.
    - Geometry-free CP combination.
    - L1-C1 difference (single frequency).
  - Pseudo-range smoothing.
  - Decimation capability.
  - On demand satellite enable/disable.
  - Elevation mask.
  - Frequency selection.
  - Discard eclipsed satellites.

- **Modelling module:**
  - Fully configurable model.
  - Satellite positions.
  - Satellite clock error correction.
  - Satellite movement during signal flight time.
  - Earth rotation during signal flight time.
  - Satellite phase center correction.
  - Receiver phase center correction. (frequency dependent).
  - Relativistic clock correction.
  - Relativistic path range correction.
  - Ionospheric correction (Klobuchar).
  - Tropospheric correction
    - Simple and Niell mappings.
    - Simple and UNB-3 nominals.
  - Differential Code Bias corrections.
  - Wind up correction.
  - Solid tides correction (up to 2nd degree).

The gLAB Tool suite

Filtering module:

- Able to chose different measurements to process (1 or more), with different weights. This design could be useful in future Galileo processing, where processing with different measurements may be desired.
- Fixed or elevation-dependent weights per observation.
- Troposphere estimation on/off.
- Carrier-Phase or Pseudo-range positioning.
- Static/Kinematic positioning (full Q/Phi/P0 customization).
- Able to do a forward/backward processing.
- Able to compute trajectories (no need for a priori position).

Output module:

- Cartesian / NEU coordinates.
- Configurable message output.

Other functionalities:

- Computation of satellite coordinates and clocks from RINEX and SP3 files.
- Satellite coordinates comparison mode. For instance RINEX navigation vs. SP3, or SP3 vs. SP3 (along-track, cross-track and radial orbit errors, clock errors, SISRE).
- Show input mode. No processing, only parsing RINEX observation files.

- **Current version allows full GPS data processing, and partial handling of Galileo and GLONASS data.**
- **Future updates may include full GNSS data processing.**

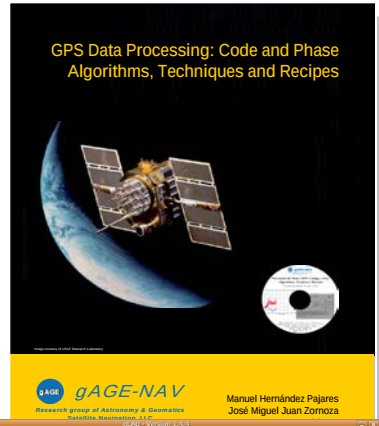
GNSS learning material package

Includes three different parts, allowing participants to follow either a guided or a self-learning GNSS course:

- **GNSS Book**: Complete book with theory, practical examples, and with a Laboratory course on GNSS Data Processing & Analysis [R-1].

- **gLAB tool suite**: Source code and binary software files, plus configuration files, allowing processing GNSS data from standard formats. The options are fully configurable through a GUI.

- **gAGE-GLUE**: Bootable USB stick with a full environment ready to use; based on LINUX (Ubuntu) OS.


GPS Data Processing: Code and Phase Algorithms, Techniques and Recipes
gAGE-NAV
Research group of Astronomy & Geomatics
Manuel Hernández Pajares
José Miguel Juan Zornoza

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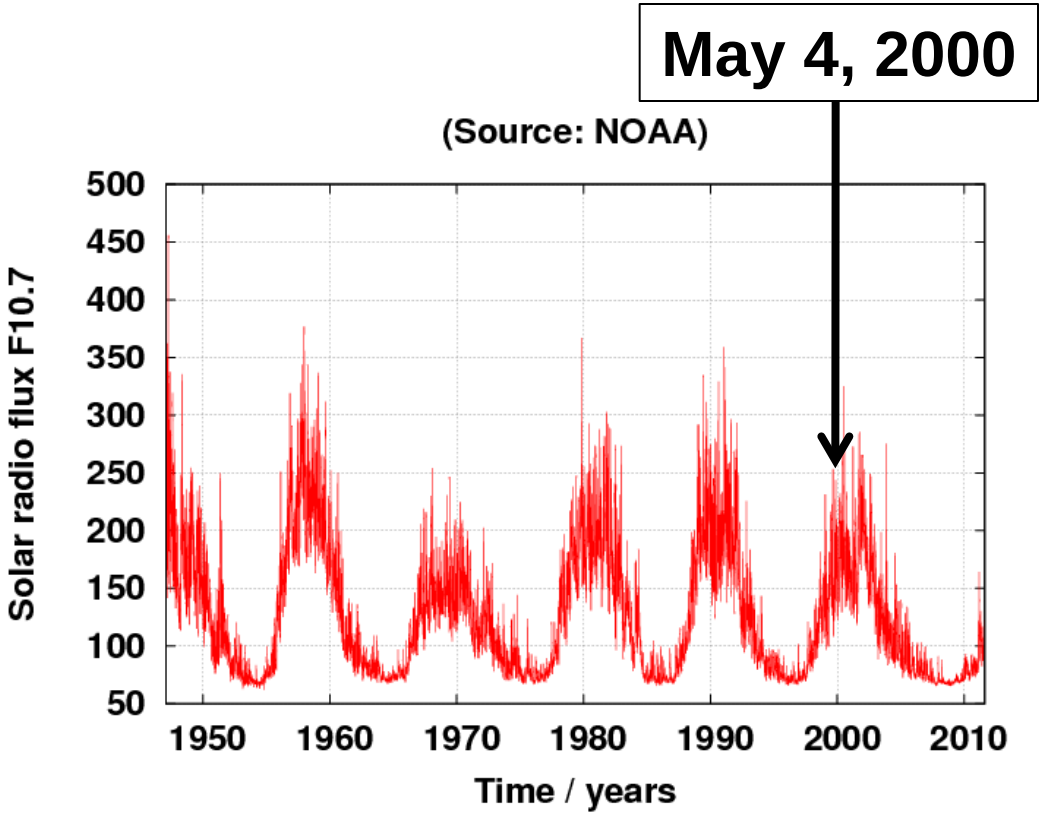
Example 1: Ionospheric effects on single frequency positioning.

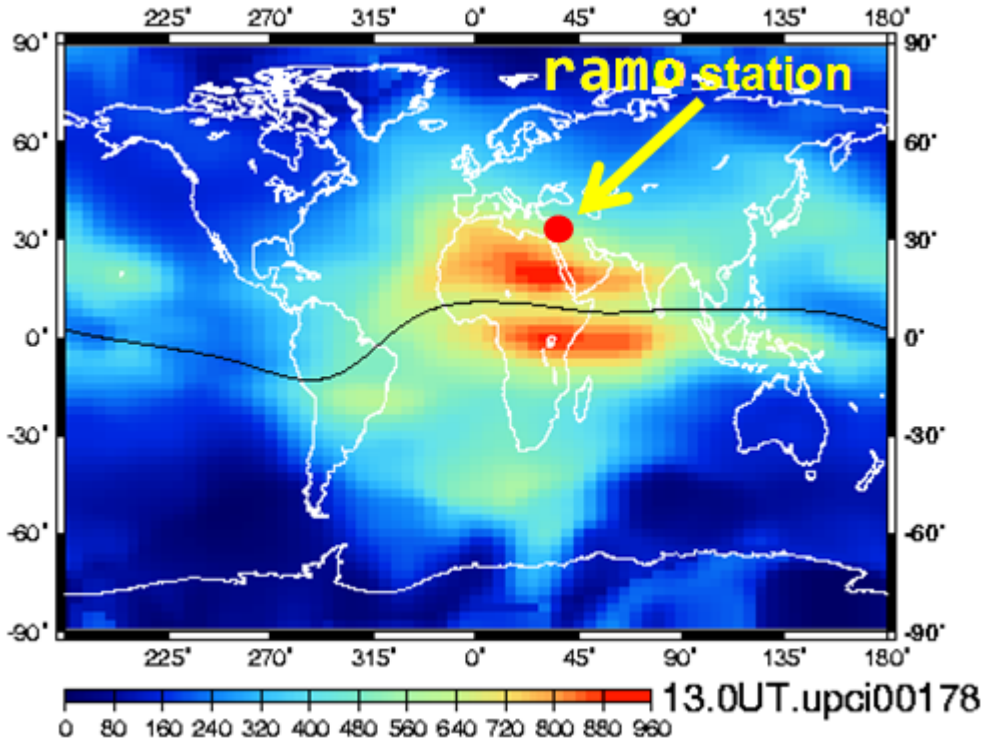
- This exercise is devoted to analysing the effect of the ionospheric error in single frequency positioning. This is done both in the Signal-In-Space (SIS) and User Domains.

- A receiver will be positioned in Standard Point Positioning (SPP) mode: a) with full modelling, b) neglecting the ionospheric correction.

Example 1: Iono effects on single freq. Posit.

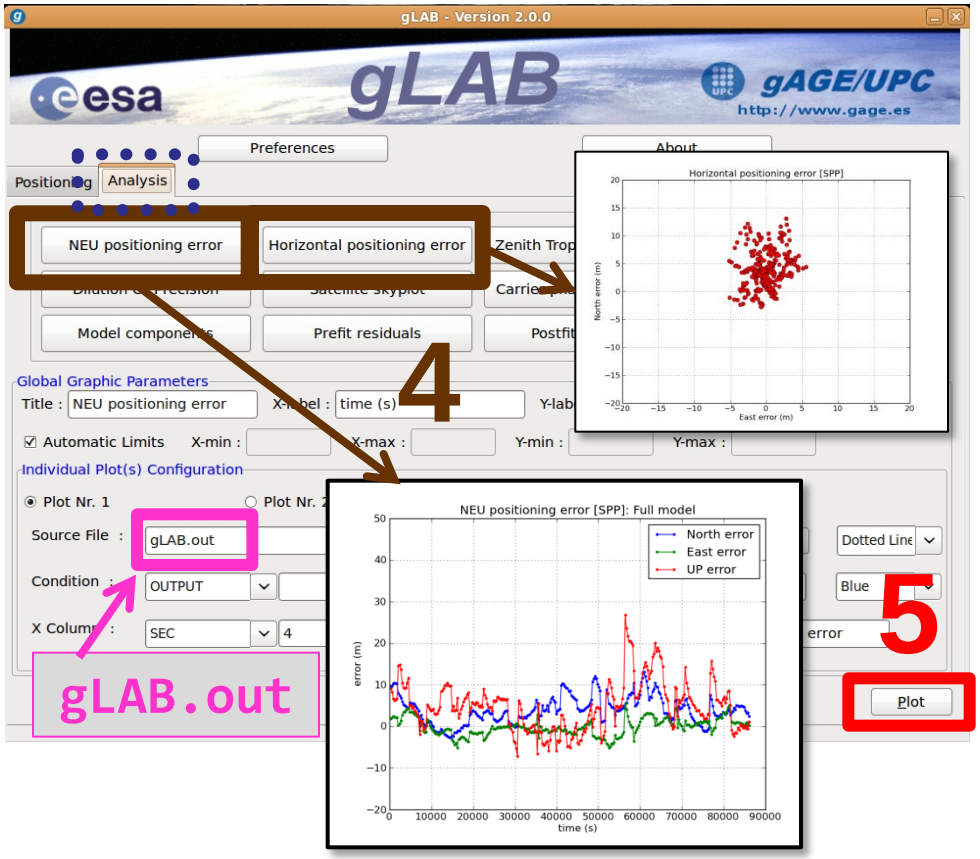
Data set: **24h data collected by the IGS permanent receiver "ramo" (Lon,Lat) on May 4th 2000.**





Example 1: Iono effects on single freq. Posit.

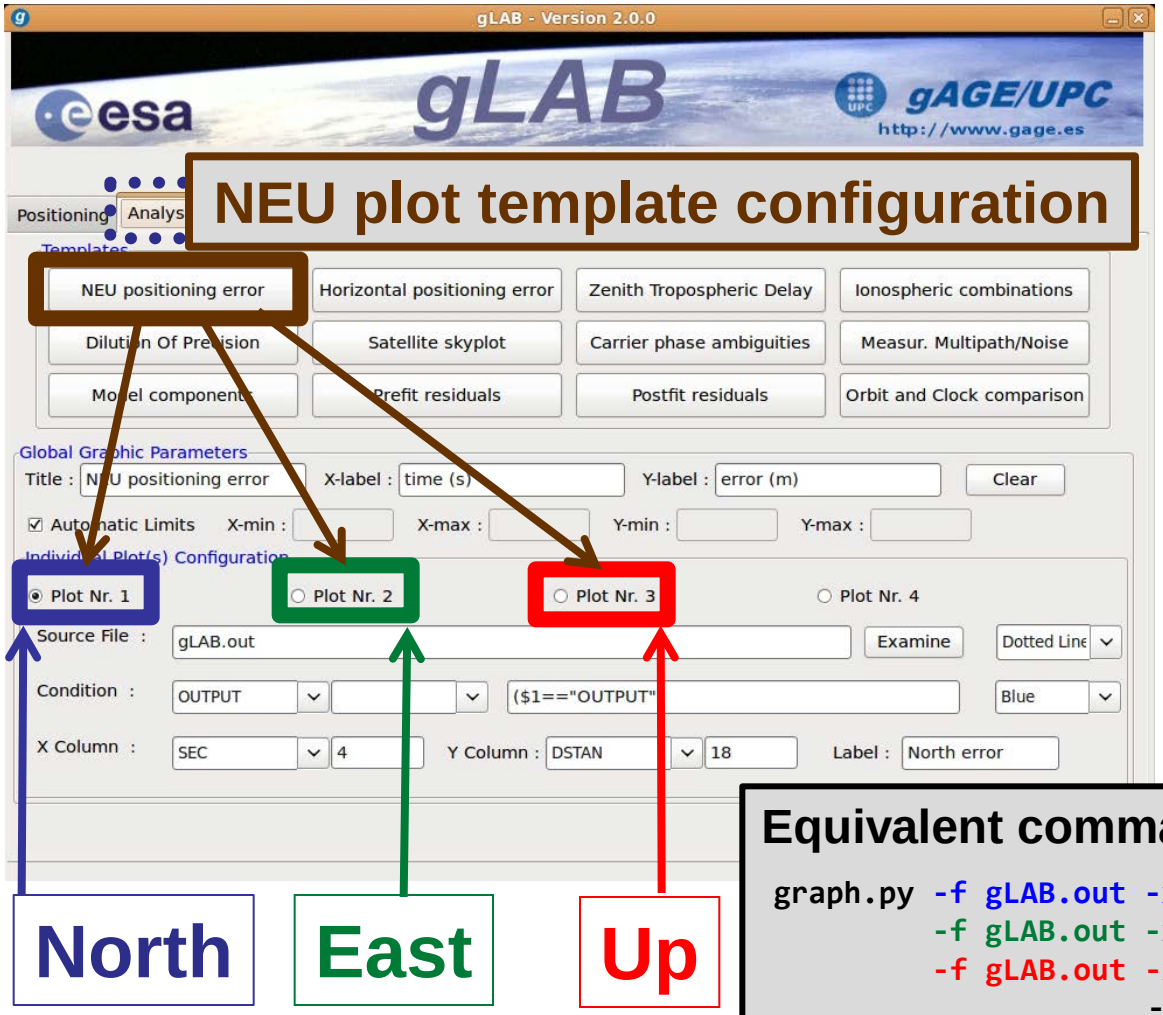
1. Compute SPP using files: `ramo1250.00o,brdc1250.00n`



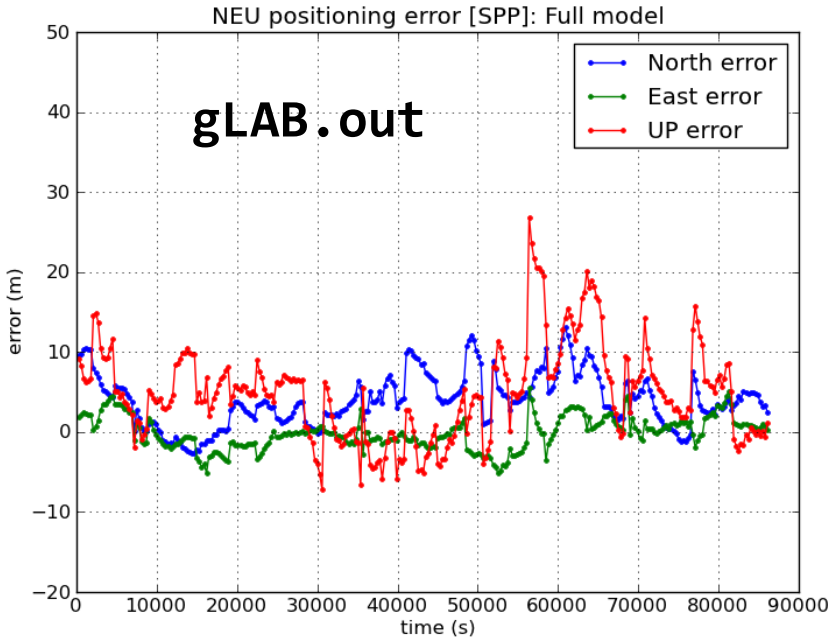
Equivalent command line sentence:

```
gLAB_linux -input:cfg gLAB_p1_Full.cfg
           -input:obs ramo1250.00o
           -input:nav brdc1250.00n
```

Example 1. NEU Position Error plot from gLAB.out



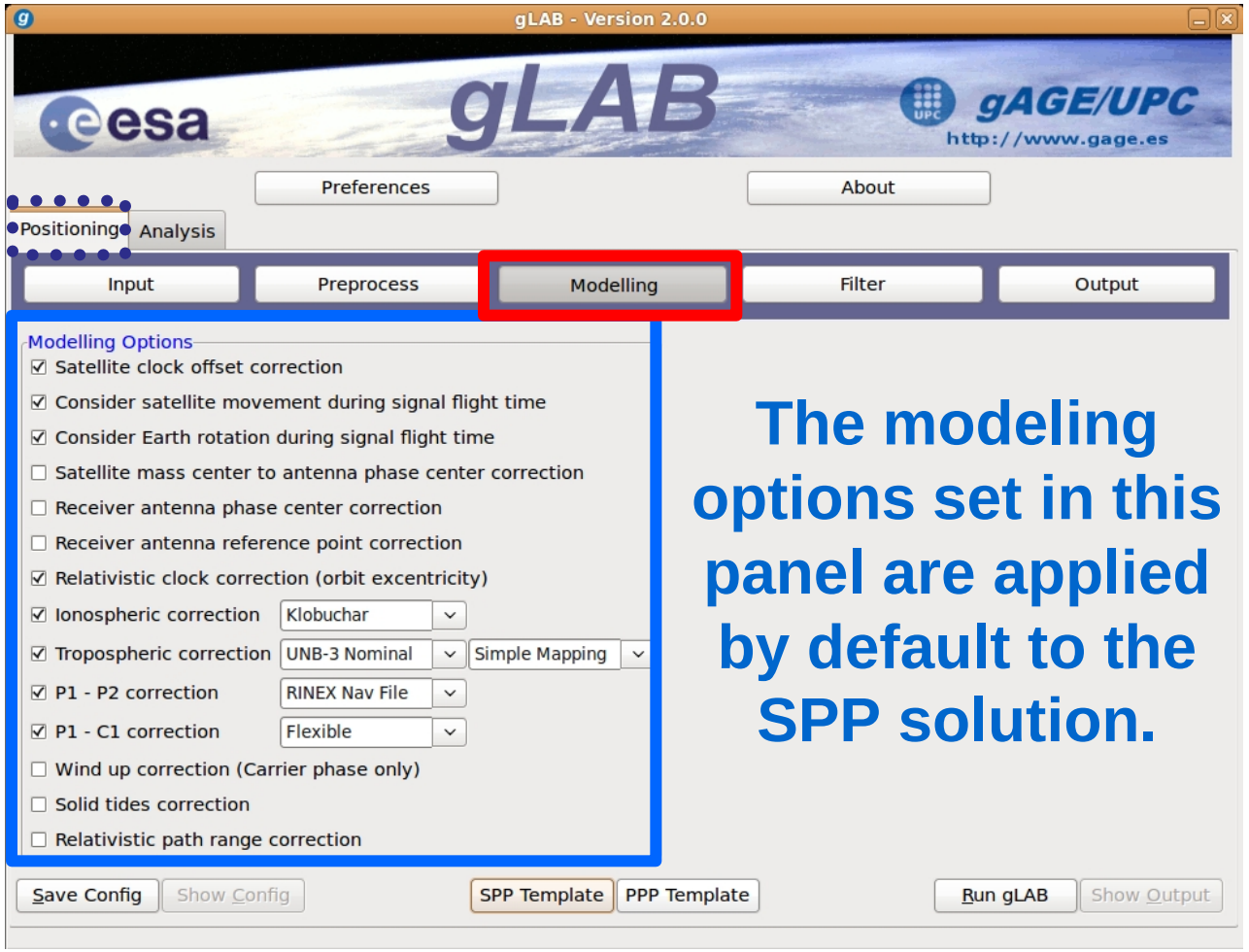
FULL SPP model



Equivalent command line sentence:

```
graph.py -f gLAB.out -x4 -y18 -s.- -c '($1=="OUTPUT")' -l "North error"
         -f gLAB.out -x4 -y19 -s.- -c '($1=="OUTPUT")' -l "East error"
         -f gLAB.out -x4 -y20 -s.- -c '($1=="OUTPUT")' -l "UP error"
                     --yn -20 --yx 50 --xl "time (s)" --yl "error (m)"
                     -t "NEU positioning error [SPP]: Full model"
```

Example 1. gLAB Modeling panel



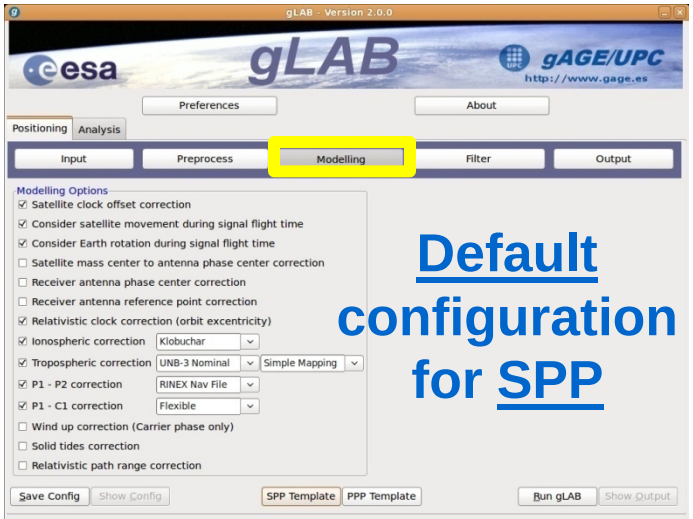
The modeling options set in this panel are applied by default to the SPP solution.

The different model terms can be analyzed with gLAB:

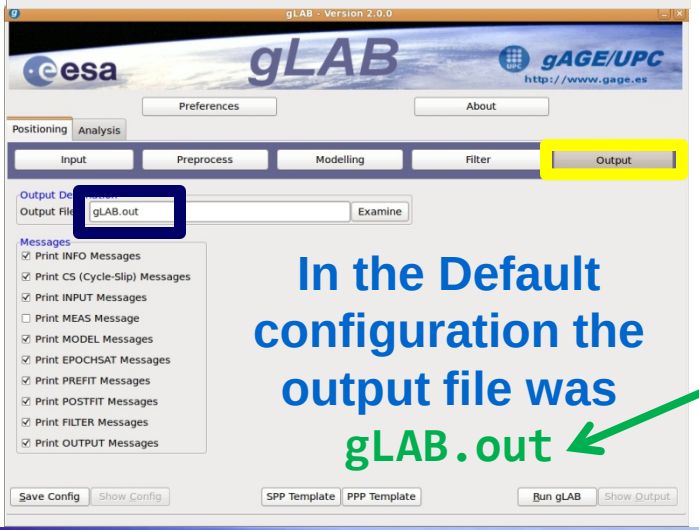
•Using the previous data file, the impact of neglecting the ionospheric correction is evaluated in the Range and Position domains.

•This is a baseline example of this analysis procedure. The same scheme must be applied for all model terms (troposphere, relativistic correction...). A full analysis of the different model components can be found in [R-2].)

Example 1. Model component analysis: **IONO.**



Default configuration for SPP



In the Default configuration the output file was `gLAB.out`

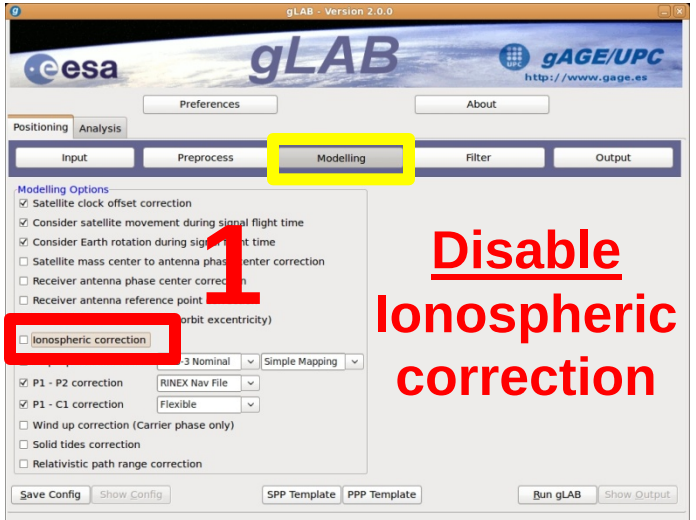
The procedure explained here is applicable for all model terms: iono, tropo…

1.In Modeling panel, disable the model component to analyze.

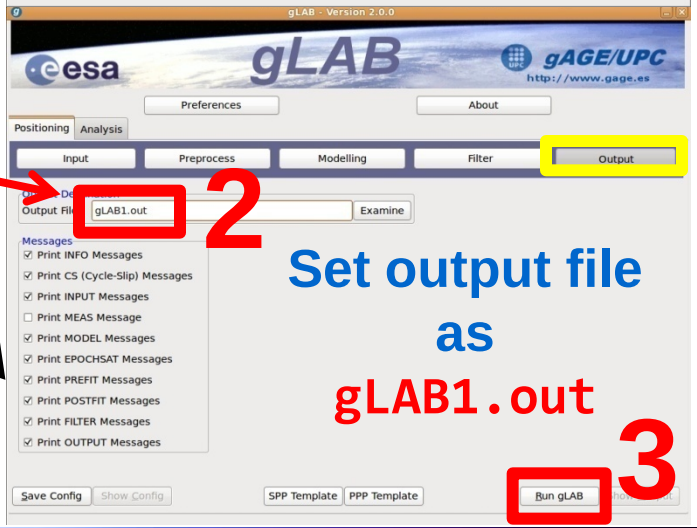
(in this example: disable **Ionospheric correction**)

2.Save as **`gLAB1.out`** the associated output file.

Notice that the **`gLAB.out`** file contains the processing results with the **FULL model**, as was set in the default configuration.



Disable Ionospheric correction

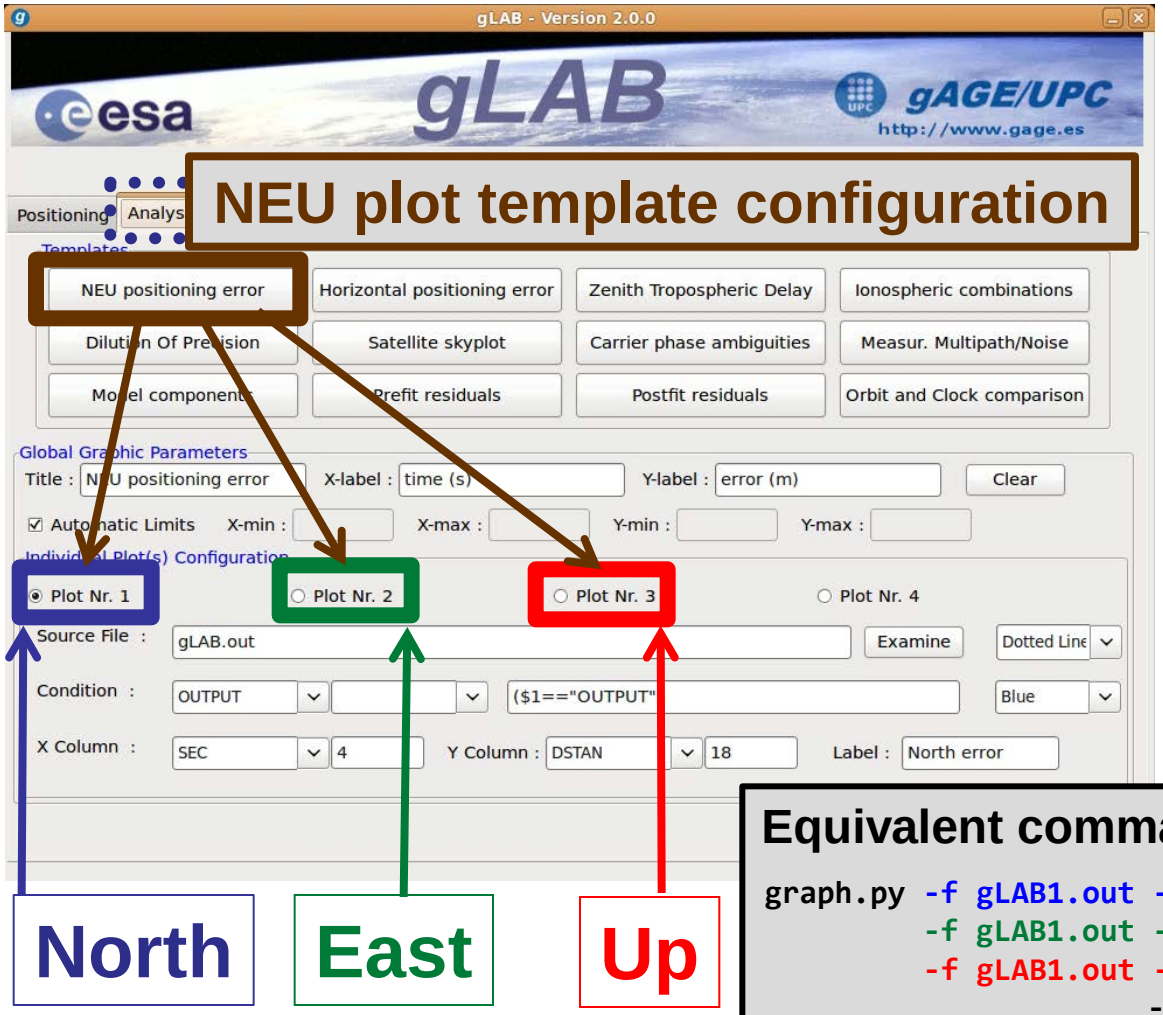


Set output file as `gLAB1.out`

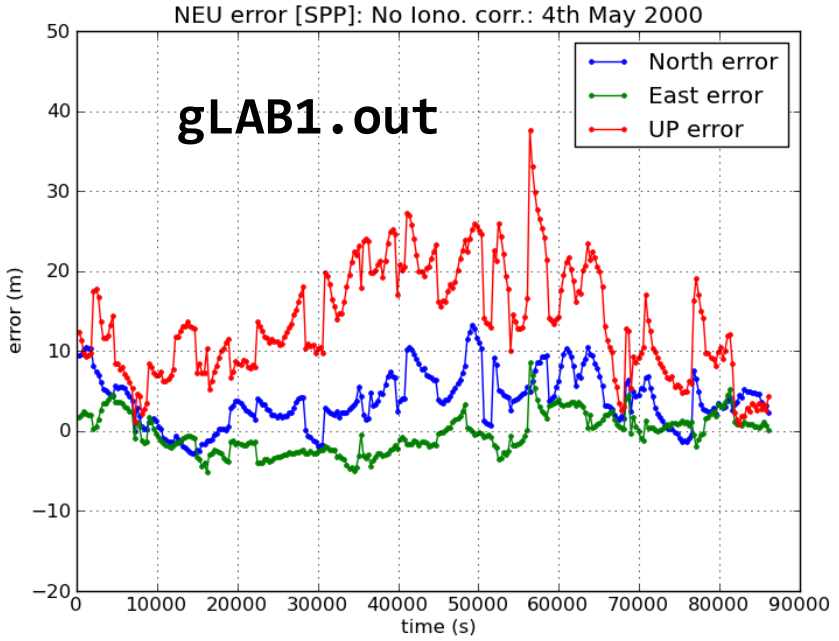
Equivalent command line sentence:

```
gLAB_linux -input:cfg gLAB_p1_NoIono.cfg
           -input:obs ramo1250.00o -input:nav brdc1250.00n
```

Example 1. NEU Position Error plot from gLAB1.out



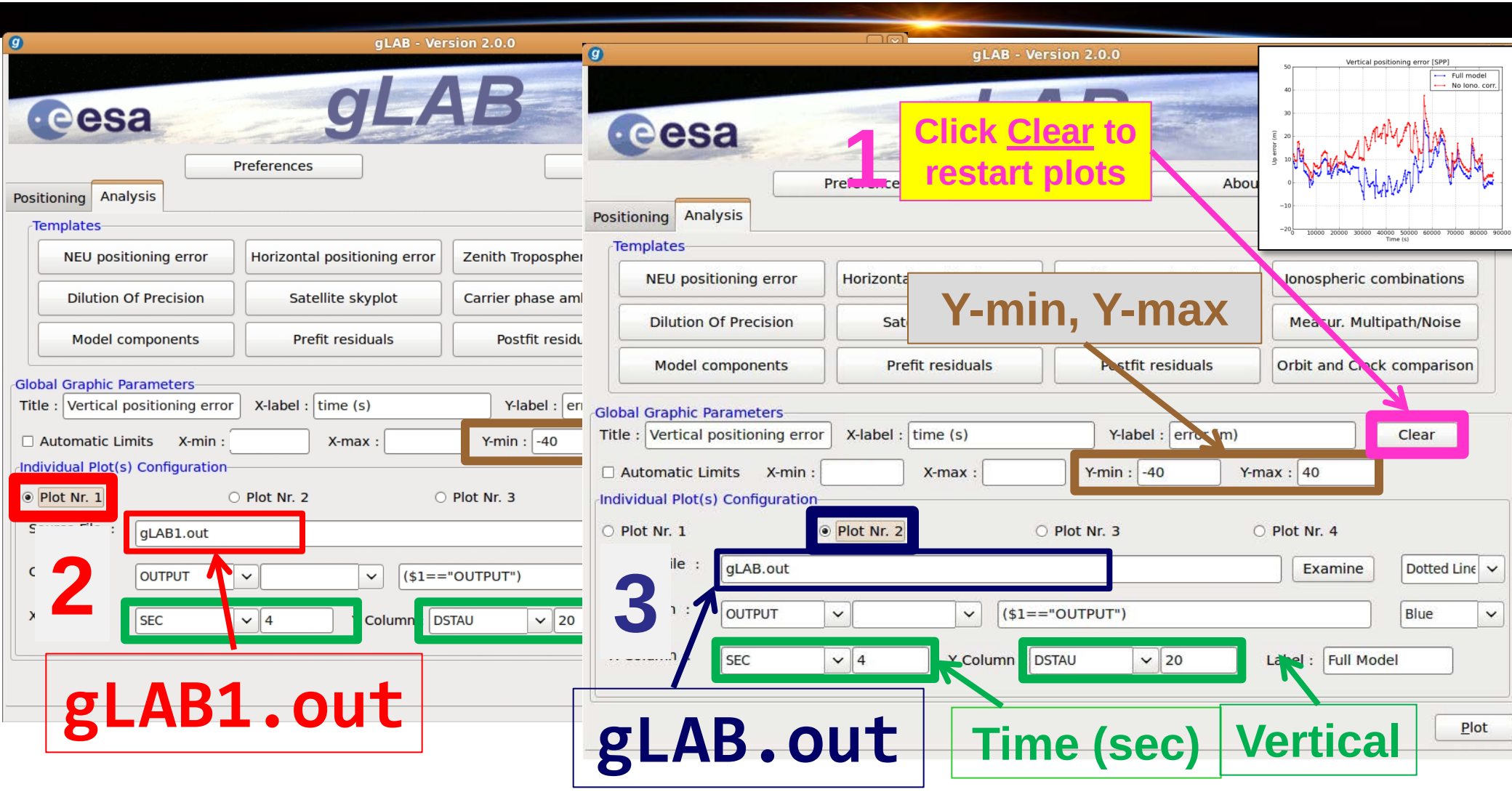
No Iono. correction



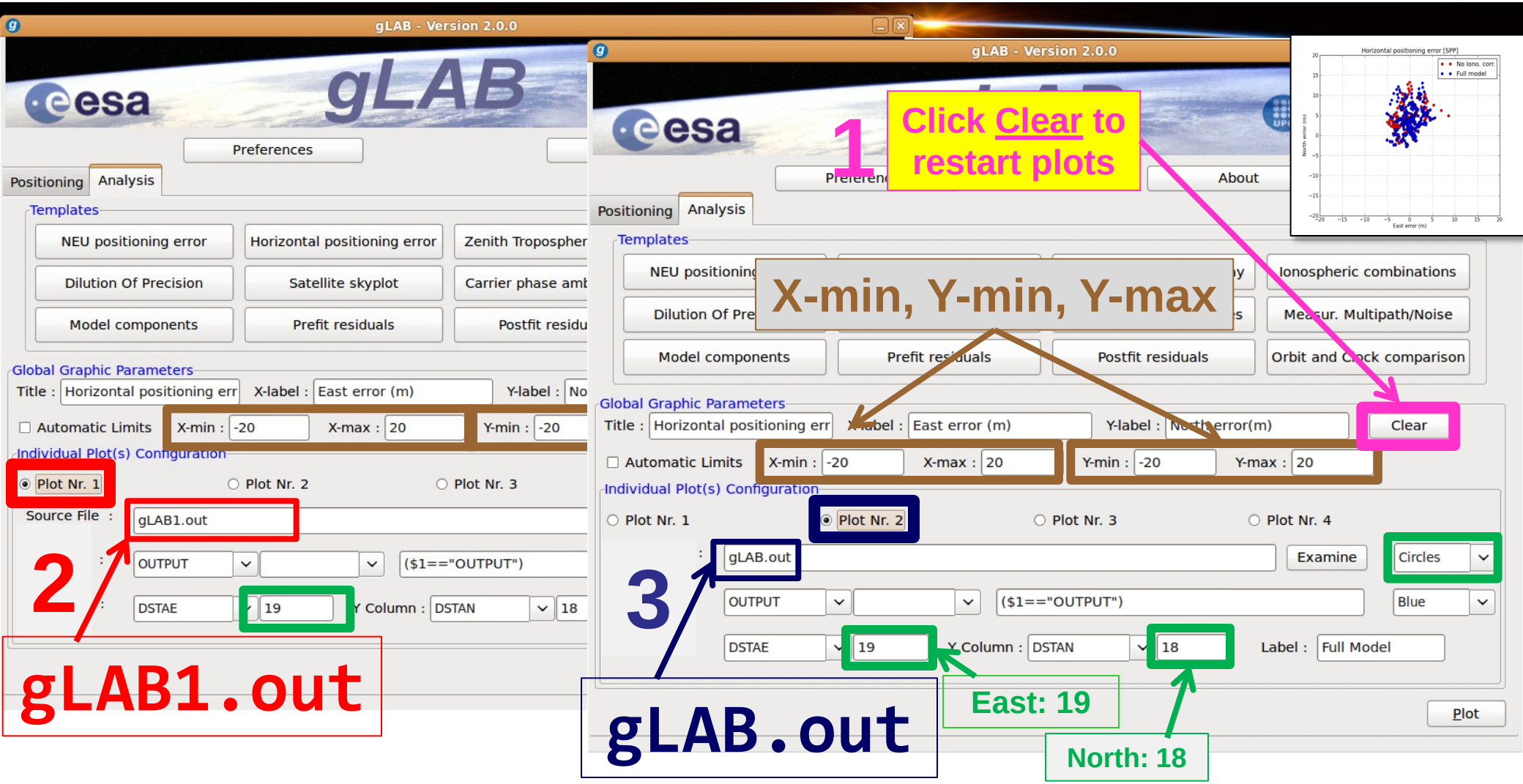
Equivalent command line sentence:

```
graph.py -f gLAB1.out -x4 -y18 -s.- -c '($1=="OUTPUT")' -l "North error"
         -f gLAB1.out -x4 -y19 -s.- -c '($1=="OUTPUT")' -l "East error"
         -f gLAB1.out -x4 -y20 -s.- -c '($1=="OUTPUT")' -l "UP error"
                  --yn -20 --yx 50 --xl "time (s)" --yl "error (m)"
                  -t "NEU positioning error [SPP]: No Iono. Corr."
```

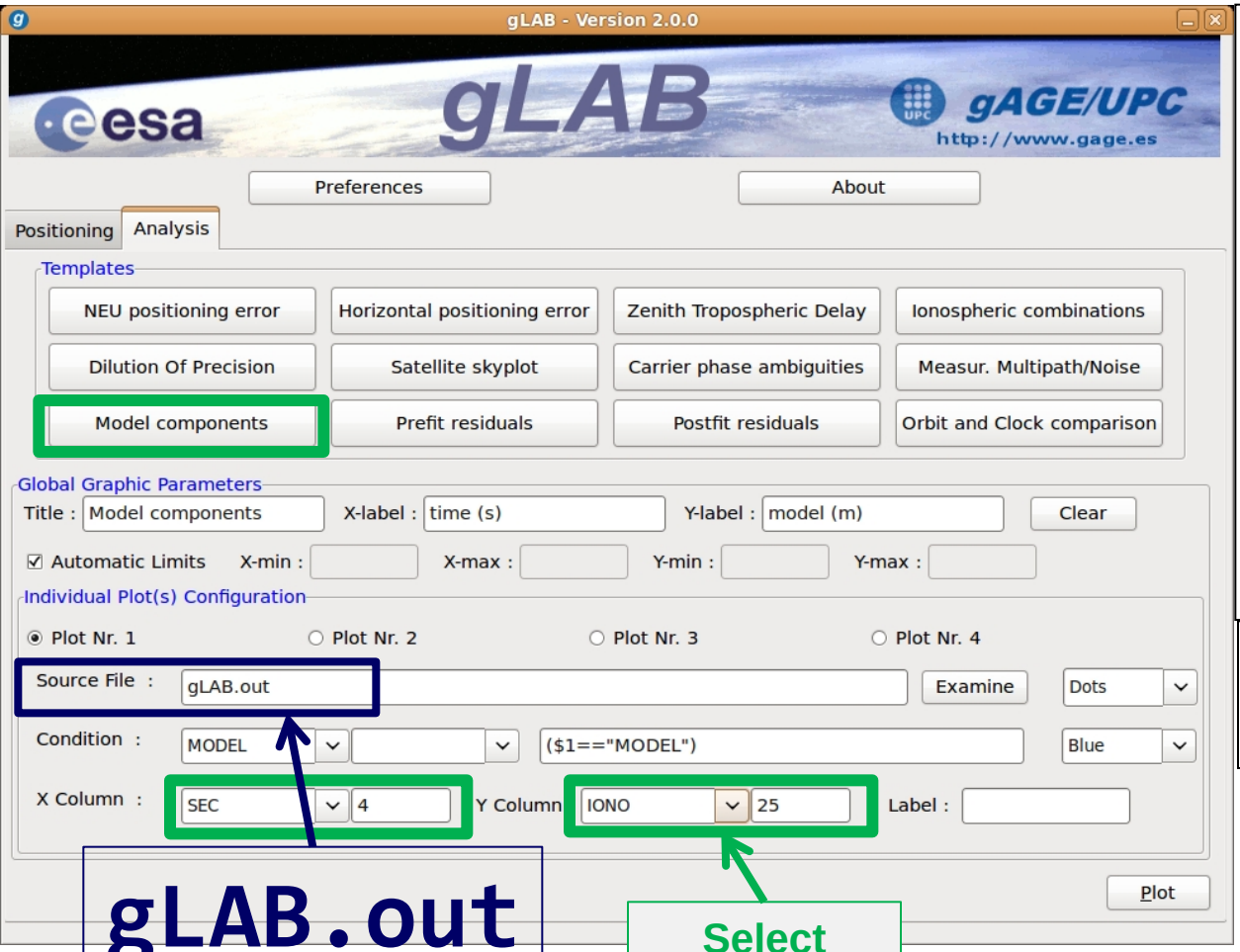
Example 1. VPE plot from gLAB.out, gLAB1.out

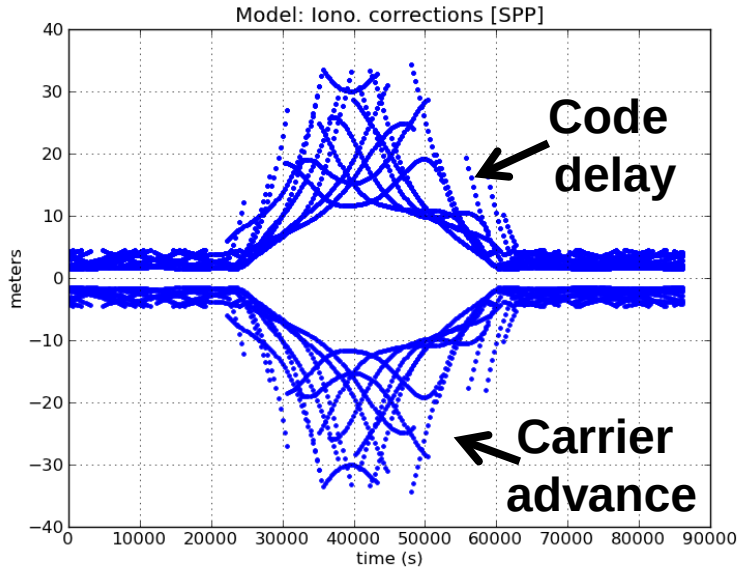


Example 1. HPE plot: gLAB.out, gLAB1.out



Example 1. Klobuchar iono. corr. plot: gLAB.out

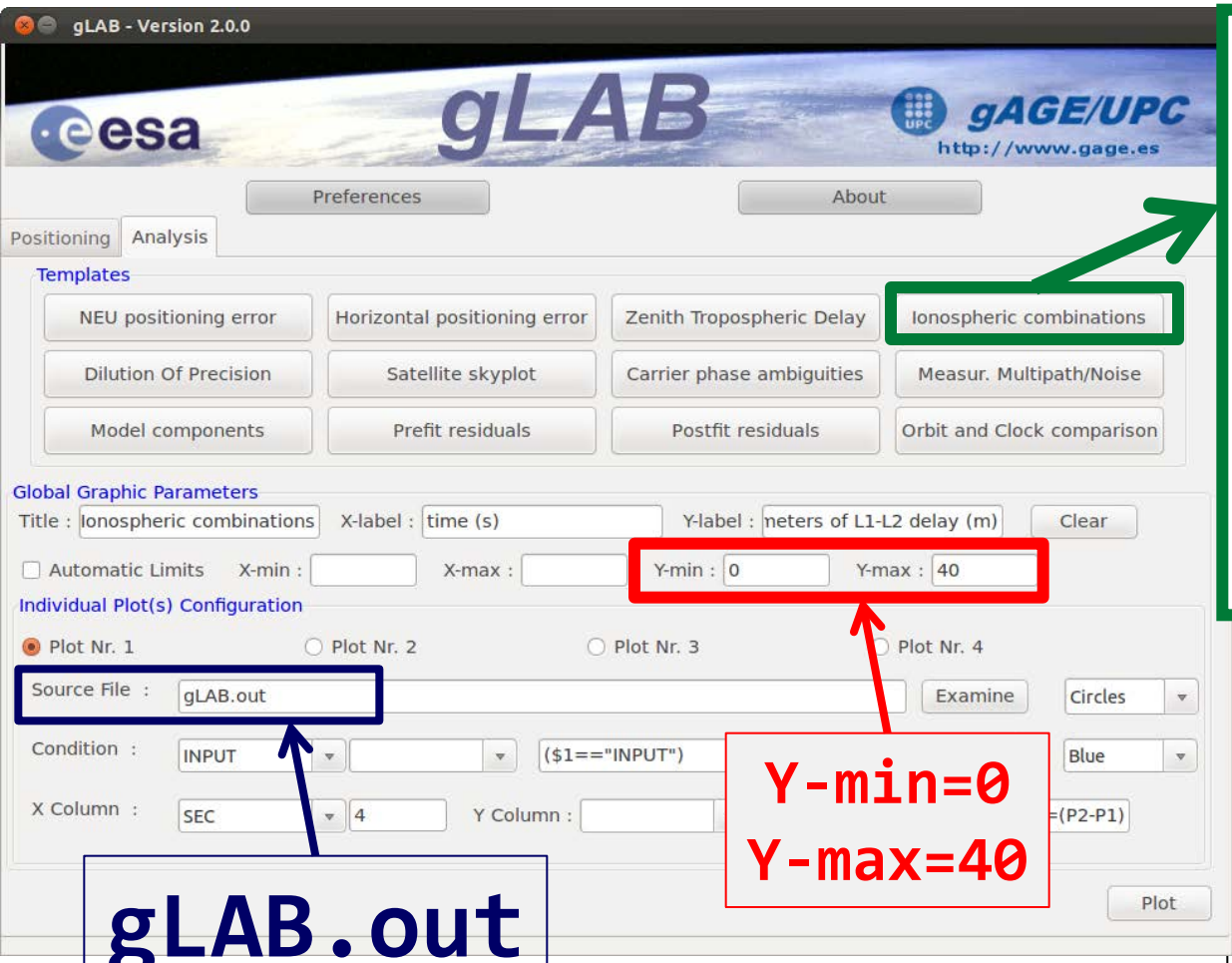


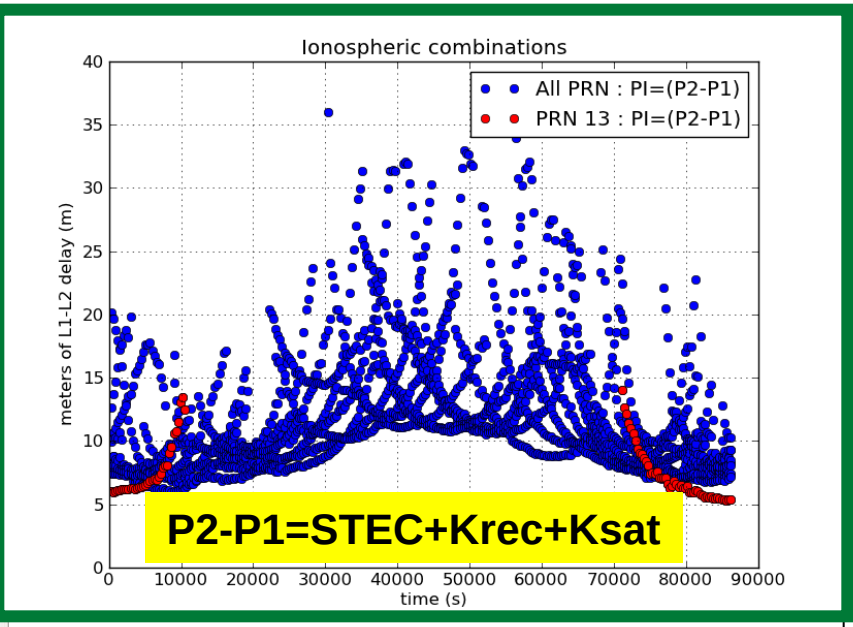


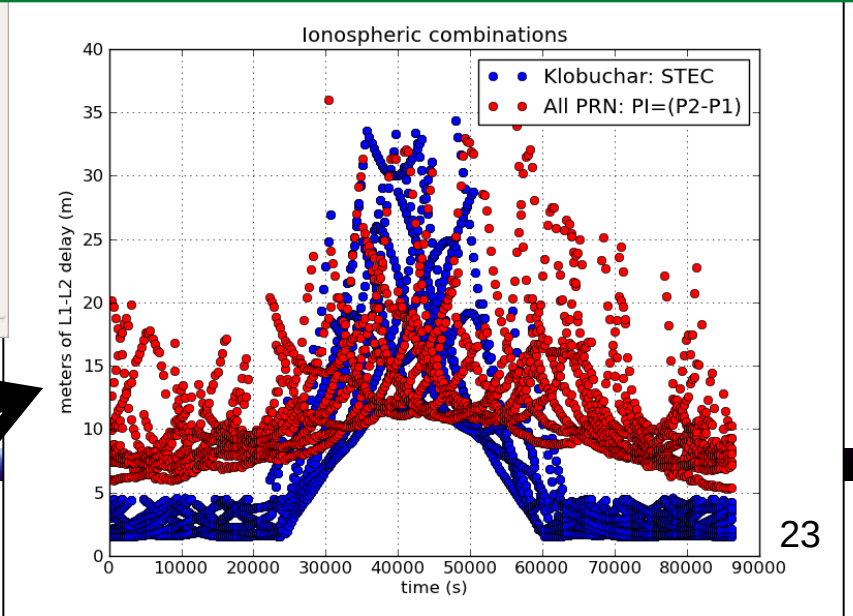
Ionosphere delays code and advances carrier measurements.

Note: Use the **gLAB.out** file. In **gLAB1.out** file this model component was switched off.

Example 1. Measur. (P2-P1) v.s. Model (Klobuchar)

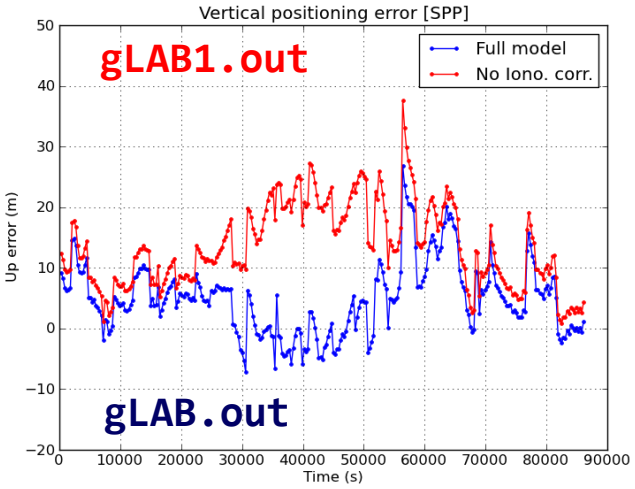


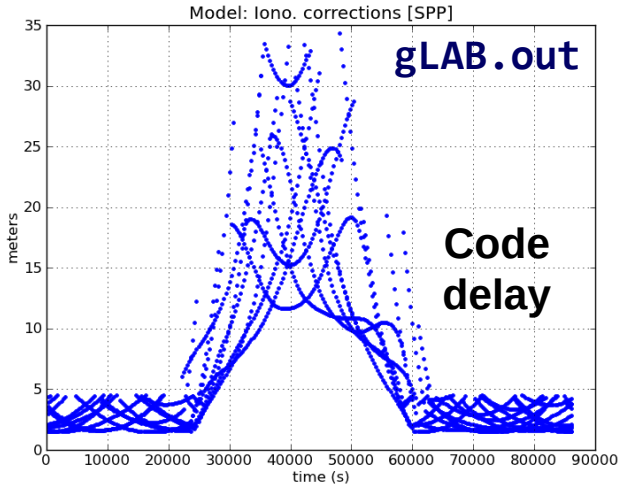


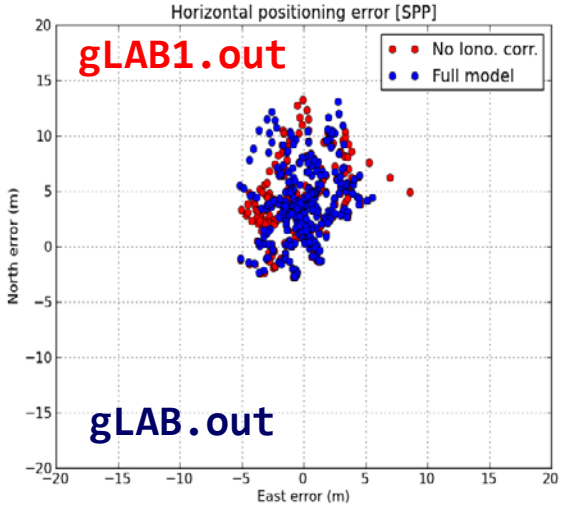


Plot Nr. 1: Klobuchar
Plot Nr. 2: P2-P1

Example 1. Summary: Klobuchar model performance







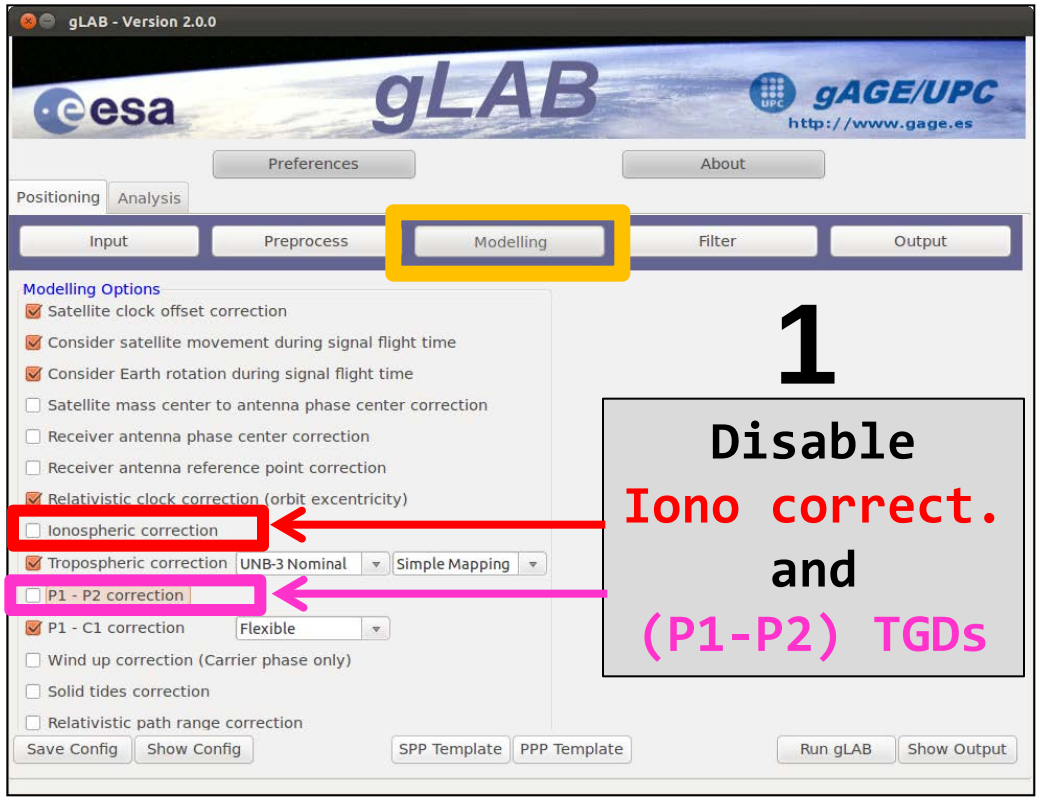
Ionospheric correction (broadcast Klobuchar)

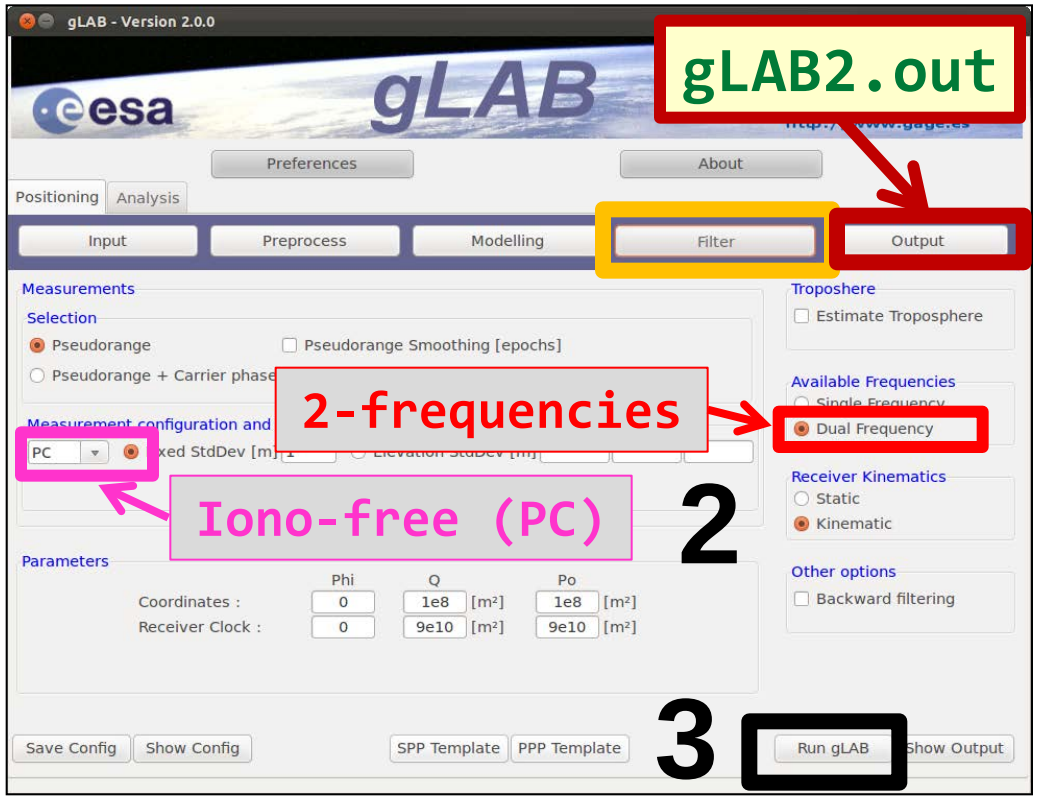
Ionospheric delays are larger at noon due to the higher illumination.

Large positioning errors (mainly in vertical) appear when neglecting ionospheric corrections.

Example 1. 2-frequency Ionosphere-free solution

From previous configuration set following options



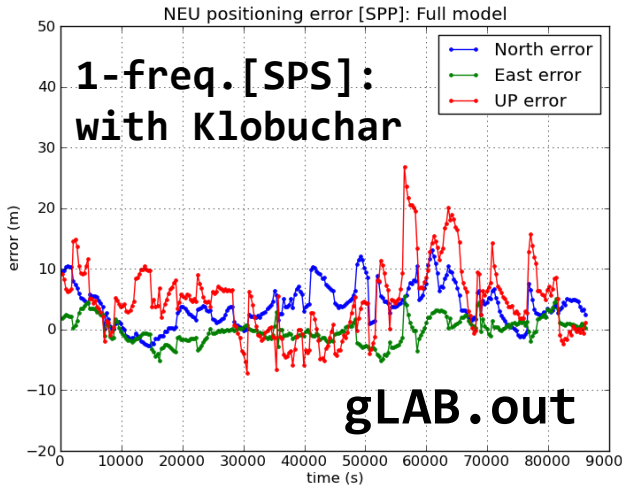


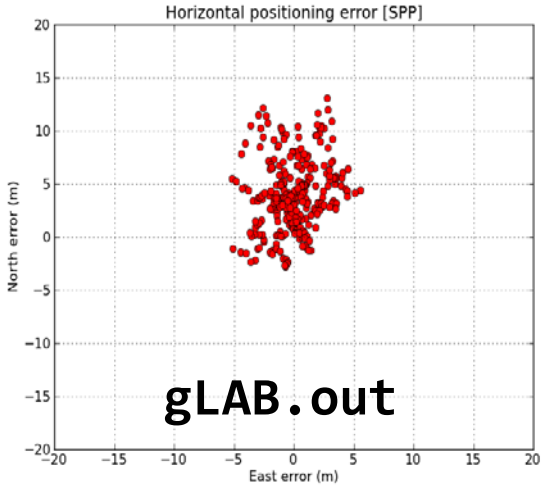
After running gLAB, plot results as in previous cases

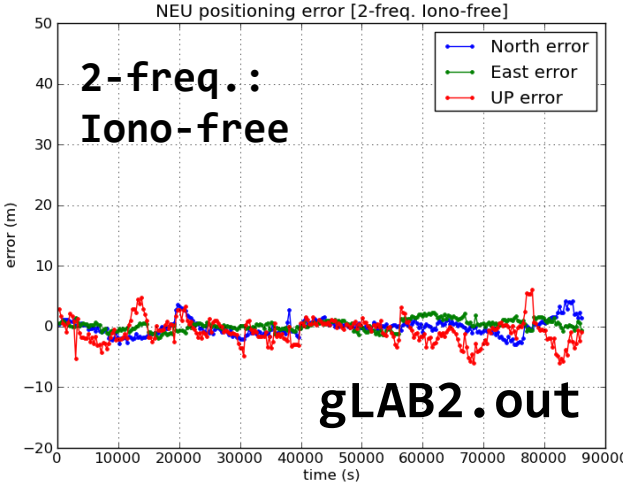
Equivalent command line sentence:

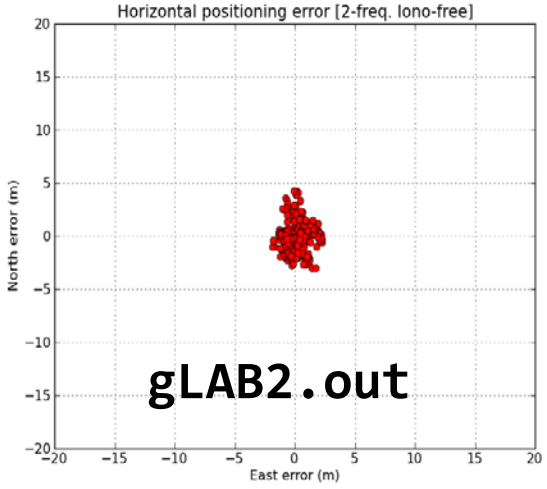
```
gLAB_linux -input:cfg gLAB_pc_IFree.cfg
           -input:obs ramo1250.00o -input:nav brdc1250.00n
```

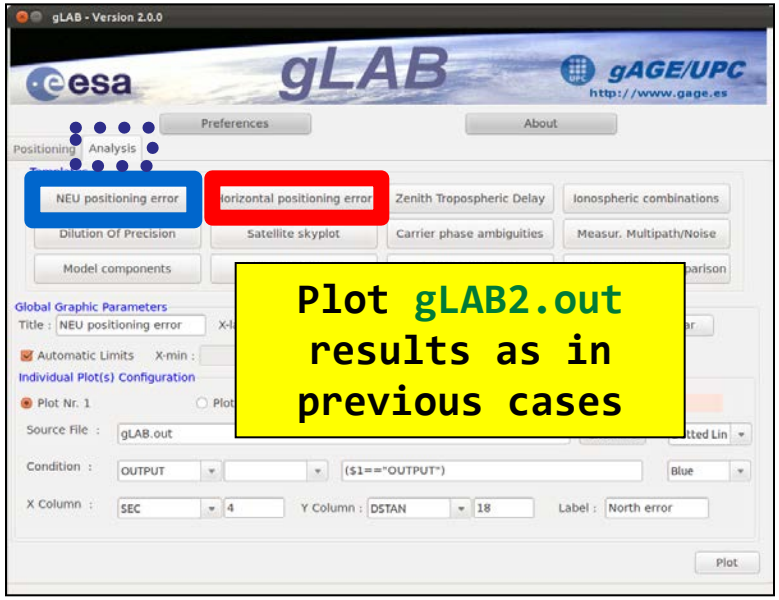
Example 1. Single-frequency vs. Dual-frequency

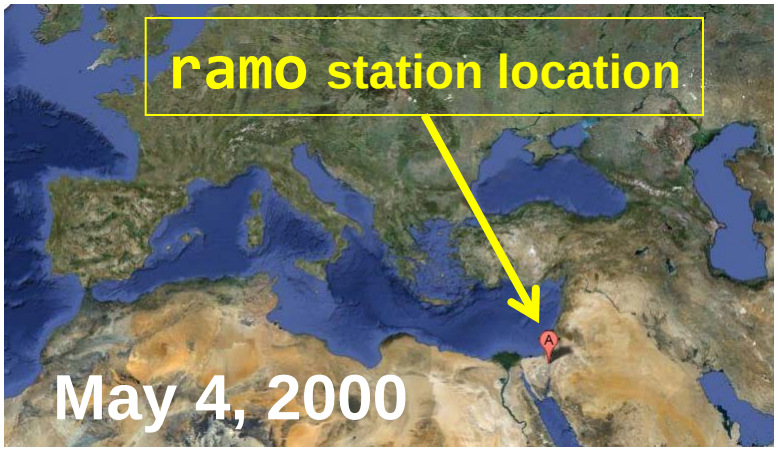












Example 1: Iono effects on single freq. Posit.

Ionospheric delay

The ionosphere extends from about *60 km* over the Earth's surface until more than *2000 km*, with a sharp electron density maximum at around *350 km*. The ionospheric refraction depends, among other things, on the location, local time and solar cycle (*11 years*).

- First order (~99.9%) ionospheric delay $I1$ depends on the inverse of squared frequency:

$$I1 = \frac{40.3}{f^2} STEC$$

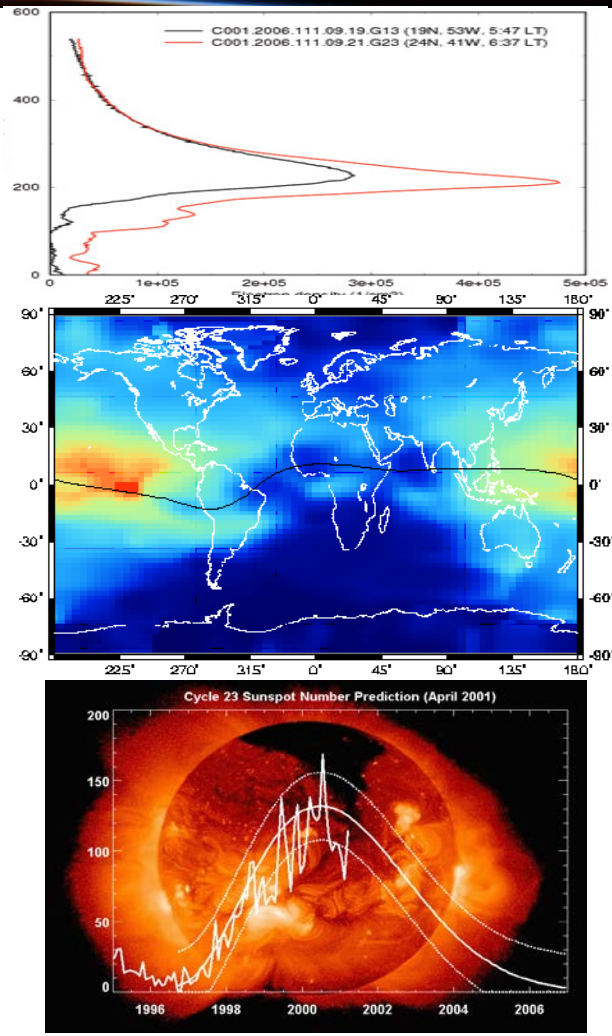
  where *STEC* is the number of electrons per area unit along ray path (STEC: Slant Total Electron Content).

$$STEC = \int N_e ds$$

- Two-frequency receivers can remove this error source (up to 99.9%) using ionosphere-free combination of pseudo-ranges (PC) or carriers (LC).

$$PC = \frac{f_1^2 P1 - f_2^2 P2}{f_1^2 - f_2^2}$$

- Single-frequency users can remove about a 50-70% of the ionospheric delay using the Klobuchar model, whose parameters are broadcast in the GPS navigation message.



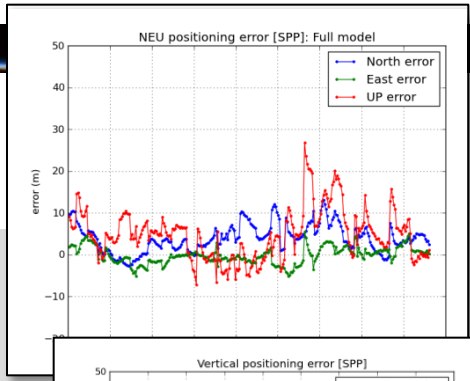
Example 1: Iono effects on single freq. Posit.

Annex:
gLAB processing in command line

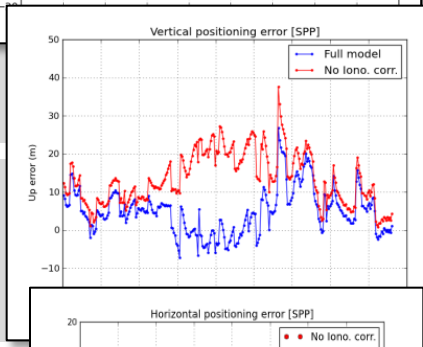
Example 1: gLAB processing in command line

Execute in a single line: (gnuplot can also be used)

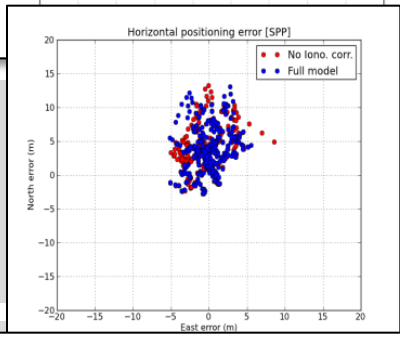
```
graph.py -f gLAB.out -x4 -y18 -s.- -c '($1=="OUTPUT")' -l "North error"
         -f gLAB.out -x4 -y19 -s.- -c '($1=="OUTPUT")' -l "East error"
         -f gLAB.out -x4 -y20 -s.- -c '($1=="OUTPUT")' -l "UP error"
                     --yn -20 --yx 50 --xl "time (s)" --yl "error (m)"
                      -t "NEU positioning error [SPP]: Full model"
```



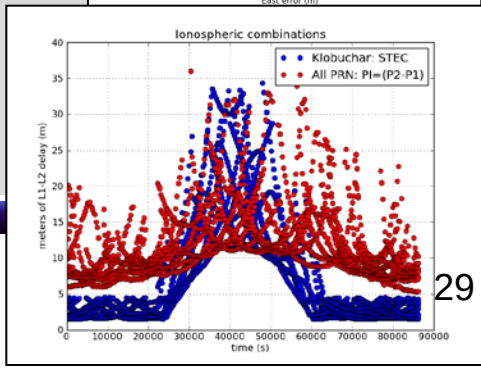

```
graph.py -f gLAB.out  -x4 -y20 -s.- -c '($1=="OUTPUT")' --l "Full model"
         -f gLAB1.out -x4 -y20 -s.- -c '($1=="OUTPUT")' --l "No Iono." --cl r
                      --yn -20 --yx 50 --xl "Time (s)" --yl "Up error (m)"
                      -t "Vertical positioning error [SPP]"
```



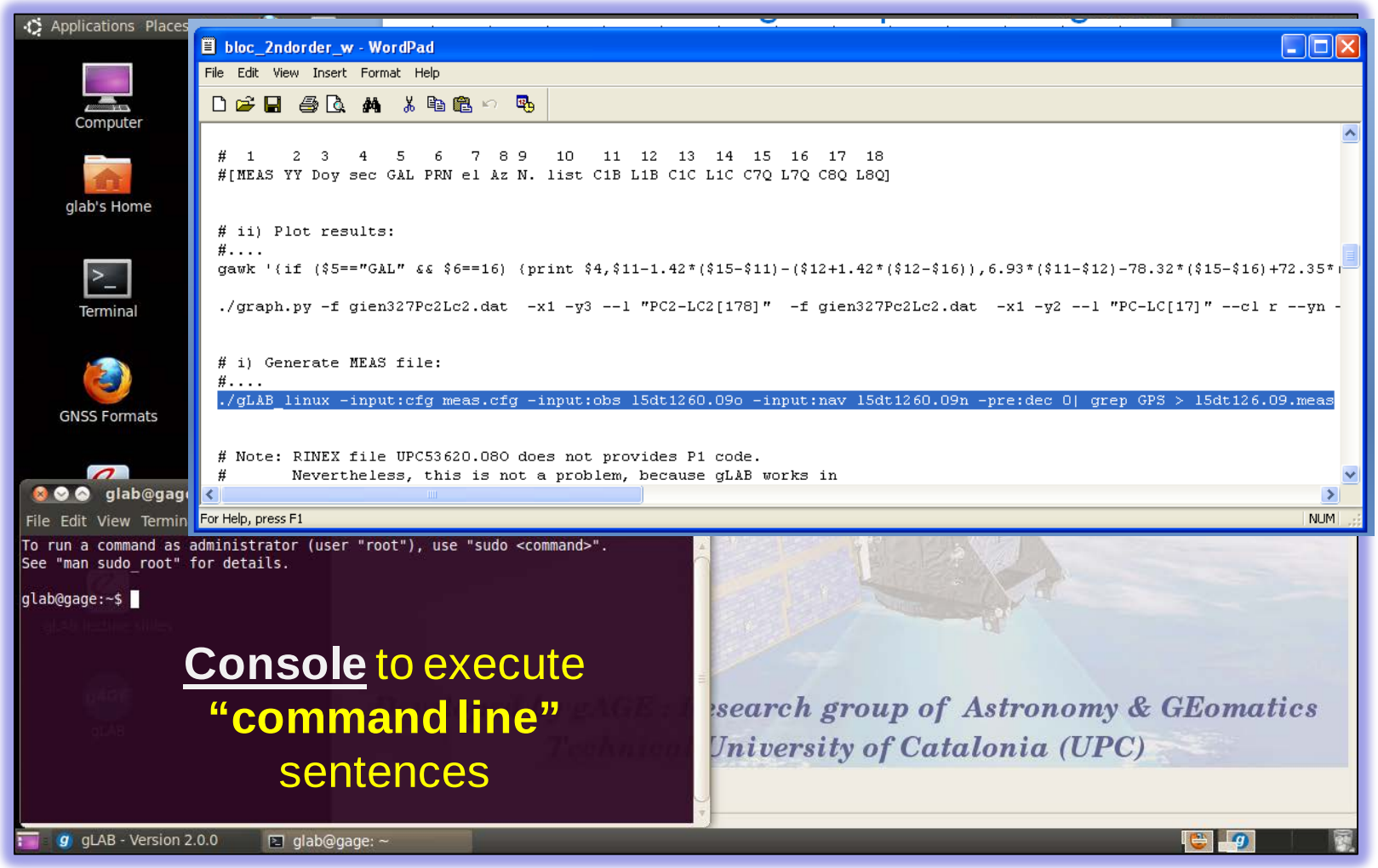

```
graph.py  -f gLAB1.out -x19 -y18 -so -c '($1=="OUTPUT")' --l "No Iono." --cl r
          -f gLAB.out  -x19 -y18 -so -c '($1=="OUTPUT")' --l "Full mod" --cl b
                       --xl "East error (m)" --yl "North error (m)"
                       --xn -20 --xx 20 --yn -20 --yx 20
                       -t "Horizontal pos. error [SPP]"
```




```
graph.py  -f gLAB.out -x4 -y25 -s. -c '($1=="MODEL")'
          -f gLAB.out -x4 -y'($10-$9)' -s. -c '($1=="INPUT")‘ --cl r
                      --xl "time (s)" --yl "meters"
                      --yn -0 --yx 40  -t "Ionospheric Combination"
```

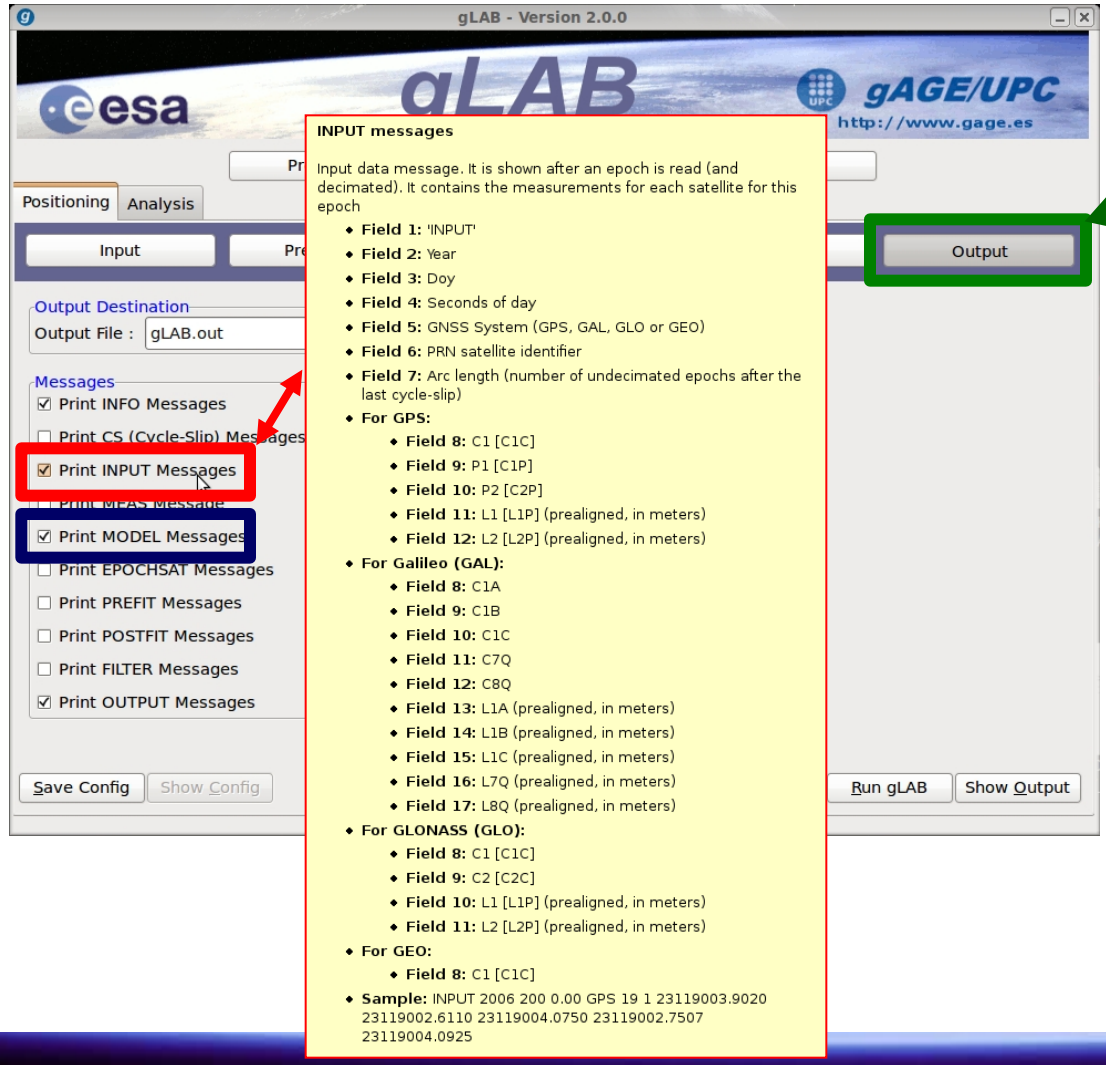


Example 1: gLAB processing in command line


Applications Places
Computer
glab's Home
Terminal
GNSS Formats
bloc_2ndorder_w - WordPad
File Edit View Insert Format Help
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18
#[MEAS YY Doy sec GAL PRN el Az N. list C1B L1B C1C L1C C7Q L7Q C8Q L8Q]
ii) Plot results:
#....
./graph.py -f gien327Pc2Lc2.dat -x1 -y3 --l "PC2-LC2[178]" -f gien327Pc2Lc2.dat -x1 -y2 --l "PC-LC[17]" --cl r --yn -
i) Generate MEAS file:
#....
./gLAB_linux -input:cfg meas.cfg -input:obs 15dt1260.09o -input:nav 15dt1260.09n -pre:dec 0| grep GPS > 15dt126.09.meas
Note: RINEX file UPC53620.08O does not provides P1 code.
Nevertheless, this is not a problem, because gLAB works in
For Help, press F1
NUM
File Edit View Termin
To run a command as administrator (user "root"), use "sudo <command>".
See "man sudo_root" for details.
glab@gage:~$
Console to execute "command line" sentences
research group of Astronomy & GEomatics
University of Catalonia (UPC)
gLAB - Version 2.0.0
glab@gage: ~

A "**notepad**" with the command line sentence is provided to facilitate the sentence writing: just "**copy**" and "**paste**" from notepad to the working terminal.

Example 1: gLAB processing in command line



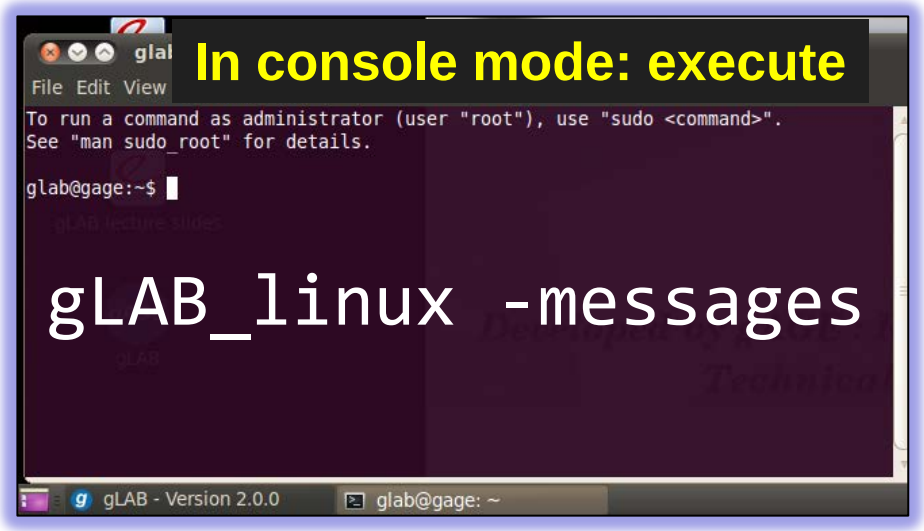
INPUT messages

Input data message. It is shown after an epoch is read (and decimated). It contains the measurements for each satellite for this epoch

- **Field 1:** 'INPUT'
- **Field 2:** Year
- **Field 3:** Doy
- **Field 4:** Seconds of day
- **Field 5:** GNSS System (GPS, GAL, GLO or GEO)
- **Field 6:** PRN satellite identifier
- **Field 7:** Arc length (number of undecimated epochs after the last cycle-slip)
- **For GPS:**
  - **Field 8:** C1 [C1C]
  - **Field 9:** P1 [C1P]
  - **Field 10:** P2 [C2P]
  - **Field 11:** L1 [L1P] (prealigned, in meters)
  - **Field 12:** L2 [L2P] (prealigned, in meters)
- **For Galileo (GAL):**
  - **Field 8:** C1A
  - **Field 9:** C1B
  - **Field 10:** C1C
  - **Field 11:** C7Q
  - **Field 12:** C8Q
  - **Field 13:** L1A (prealigned, in meters)
  - **Field 14:** L1B (prealigned, in meters)
  - **Field 15:** L1C (prealigned, in meters)
  - **Field 16:** L7Q (prealigned, in meters)
  - **Field 17:** L8Q (prealigned, in meters)
- **For GLONASS (GLO):**
  - **Field 8:** C1 [C1C]
  - **Field 9:** C2 [C2C]
  - **Field 10:** L1 [L1P] (prealigned, in meters)
  - **Field 11:** L2 [L2P] (prealigned, in meters)
- **For GEO:**
  - **Field 8:** C1 [C1C]
- **Sample:** INPUT 2006 200 0.00 GPS 19 1 23119003.9020 23119002.6110 23119004.0750 23119002.7507 23119004.0925

The different messages provided by gLAB and its content can be found in the [OUTPUT] section.

By placing the mouse on a given message name, a tooltip appears describing the different fields.


In console mode: execute
File Edit View
To run a command as administrator (user "root"), use "sudo <command>".
See "man sudo_root" for details.
glab@gage:~$
gLAB_linux -messages
gLAB - Version 2.0.0
glab@gage: ~

Example 2: Ionospheric delay analysis

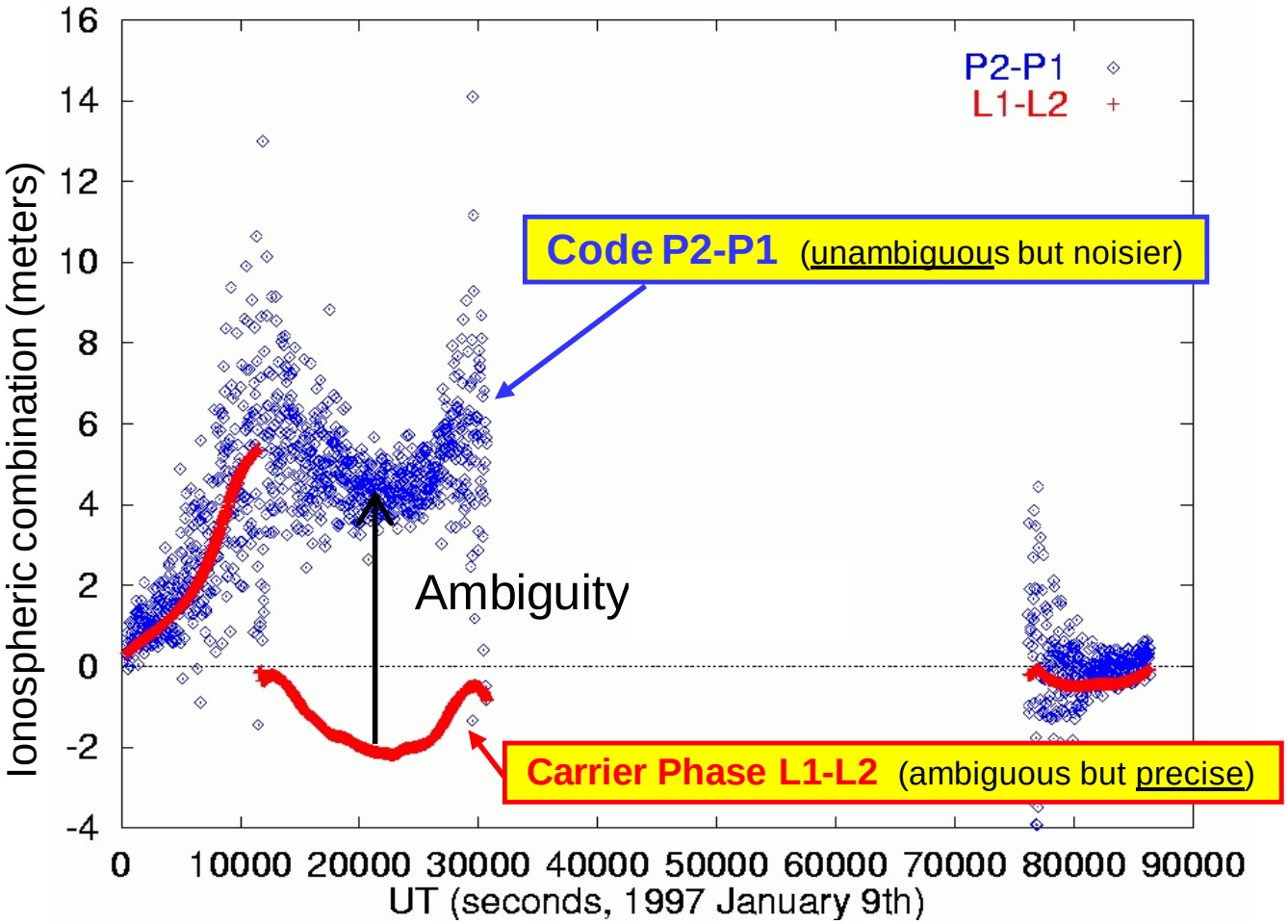
Example 2: Depict the ionospheric delays for the different satellites in view from station amc2

- This is a simple exercise aimed to illustrate how to use gLAB to easily analyze GNSS measurements and their combinations.
- gLAB will used to read the RINEX measurements file and to generate a "text" with the measurements provided in a columnar format (more suitable to make plots).
- From "text" file, compute and plot the *Ionospheric delay* for a given satellite, by using code and carrier measurements at *f1, f2*:

$$P_I \equiv P_2 - P_1 = I + K_{21}$$
$$L_I \equiv L_1 - L_2 = I + Ambiguity$$

$$P_1 - L_1 = 2\tilde{\alpha}_1 I + ambiguity1$$
$$P_2 - L_2 = 2\tilde{\alpha}_2 I + ambiguity2$$

Example 2: Ionospheric delay analysis



The target is to generate this plot to depict the ionospheric delay from code & carrier data

$$P_I \equiv P_2 - P_1 = I + K_{21}$$
$$L_I \equiv L_1 - L_2 = I + Ambiguity$$

$$P_1 - L_1 = 2\tilde{\alpha}_1 I + ambiguity1$$

$$P_2 - L_2 = 2\tilde{\alpha}_2 I + ambiguity2$$

$$\tilde{\alpha}_1 = \frac{1}{\gamma_{21} - 1} = 1.546\,; \quad \tilde{\alpha}_2 = 1 + \tilde{\alpha}_1$$

$$\gamma_{21} = \left(f_1 / f_2 \right)^2 = (154/120)^2$$

Example2: GPS measurements content

Code measurement content

$$P_1 = \rho + \tilde{\alpha}_1 \left(I + K_{21} \right) + \varepsilon_1$$
$$P_2 = \rho + \tilde{\alpha}_2 \left(I + K_{21} \right) + \varepsilon_2$$

Carrier measurement content

$$L_1 = \rho - \tilde{\alpha}_1 I + B_1 + \varsigma_1$$
$$L_2 = \rho - \tilde{\alpha}_2 I + B_2 + \varsigma_2$$

$$\tilde{\alpha}_2 - \tilde{\alpha}_1 = 1$$
$$\tilde{\alpha}_1 = \frac{1}{\gamma_{21} - 1} = 1.546$$
$$\gamma_{21} = \left(f_1 / f_2 \right)^2$$

ρ Refers to all non dispersive terms: geometric range, clocks, tropo. delay… (see [R-1]).

Ionospheric delay

$$I = \frac{40.3\left(f_1^{\,2} - f_2^{\,2} \right)}{f_1^{\,2} f_2^{\,2}} 10^{16} STEC \text{; } (I \text{ is in } m \text{ of } L_1 - L_2 \text{ delay})$$

$$STEC = \int_{rec}^{sat} N_e dl, \quad (STEC \text{ is in } TECUs)$$

$$1\,TECU = 10^{16} e^- / m^2 = 0.10m \text{ of } L1\text{-}L2 \text{ delay}$$

Interfrequency bias

$$K_{21} = K_{21,rec} - K_{21}^{sat}$$

As the satellite clocks are referred to the ionosphere-free combination of codes (P_C), the K_{21}^{sat} cancels in such combination.

Note: $TGD = -\tilde{\alpha}_1 K_{21}^{sat}$ is broadcast in GPS nav. Message.

$$P_C = \frac{f_1^{\,2} P_1 - f_2^{\,2} P_2}{f_1^{\,2} - f_2^{\,2}}$$

Carrier ambiguities

$$B_i = \lambda_i N_i + b_i$$

N_i is an integer number. b_i is a real number (fractional part of ambiguity)

Example 2: Ionospheric delay analysis

1.- **Read RINEX** file with **gLAB** and generate a "measurements file" in a **columnar format** (the easiest to manipulate and plot content):

→ **Using** the configuration file **meas.cfg**, READ the RINEX and generate the MEAS file:

```
gLAB_linux -input:cfg meas.cfg -input:obs coco0090.97o -input:nav brdc0090.97n > coco.meas
```

gLAB configuration file

```
-pre:dec 1
-print:none
-print:meas

--model:satphasecenter
--model:recphasecenter
--model:satclocks
--pre:cs:li
--pre:cs:bw
```

RINEX Measurement file

RINEX Navigation file

OUTPUT: measurement file in columnar format

```
[Id YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2P L2P]
 1  2  3   4   5    6  7   8  9  10   11  xx  xx  14  15 16 ]
```

Example 2: Ionospheric delay analysis

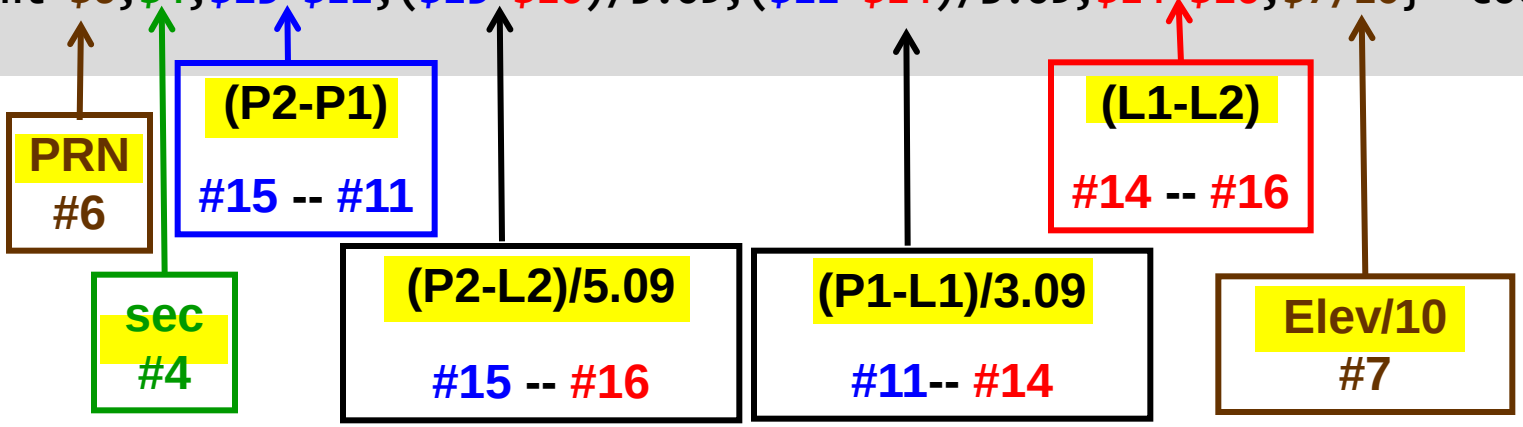
2.- **Manipulate the file** with the easy & powerful awk (or **gawk**) programming language (to compute the combinations of measurements):

→ From `coco.meas` file:

```
                                                    P1                    L1   P2   L2 ]
[Id YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2P L2P]
 1  2  3   4   5   6  7   8  9  10  11  xx  xx  14  15  16
```

Compute different ionospheric combination of codes and carriers, and generate the **obs.txt** file containing the fields: **[PRN,sec, P2-P1, (P2-L2)/5.09, (P1-L1)/3.09, L1-L2, Elev/10]**

```
gawk '{print $6,$4,$15-$11,($15-$16)/5.09,($11-$14)/3.09,$14-$16,$7/10}' coco.meas >
                                                                        obs.txt
```



Example 2: Ionospheric delay analysis

3.-Plot results with "graph.py" (you can use the gnuplot as well)

→From obs.txt file:

```
[PRN, sec, P2-P1, (P2-L2)/5.09, (P1-L1)/3.09, L1-L2, Elev/10]
  1    2     3         4              5          6      7
```

Show in the same plot the following iono. delays for satellite **PRN01**:

P2-P1, (P2-L2)/5.09, (P1-L1)/3.09, L1-L2, Elev./10

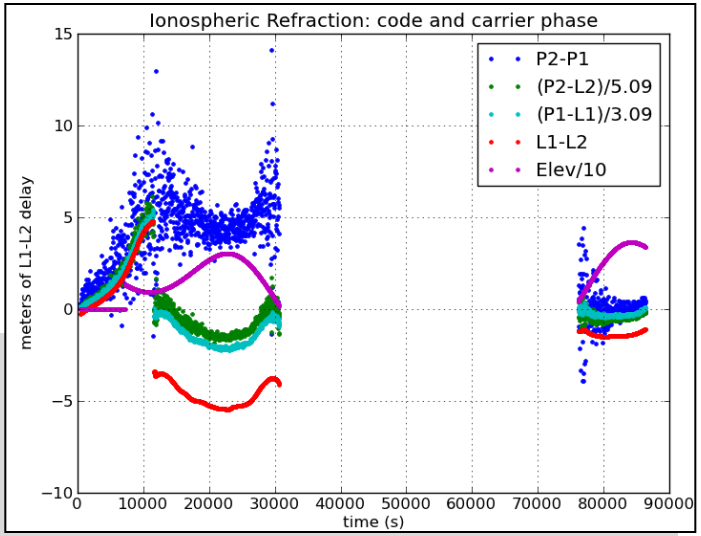
Condition:
Select PRN01
(from 1-st field)

Fields to plot:
#2 (x-axis)
versus
#3 (y-axis)

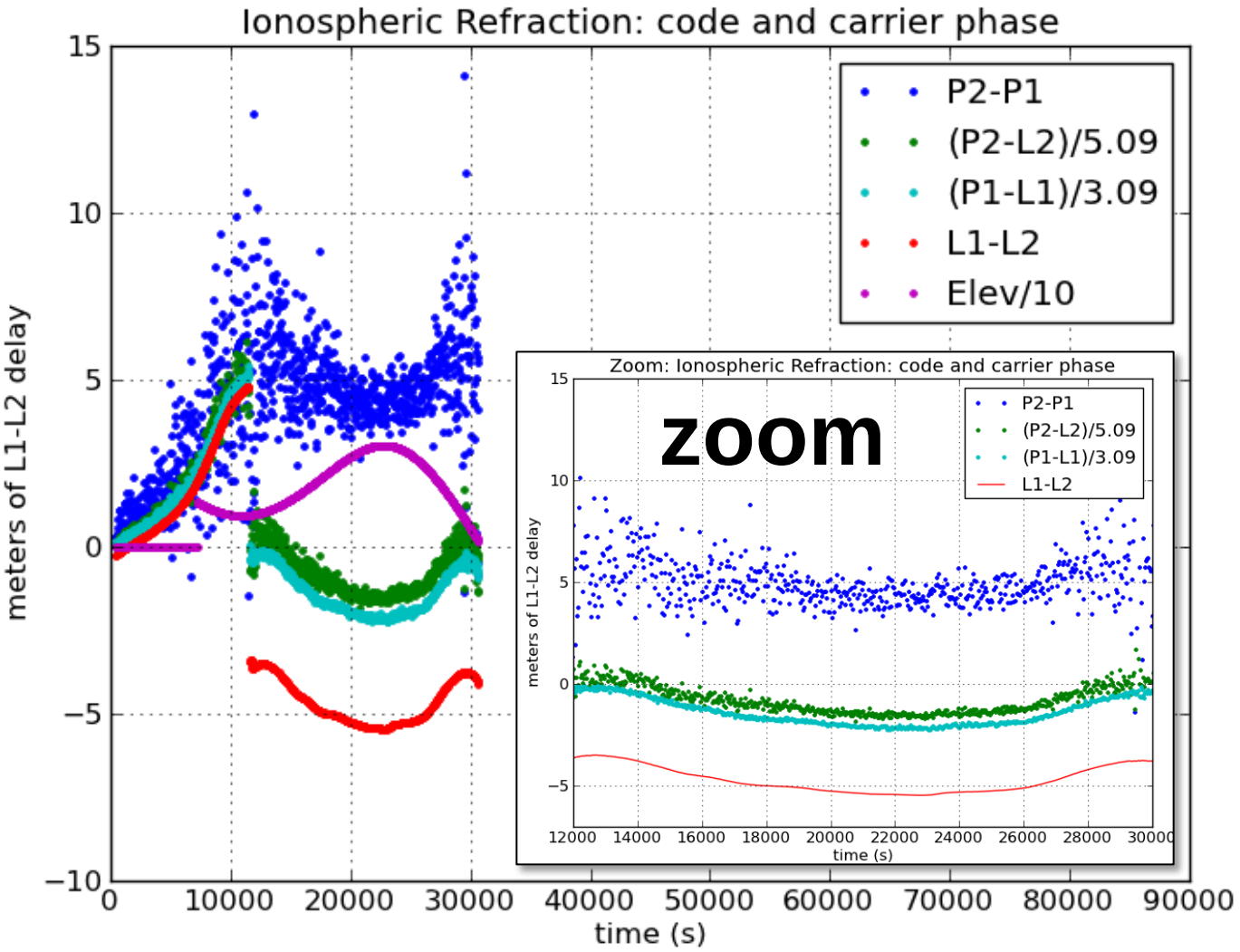
Label:
P2-P1

File to plot

```
graph.py -f obs.txt -c'($1==01)' -x2 -y3 --l "P2-P1"
         -f obs.txt -c'($1==01)' -x2 -y4 --l "(P2-L2)/5.09"
         -f obs.txt -c'($1==01)' -x2 -y5 --l "(P1-L1)/3.09"
         -f obs.txt -c'($1==01)' -x2 -y6 --l "L1-L2"
         -f obs.txt -c'($1==01)' -x2 -y7 --l "Elev/10"
         --yn -10 --yx 15 --xl "time (s)" --yl "meters of L1-L2 delay"
```



Example 2: Ionospheric delay analysis



$$P_I \equiv P_2 - P_1 = I + K_{21}$$
$$L_I \equiv L_1 - L_2 = I + Ambiguity$$

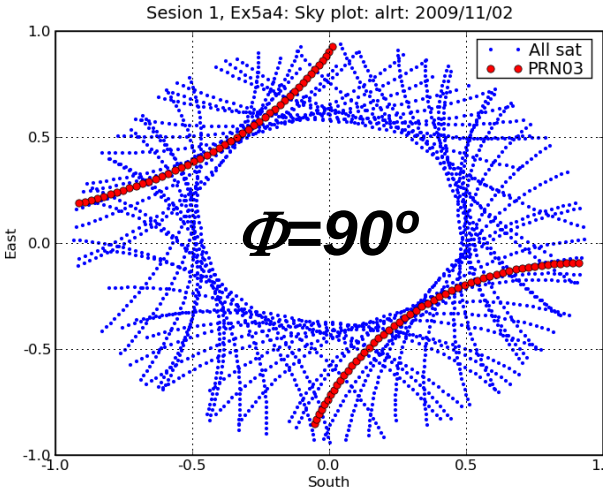
$$P_1 - L_1 = 2\tilde{\alpha}_1 I + ambiguity1$$

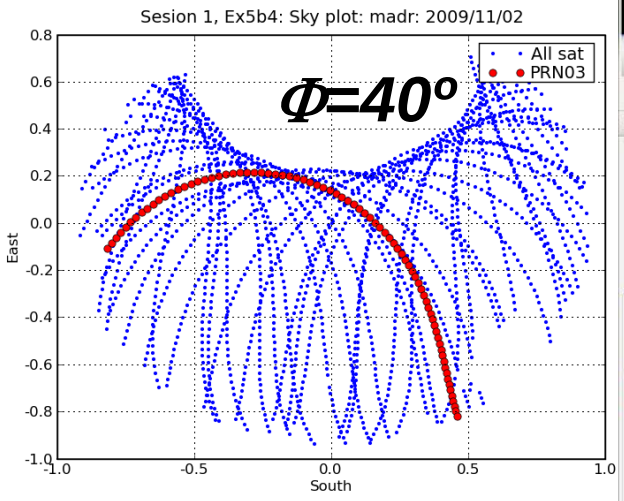
$$P_2 - L_2 = 2\tilde{\alpha}_2 I + ambiguity2$$

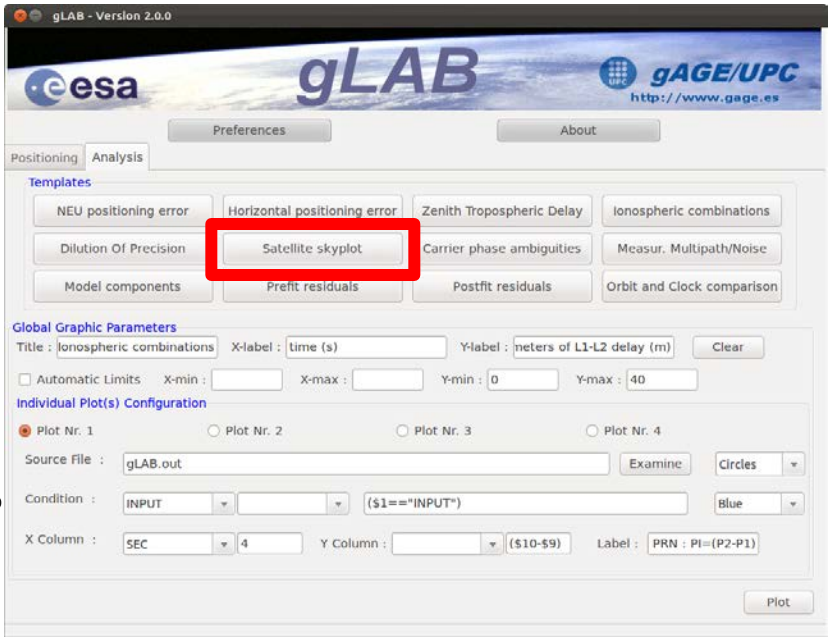
$$\tilde{\alpha}_1 = \frac{1}{\gamma_{21} - 1} = 1.546\,; \quad \tilde{\alpha}_2 = 1 + \tilde{\alpha}_1$$

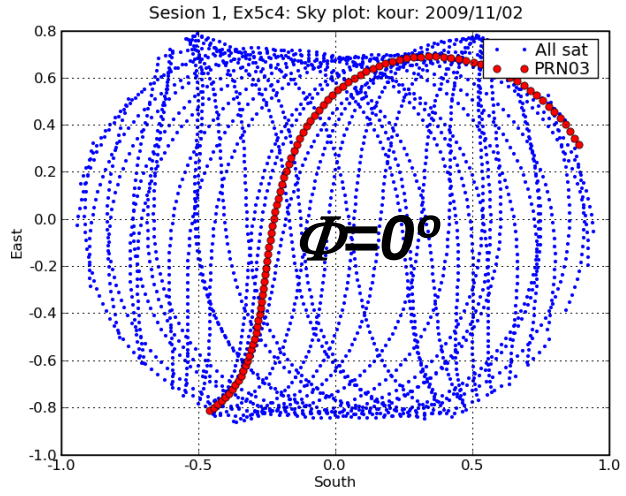
$$\gamma_{21} = \left(f_1 / f_2 \right)^2 = (154/120)^2$$

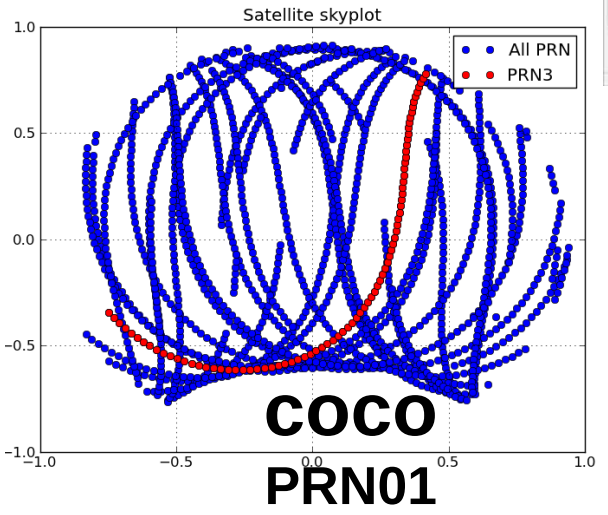
Example 2: Sky plots







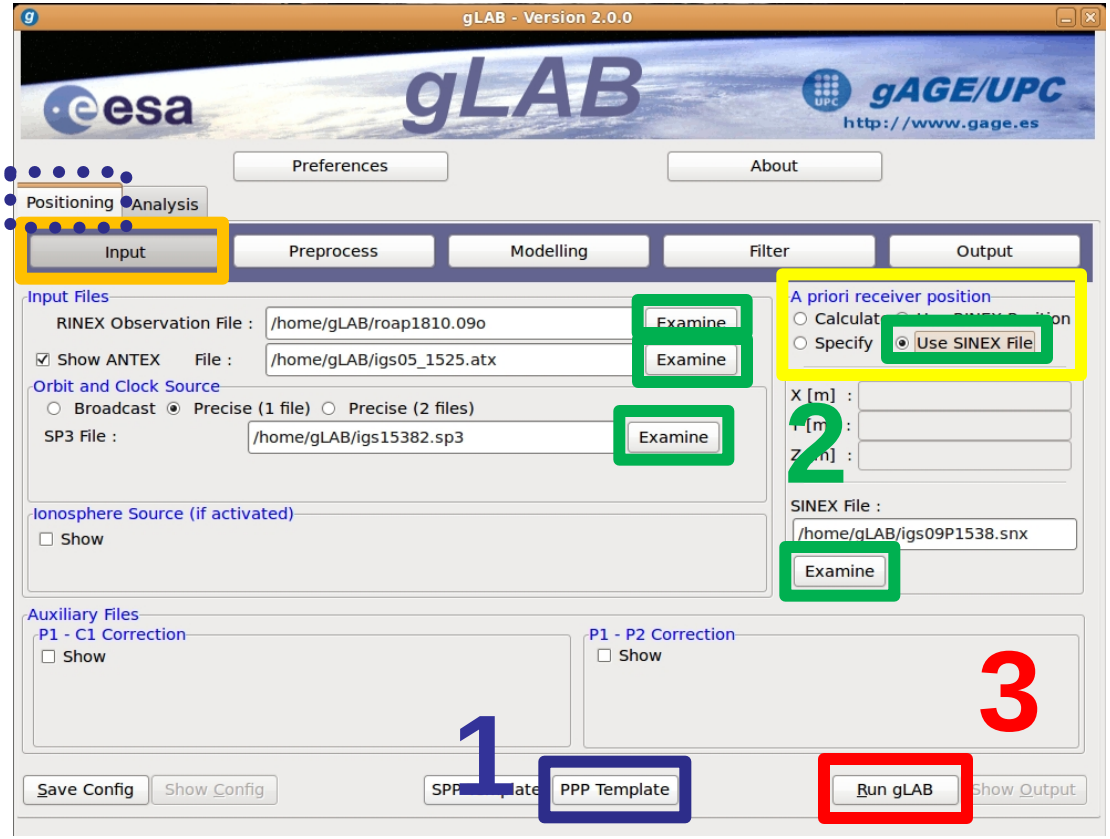




Sky plots at different latitudes

Example 3: Zenith Troposphere Delay estimation

PPP Template: Static positioning with dual freq. code & carrier (ionosphere-free combination PC,LC) + post-processed precise orbits & clocks.



1. Select the **PPP Template**
2. **Upload data** files:
   - -Measurement : `roap1810.09o`
   - - ANTEX: `igs05_1525.atx`
   - - Orbits & clocks: `igs15382.sp3`
   - - SINEX: `igs09P1538.snx`
3. **RUN** gLAB

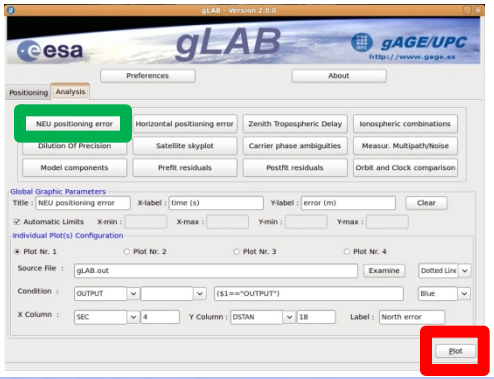
Default output file:

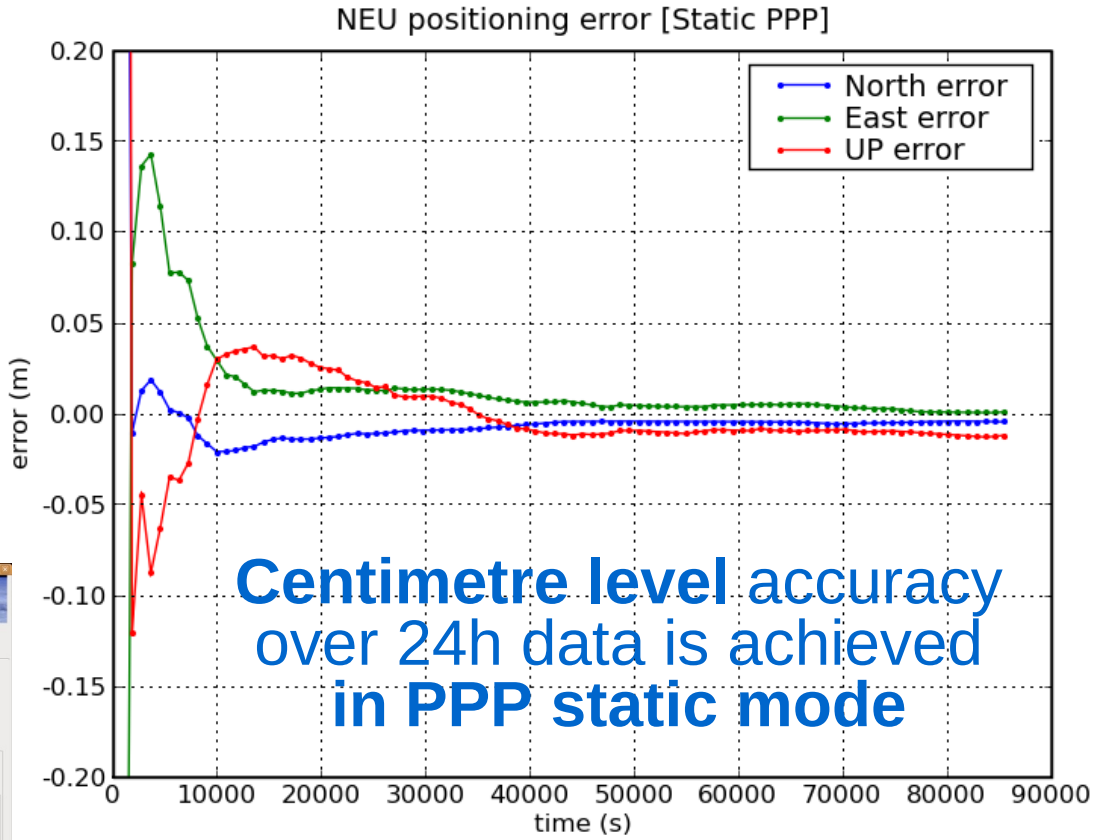
gLAB.out

Example 3: Zenith Troposphere Delay estimation

Plotting Results

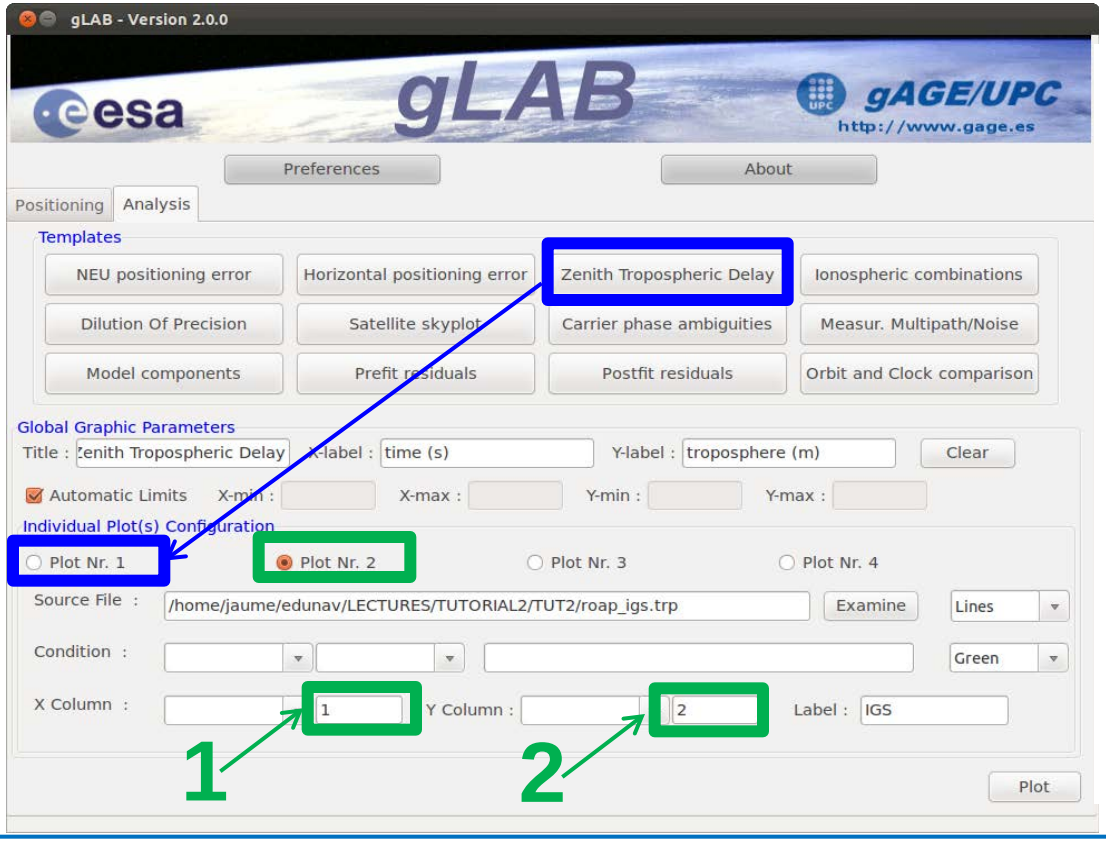
- Coordinates are taken as constants in nav. filter.
- Dual frequency Code and Carrier measurements.
- Precise orbits and clocks.
- Measurements modelling at the centimetre level.

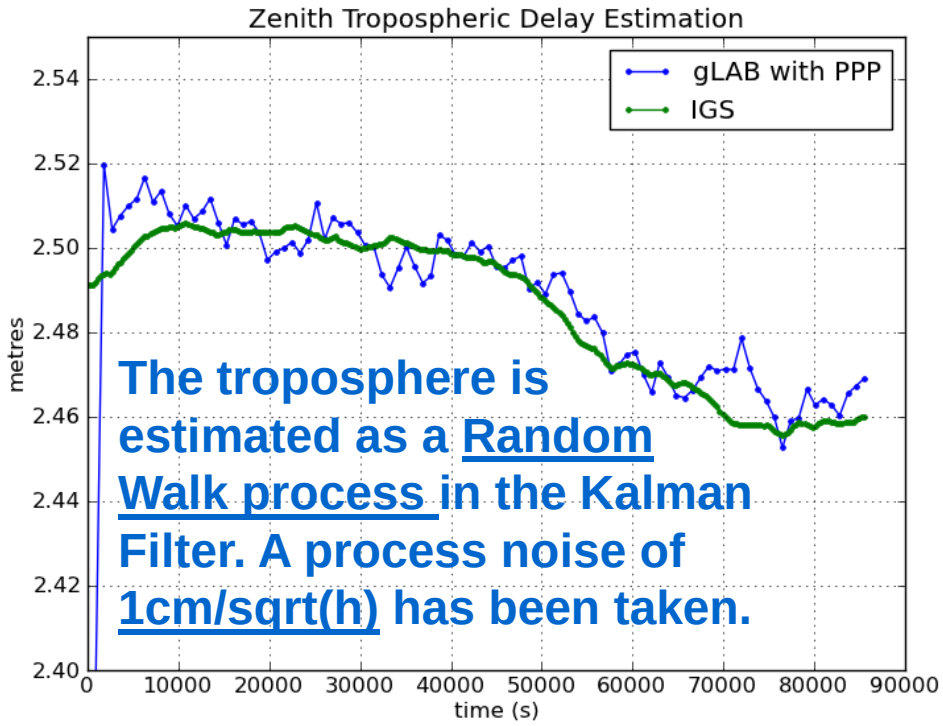




Centimetre level accuracy over 24h data is achieved **in PPP static mode**

Example 3: Zenith Troposphere Delay estimation





ftp://cddis.gsfc.nasa.gov/pub/gps/products/troposphere/new/2009/181/roap1810.09zpd.gz

The ZTD in this file is given in mm of delay. Thus, it is converted to m to compare with gLAB results

grep ROAP roap1810.09zpd | gawk -F\: '{print $3} ' | gawk '{print $1,$2/1000}' > roap_igs.trp

Example 3: Zenith Troposphere Delay estimation

Tropospheric delay

The troposphere is the atmospheric layer situated between the Earth's surface and an altitude of about 50 km.

The effect of the troposphere on GNSS signals appears as an extra delay in the measurement of the signal travelling from satellite to receiver.

The tropospheric delay does not depend on frequency and affects both the pseudo-range (code) and carrier phases in the same way. It can be modeled by:

- A hydrostatic component, composed of dry gases (mainly nitrogen and oxygen) in hydrostatic equilibrium. This component can be treated as an ideal gas. Its effects vary with the temperature and atmospheric pressure in a reasonably predictable manner, and it is responsible for about 90% of the delay.
- A wet component caused by the water vapor condensed in the form of clouds. It depends on the weather conditions and varies faster than the hydrostatic component and in a totally random way. For high accuracy positioning, this component must be estimated together with the coordinates and other parameters in the navigation filter.

OVERVIEW

- Introduction
- The gLAB tool suite
- Examples of GNSS processing using gLAB
- Laboratory session organization

LABORATORY Session

- Starting up your laptop
- **Basic:** Introductory lab exercises: Iono & Posit, SF, storm,TIDs
- **Medium:** Laboratory Work Projects: LWP1 to LWP4
- **Advanced:** Homework

Laboratory session organization

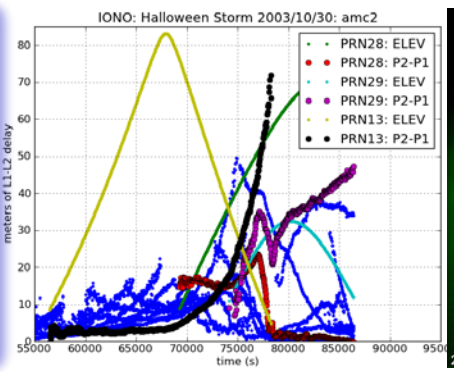
- The laboratory session is organized as an **assisted activity** where a set of **exercises must be developed individually or in groups of two**.
- As they are conceived as self-learning work, a detailed guide is provided in the slides (pdf file) to carry out the exercises.
- A notepad file with the command line instructions is also provided to help the sentence writing (doing copy & paste).
- A set of questions is presented, and the answers are also included in the slides.
- Teachers will attend individual (or collective) questions that could arise during exercise resolution.

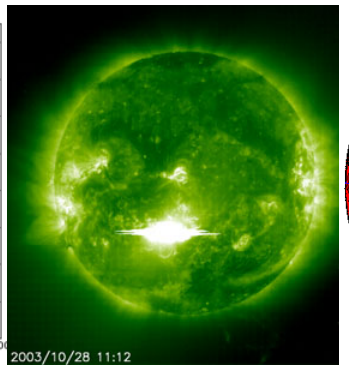
Laboratory session organization

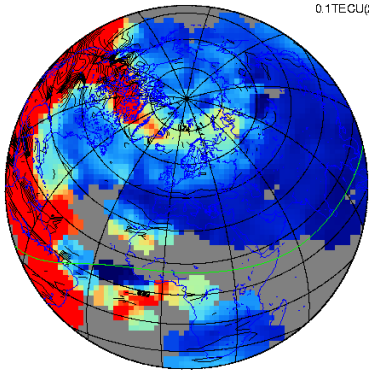
- The exercises are organized at **three different levels of difficulty**. The student can choose the level of exercises to do, although at least one introductory exercise is recommended to learn basic **gLAB** usage.

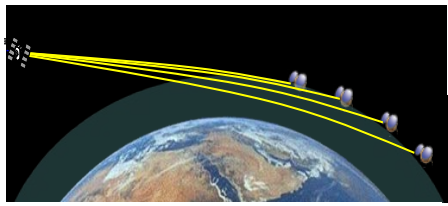
- **1. Basic: Introductory exercises. From 1 to 6.**

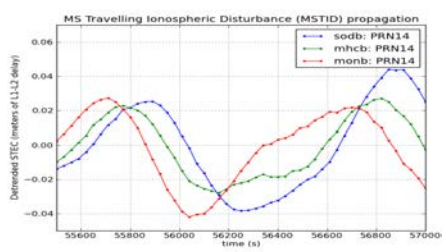
  They consist of simple exercises to: 1) Study the Ionosphere effects on single frequency positioning. 2) To depict the STEC on a Radio occulation 3) Solar Flare effect on TEC, 4,5) TEC evolution during the Halloween Storm, 6) To depict a TID propagaction.











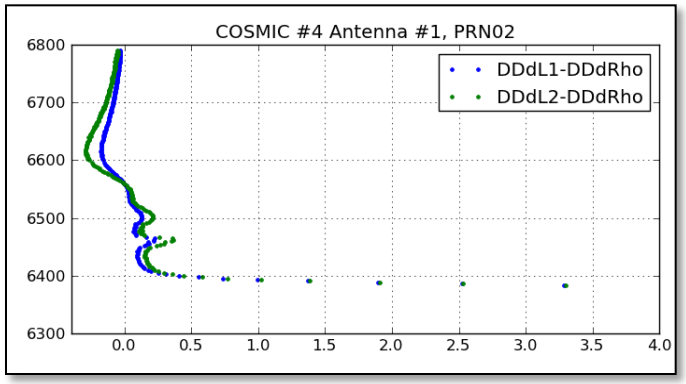
Laboratory session organization

2. Medium: Laboratory Work Projects (LWP).

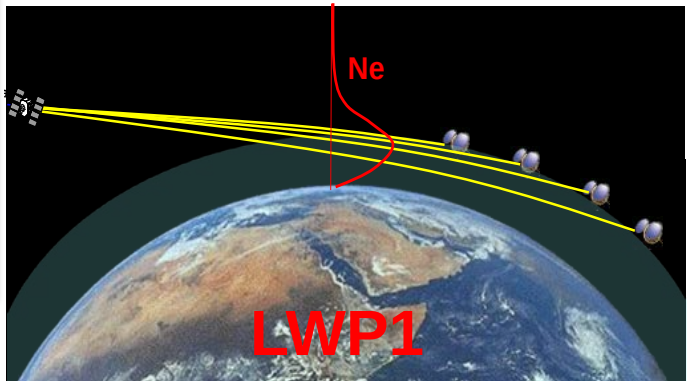
Four different LWP are proposed (to choose from):

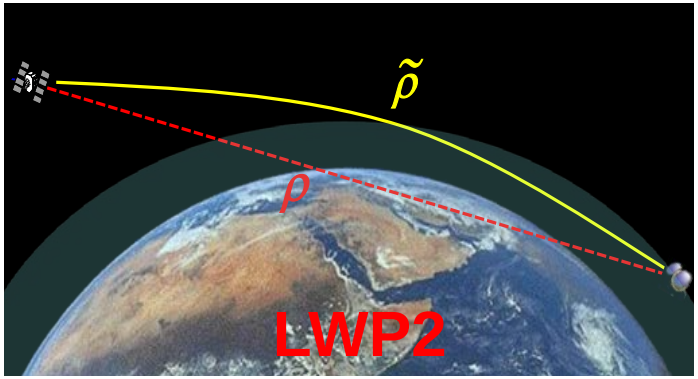
- **LWP1**: To show a simple numerical method to estimate electron density profiles (Ne(h)) from RO data.
- **LWP2**: To analyse the phase excess rate from GPS to LEO due to atmospheric (ionosphere & troposphere) bending.

Actual measurements from FORMOSAT-3/COSMIC LEOs will be used



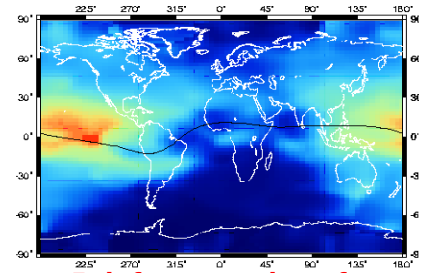
A minimum knowledge of UNIX (e.g., awk) would be desirable





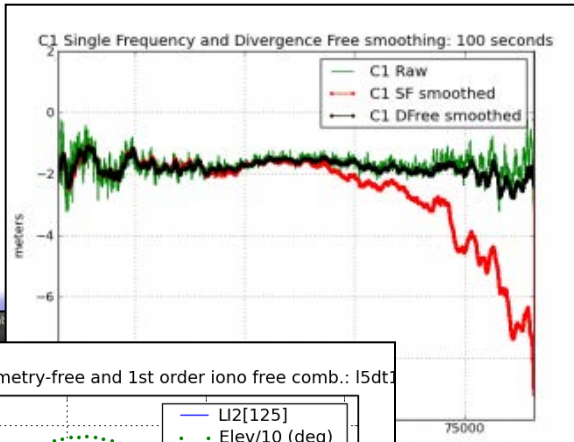
Laboratory session organization

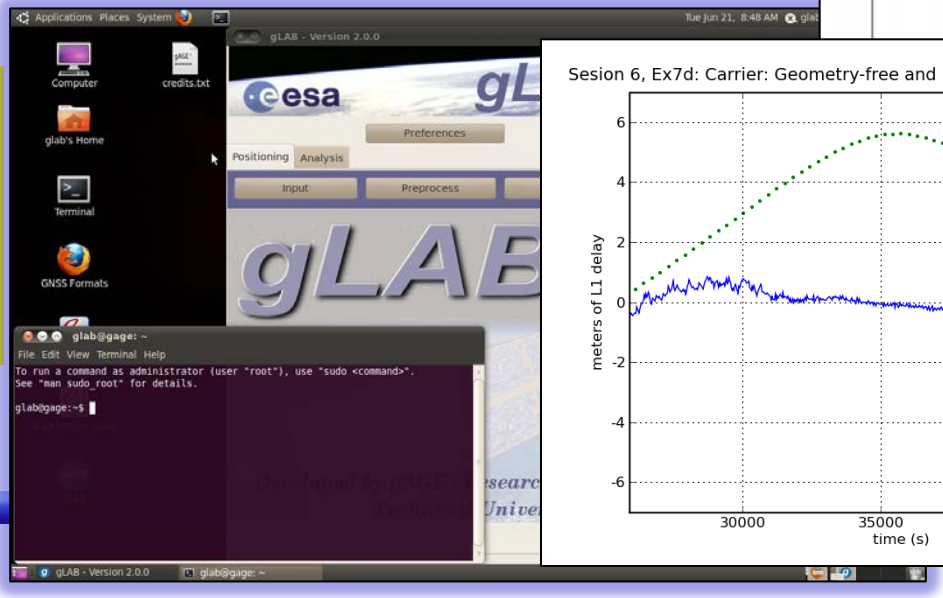
2. Medium: Laboratory Work Projects (LWP).

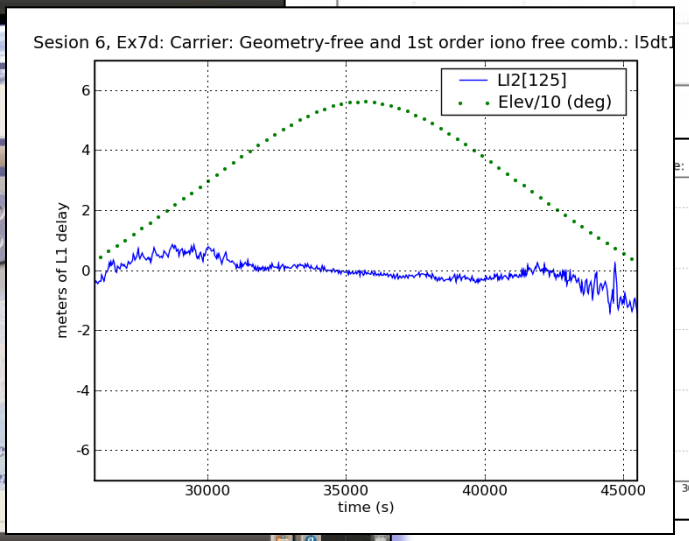


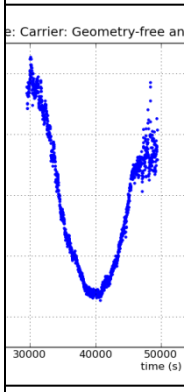
Four different LWP are proposed (to choose from):

- **LWP3**: To study the code-carrier ionosphere divergence effect on single-frequency carrier smoother code.
- **LWP4**: To analyse if second-order ionospheric effects can be depicted from three-frequency GNSS measurements.









Given that session time is limited to 3h, students who feel comfortable using gLAB, can skip part of the previous basic exercises (Ex1, Ex2,..) and jump to the Lab. Work Project.

A minimum knowledge of UNIX (e.g., awk) would be desirable

Laboratory session organization

3 . **Advanced:** Labeled as **"Homework exercises"**

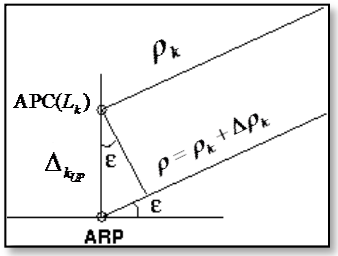
A set of additional exercises addressed to those students that already have a solid background in GPS data processing.

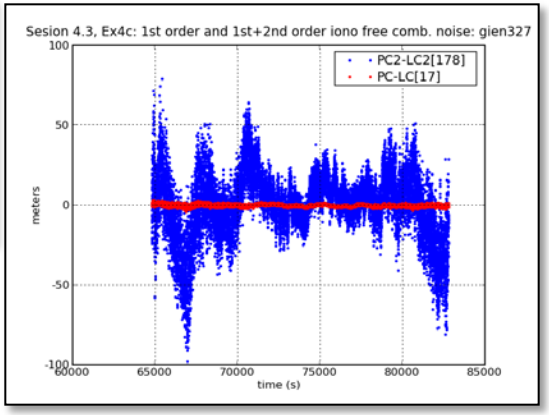
These exercises are beyond the scope of this 3h laboratory session, and are given for a possible further discussion…

As in the previous cases, the answers to the questions are also included as BACKUP slides.

A minimum knowledge of UNIX (e.g., awk) is desirable for these homework exercises.

$$\sum_k \alpha_k L_k + \underbrace{\sum_k \alpha_k \Delta_{k_{UP}} \sin\varepsilon}_{\text{APC correction term}} = bias$$





$$I2_{L1} = -\frac{7257c}{2f_1^3}\int_{rec}^{sat} N_e B\cos\theta ds \simeq -\frac{7427cB_0\cos\theta}{2f_1^3} STEC$$

```
gawk 'BEGIN{g=(77/60)^2}{print $6, $4, (g*($13-$14)-($15-$16))/(g-1)}' meas.txt > PC.txt
```

OVERVIEW

- Introduction
- The gLAB tool suite
- Examples of GNSS processing using gLAB
- Laboratory session organization

LABORATORY Session

- **Starting up your laptop**
- **Basic:** Introductory lab exercises: Iono & Posit, SF, storm,TIDs
- **Medium:** Laboratory Work Projects: LWP1 to LWP4
- **Advanced:** Homework

Starting up your laptop

1. **Plug the stick into an USB port and *boot your laptop from the stick*.**

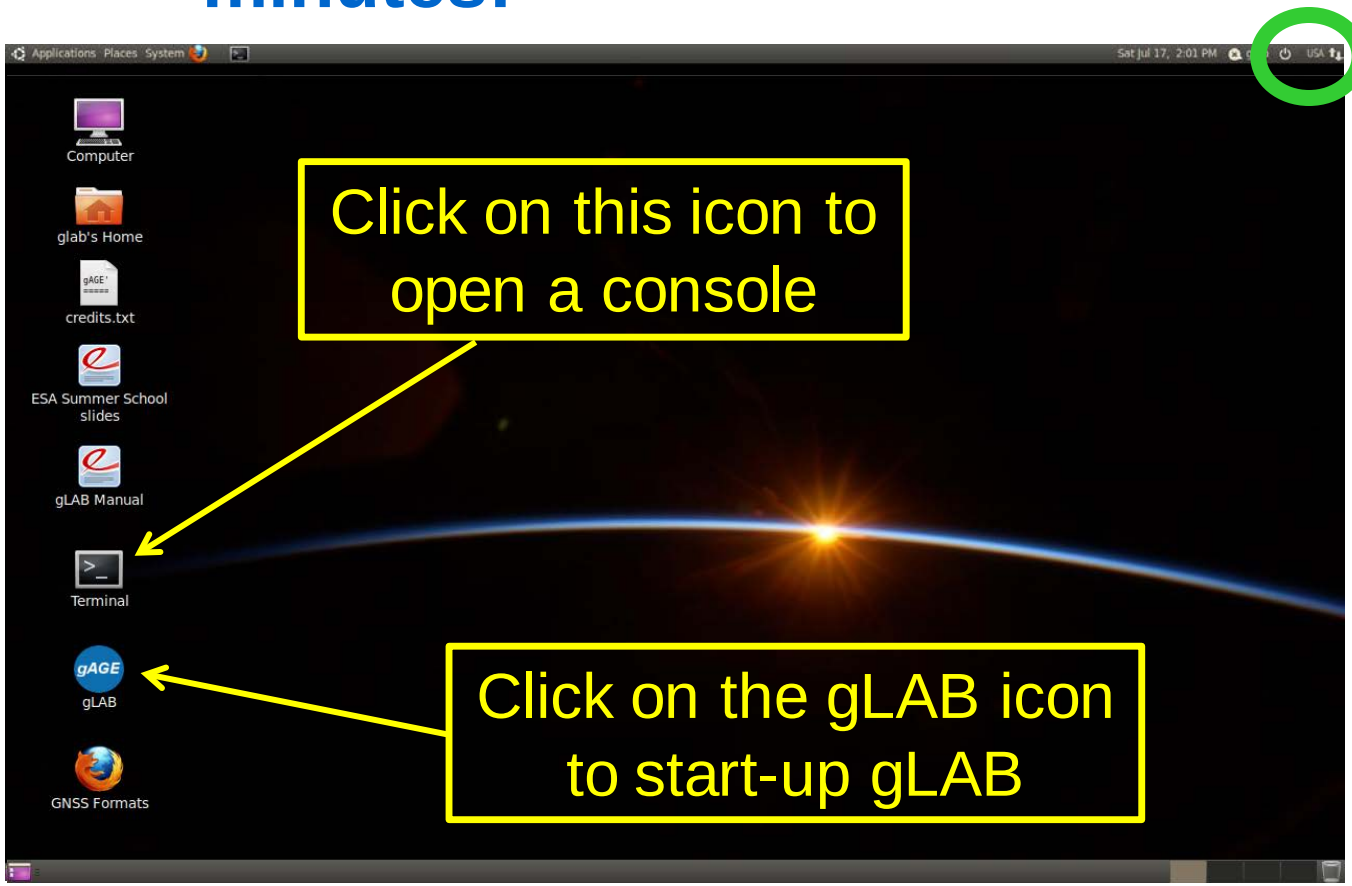
2. **Access the Boot Device Menu when starting up the laptop.**

   Note: The way to do it *depends on your computer*:

   Usually, you should press **[ESC]** or **[F4]**, **[F10]**, **[F12]**....

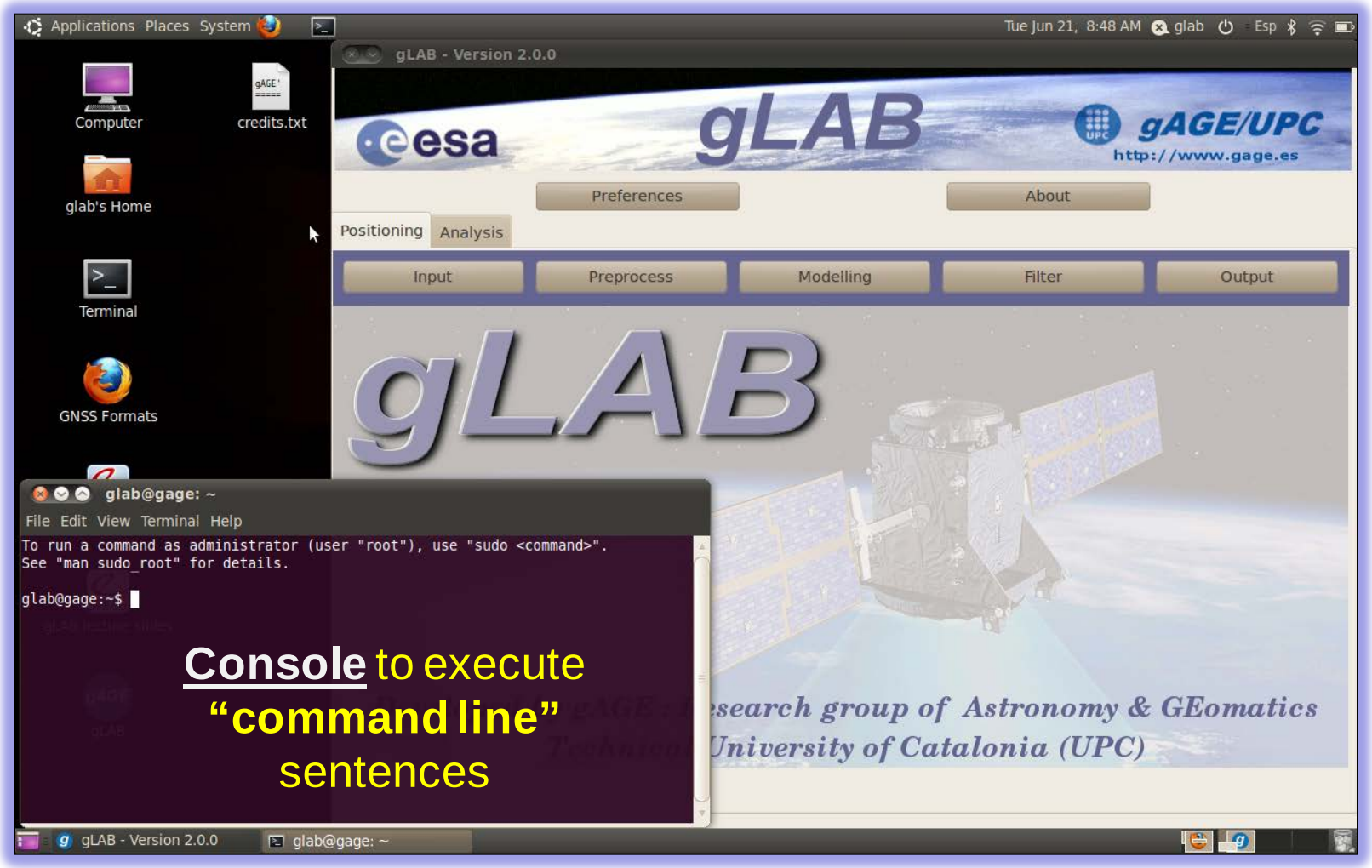
Starting up your laptop

3. The following screen will appear after about 2 minutes:



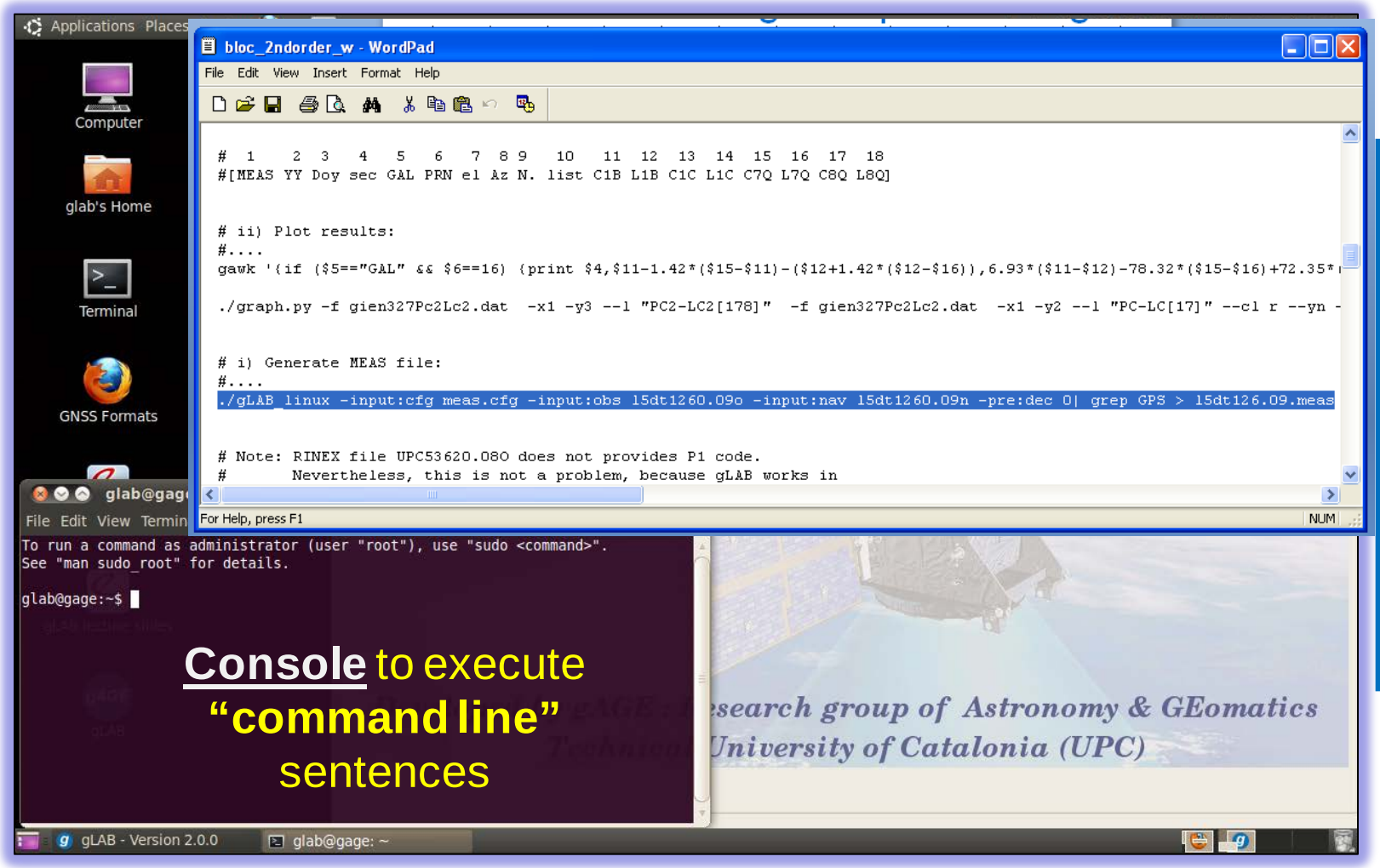
The US keyboard is set by default. You can change it by clicking on the upper right corner.

Starting up your laptop



Now, the system is ready to start working!

Starting up your laptop


Applications Places
Computer
glab's Home
Terminal
GNSS Formats
bloc_2ndorder_w - WordPad
File Edit View Insert Format Help
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18
#[MEAS YY Doy sec GAL PRN el Az N. list C1B L1B C1C L1C C7Q L7Q C8Q L8Q]
ii) Plot results:
#....
./graph.py -f gien327Pc2Lc2.dat -x1 -y3 --l "PC2-LC2[178]" -f gien327Pc2Lc2.dat -x1 -y2 --l "PC-LC[17]" --cl r --yn -
i) Generate MEAS file:
#....
./gLAB_linux -input:cfg meas.cfg -input:obs 15dt1260.09o -input:nav 15dt1260.09n -pre:dec 0| grep GPS > 15dt126.09.meas
Note: RINEX file UPC53620.08O does not provides P1 code.
Nevertheless, this is not a problem, because gLAB works in
For Help, press F1
NUM
File Edit View Termin
To run a command as administrator (user "root"), use "sudo <command>".
See "man sudo_root" for details.
glab@gage:~$
Console to execute
"command line"
sentences
gLAB - Version 2.0.0
glab@gage: ~

Copy and paste the sentences from notepad to console

OVERVIEW

- Introduction
- The gLAB tool suite
- Examples of GNSS processing using gLAB
- Laboratory session organization

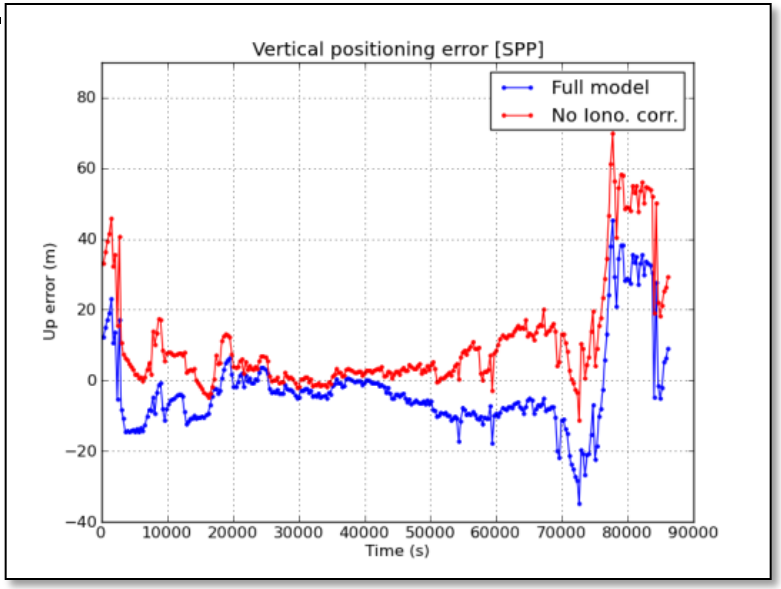
LABORATORY Session

- Starting up your laptop
- **Basic:** Introductory lab exercises: Iono & Posit, Solar Flair, Halloween storm,TIDs
- **Medium:** Laboratory Work Projects: LWP1 to LWP4
- **Advanced:** Homework

EX. 1 Halloween storm: October 2003

A severe ionospheric storm was experienced on October 29-31, 2003 producing and increase of the electron density which led to large ionospheric refraction values on the GPS signals. Such conditions were beyond the capability of the GPS Klobuchar model broadcast for single frequency users, producing large errors in the SPS (see details in [R-3]).

Dual frequency users, navigating with the ionospheric-free combination of GPS signals were not affected by such ionospheric errors, as the ionospheric refraction can be removed up to 99:9% using dual-frequency signals.



Ex. 1: Assessing Iono effects on single freq. pos.

Exercise: Repeat the previous study of Example 1 to analyze the single freq. solution, but for the Halloween storm.

The following steps are recommended:

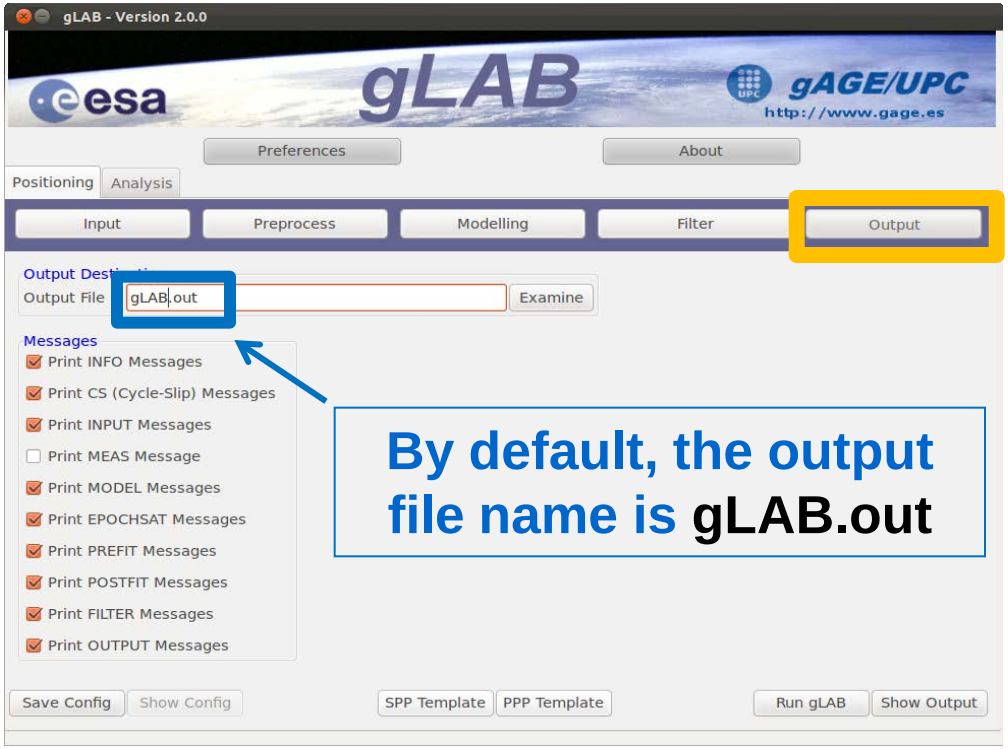
1. Using files **amc23020.03o,brdc3030.03n** compute with gLAB the following solutions:
   1. Solution with full SPS modeling. Name output file as: **gLAB.out**
   2. Solution with the ionospheric corrections disabled ➔ **gLAB1.out**
   3. Solution with the 2-freq. Ionosphere-free code (PC) ➔ **gLAB2.out**
2. Plot results

Note: The gLAB GUI or the command line sentences can also be used .

A "notepad" with the command line sentence is provided to facilitate the sentence writing: just "copy" and "paste" from notepad to the working terminal

Ex. 1: Full processing ➔ gLAB.out

1. Compute SPP using files: amc23020.03o,brdc3030.03n



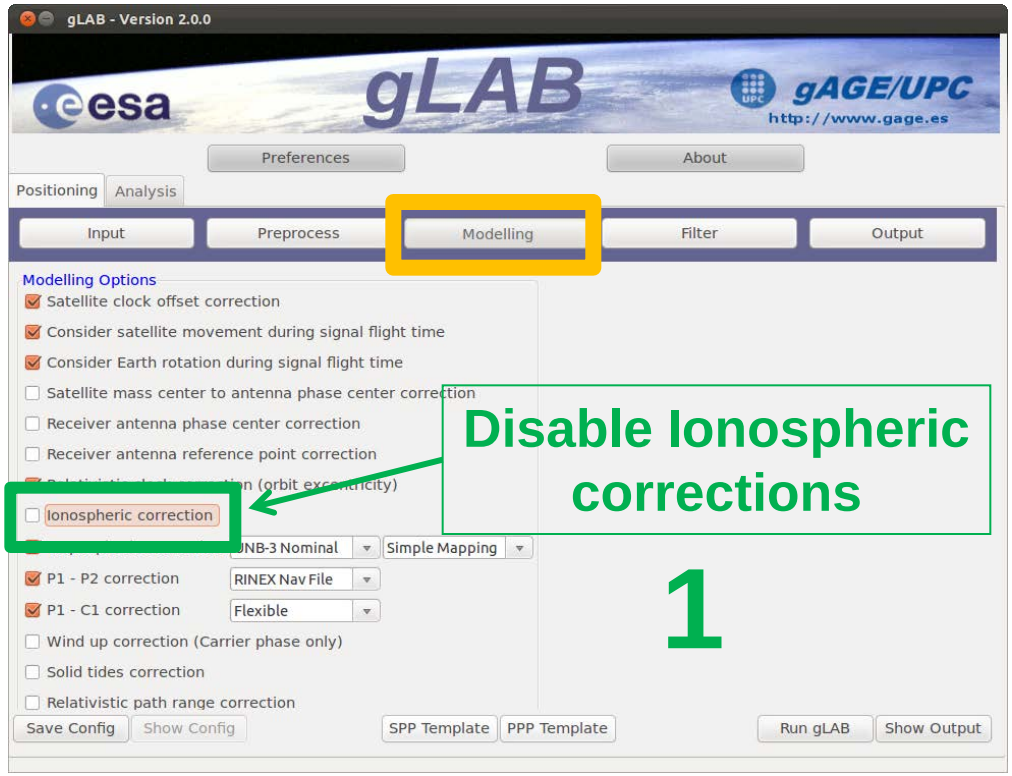
By default, the output file name is gLAB.out

Equivalent command line sentence:

```
gLAB_linux -input:cfg gLAB_p1_Full.cfg
           -input:obs amc3030.03o
           -input:nav brdc3030.03n
```

Ex. 1: Iono. Disabled ➔ gLAB1.out

2. Reprocess the same files, with the iono. corrections disabled

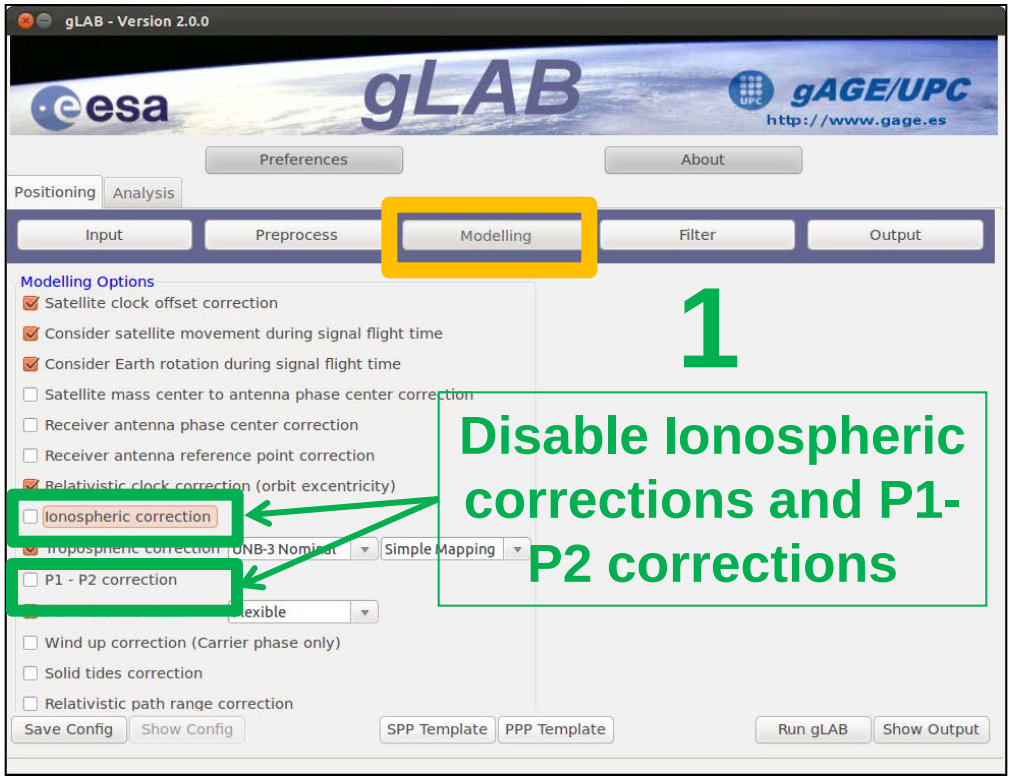


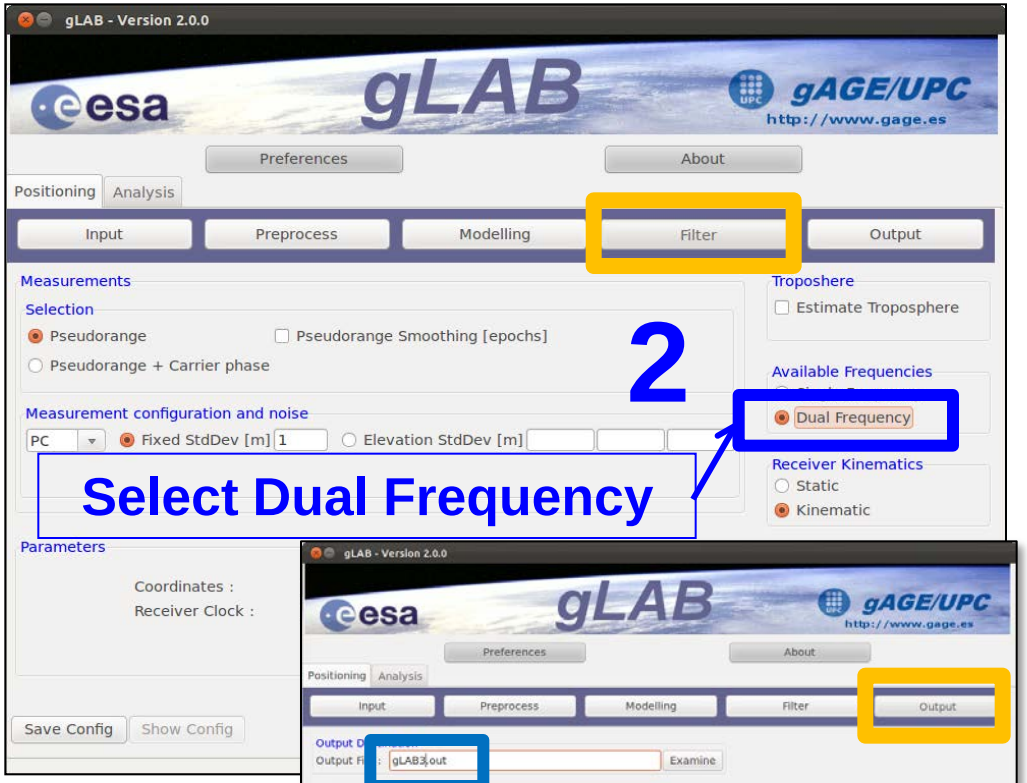
Equivalent command line sentence:

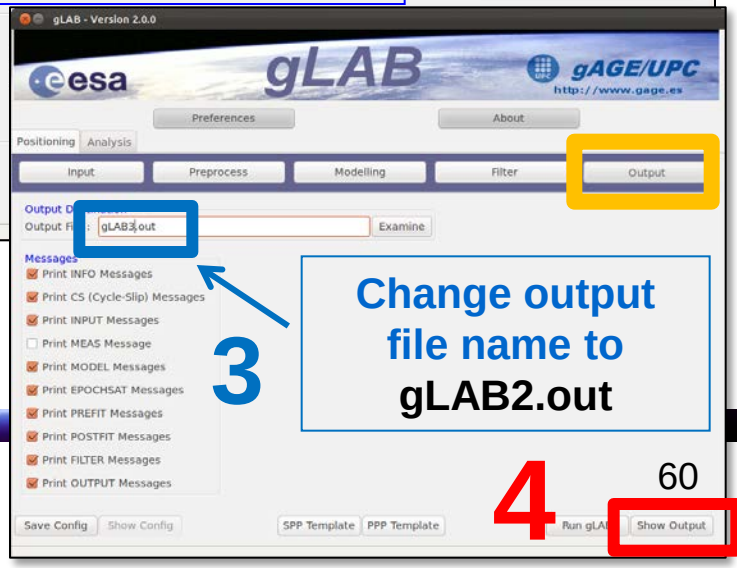
```
gLAB_linux -input:cfg gLAB_p1_NoIono.cfg
           -input:obs amc3030.03o
           -input:nav brdc3030.03n
```

Ex. 1: Processing with PC➔ gLAB2.out

3. **Reprocess** the same files, but with 2-frequency ionosphere-free (**PC**)







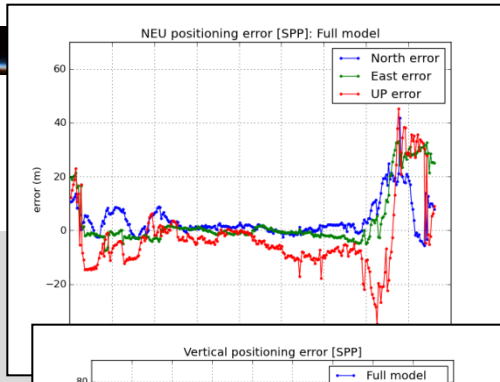
Equivalent command line sentence:

```
gLAB_linux -input:cfg gLAB_p1_IFree.cfg
           -input:obs amc3030.03o
           -input:nav brdc3030.03n
```

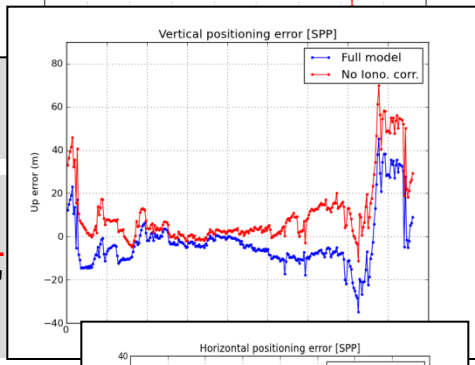
Ex. 1: Assessing Iono effects on single freq. pos.

Execute in a single line: (or use the gLAB GUI)

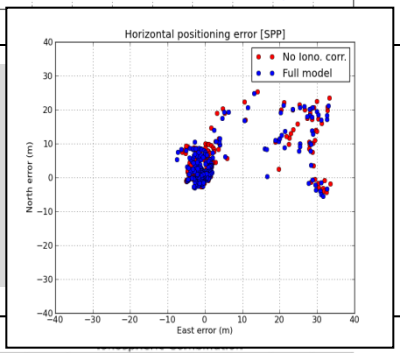
```
graph.py -f gLAB.out -x4 -y18 -s.- -c '($1=="OUTPUT")' -l "North error"
         -f gLAB.out -x4 -y19 -s.- -c '($1=="OUTPUT")' -l "East error"
         -f gLAB.out -x4 -y20 -s.- -c '($1=="OUTPUT")' -l "UP error"
                     --yn -40 --yx 70 --xl "time (s)" --yl "error (m)"
                     -t "NEU positioning error [SPP]: Full model"
```




```
graph.py -f gLAB.out  -x4 -y20 -s.- -c '($1=="OUTPUT")' --l "Full model"
         -f gLAB1.out -x4 -y20 -s.- -c '($1=="OUTPUT")' --l "No Iono." --cl
                      --yn -40 --yx 90 --xl "Time (s)" --yl "Up error (m)"
                      -t "Vertical positioning error [SPP]"
```

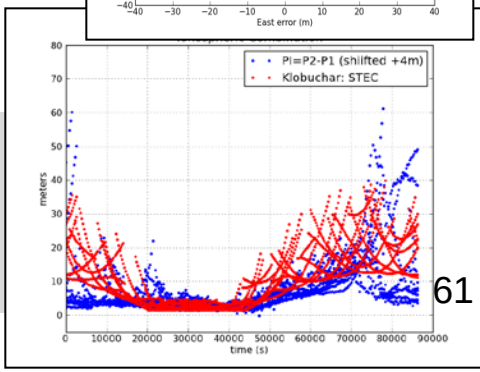



```
graph.py  -f gLAB1.out -x19 -y18 -so -c '($1=="OUTPUT")' --l "No Iono." --cl r
          -f gLAB.out  -x19 -y18 -so -c '($1=="OUTPUT")' --l "Full mod" --cl b
                       --xl "East error (m)" --yl "North error (m)"
                       --xn -40 --xx 40 --yn -40 --yx 40
                       -t "Horizontal pos. error [SPP]"
```

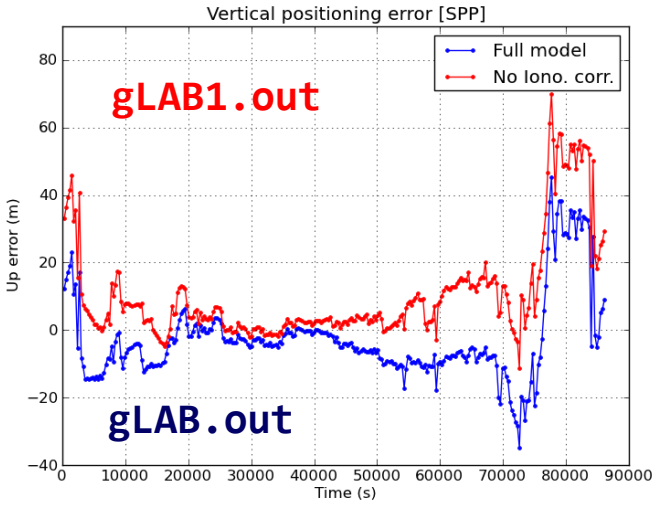


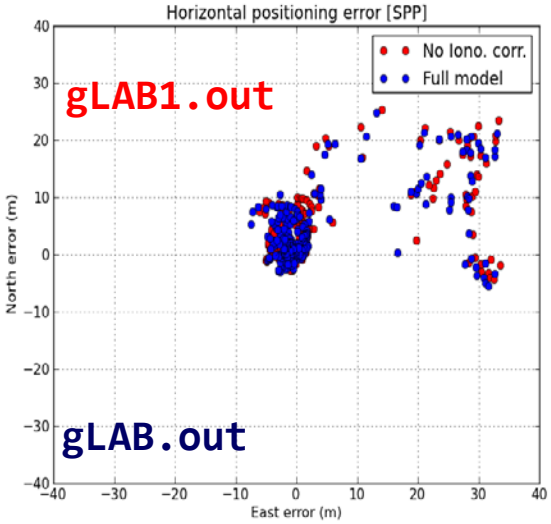
P2-P1 shifted +4 m

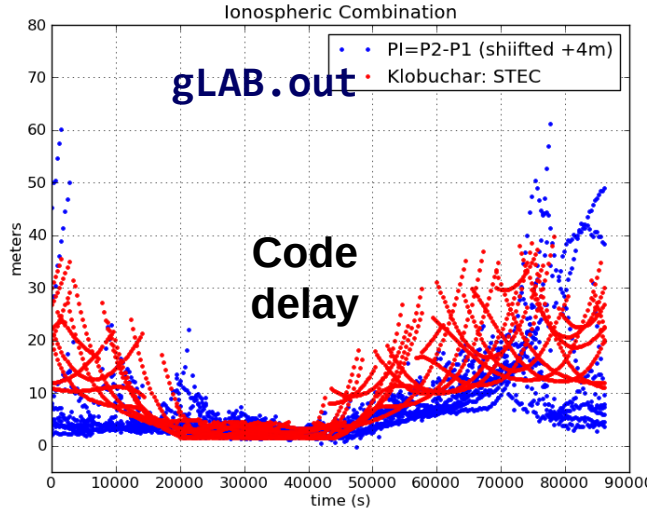
```
graph.py -f gLAB.out -x4 -y'($10-$9+4)'  -s. -c '($1=="INPUT")'
         -f gLAB.out -x4 -y25 -s. -c '($1=="MODEL")' --cl r
                     --xl "time (s)" --yl "meters"
                     --yn -5 --yx 80  -t "Ionospheric Combination"
```



Ex. 1: Assessing Iono effects on single freq. pos.





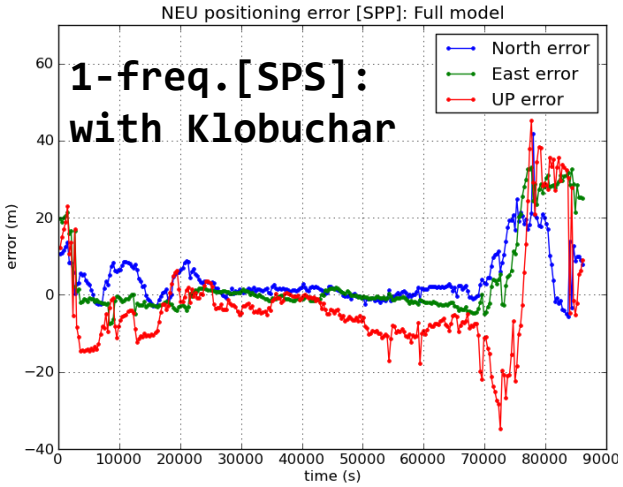


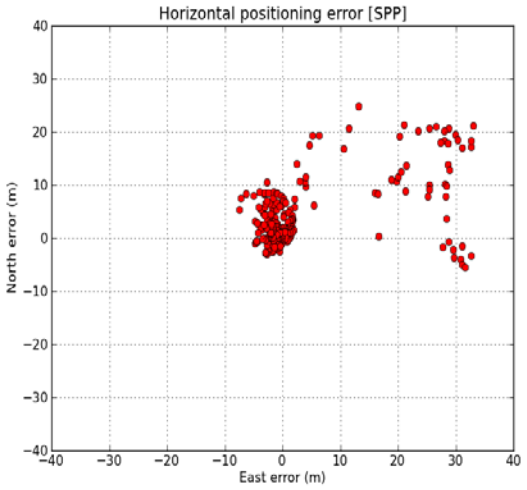
Ionospheric correction (broadcast Klobuchar)

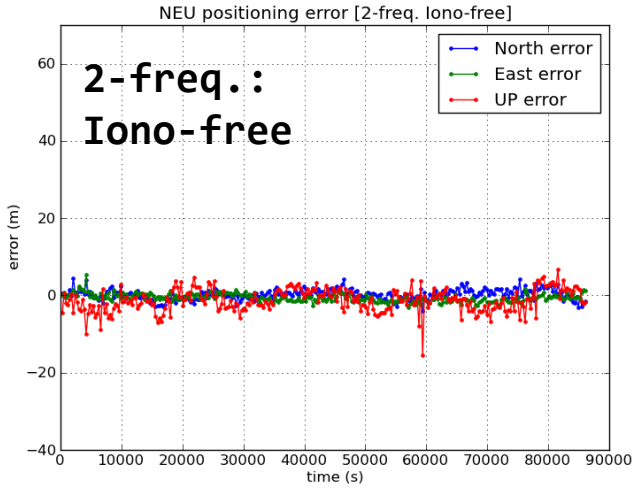
Ionospheric delays are larger at noon due to the higher insulation.

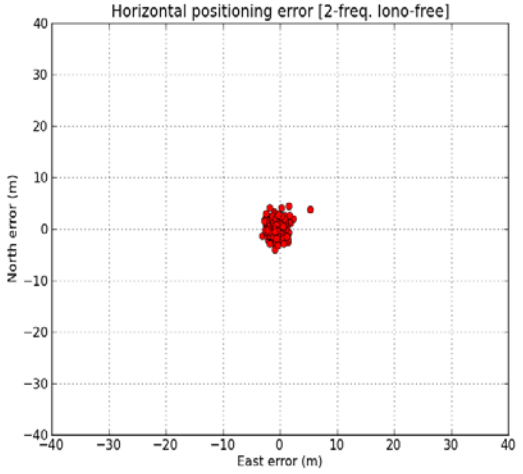
Klobuchar model is unable to mitigate the large ionospheric errors during the storm. Position domain errors reach up to 40 meters with Klobuchar corrections used.

Ex. 1: Assessing Iono effects on single freq. pos.





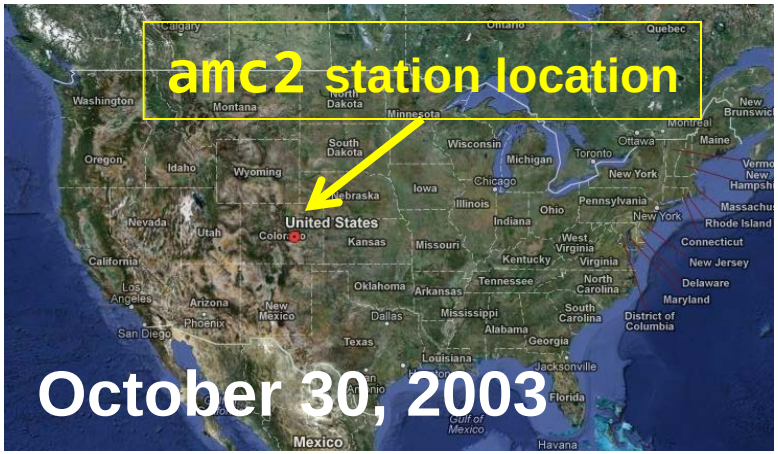




Ionospheric correction (broadcast Klobuchar)

- The ionosphere-free combination (PC) of P1 and P2 codes is immune to the ionospheric storm.
- Although PC is three-times noisier than P1 or P2, it provides positioning accurate at the level of a few meters during the storm.

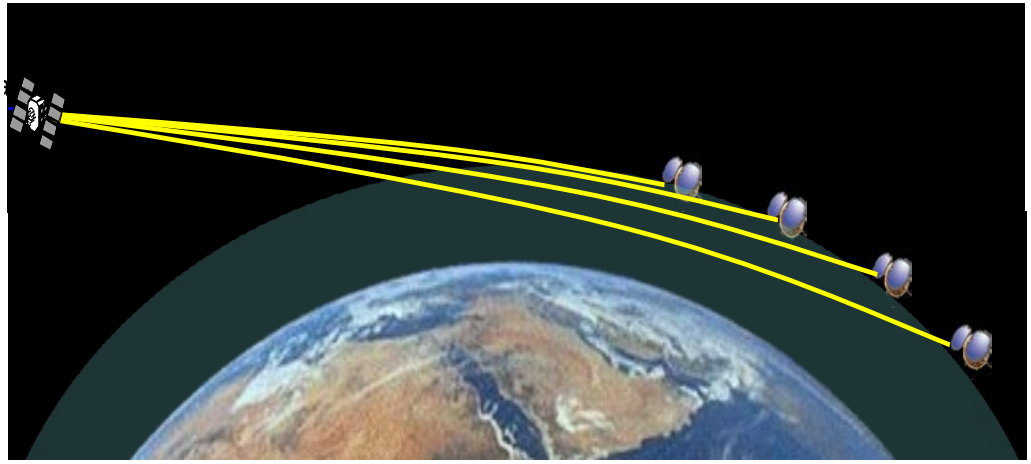
$$P_C = \frac{f_1^2 P_1 - f_2^2 P_2}{f_1^2 - f_2^2}$$



Ex. 2: STEC in a Radio Occultation (RO)

Radio Occultation (RO) commonly refers to a sounding technique in which a radio signal from a transmitting satellite (e.g., GPS) passes through a planetary atmosphere before arriving at a receiver on board a Low Earth Orbiter (LEO) satellite.

Along the ray path, the phase of the radio signal is perturbed in a manner related to the refractivity.
RO measurements can reveal the refractivity, from which one can then derive atmospheric quantities such as Pressure, Temperature and the partial pressure of water vapor; and electron density, among others.

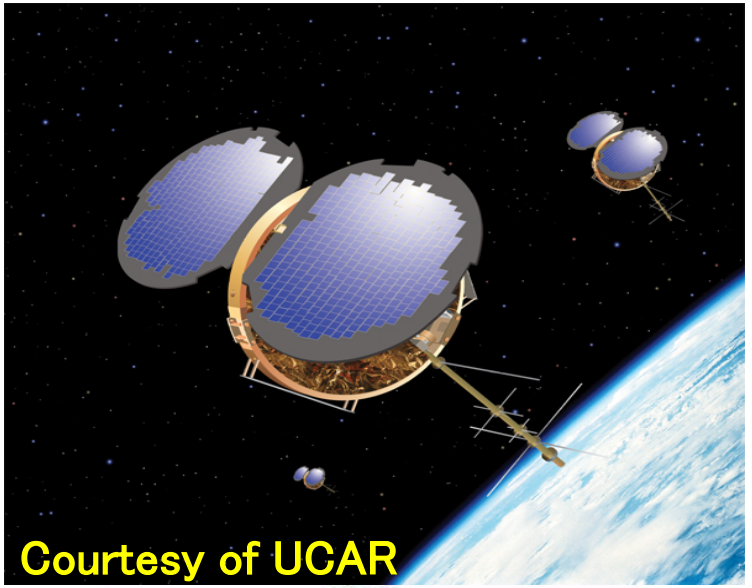


This is a simple exercise where the STEC variation along a radio occultation will be depicted using GPS L1, L2 measurements from a receiver on board a LEO of COSMIC constellation.

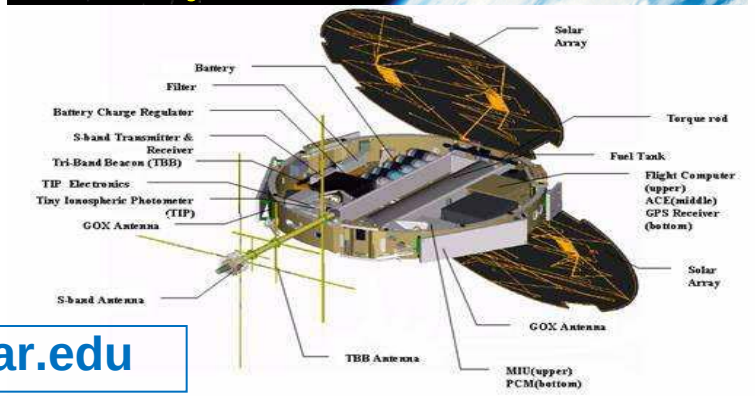
In the LWP1, Electron Density Profiles will be retrieved from this data using an algorithm equivalent to the Abel Transform.

FORMOSAT-3/COSMIC mission

Constellation Observing System for Meteorology Ionosphere and Climate:
6 microsatellites; orbit altitude ~ 800km



- **Three instruments:**
  - GPS receiver. 4 antennas: 2 for POD, 2 for RO.
  - TIP, Tri-band beacon
- **Weather + Space Weather data.**
- **Global observations of:**
  - Pressure, Temperature, Humidity
  - Refractivity
  - Ionospheric Electron Density
  - Ionospheric Scintillation
- **Demonstrate quasi-operational GPS limb** sounding with global coverage in near-real time
- **Climate Monitoring**



Information available at **www.cosmic.ucar.edu**

Ex. 2: STEC in a Radio Occultation (RO)

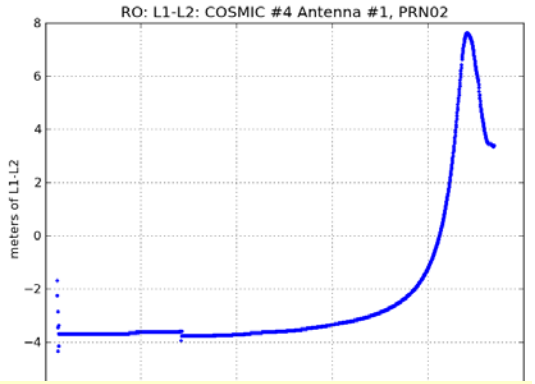
Exercise: The file "RO.obs" contains the following fields [*]:

```
                                  |<------ LEO ------>|<------- GPS ------->|
YY DoY HH.HH CODE PRN  elev  r_LEO AR_LEO DEC_LEO  r_GPS AR_GPS DEC_GPS   L1  L2   L1-L2 arc
                       (deg)  (km) (Deg)   (Deg)    (km)  (Deg)  (Deg)   (cycles)   (m)
 1  2    3    4    5    6     7     8       9       10     11     12     13  14    15   16
```

Plot the L1-L2 measurement in function of time to depict the variation of STEC along the occultation:

Select for instance : PRN=02 and "CODE=l241", that corresponds to LEO=4 and Antenna 1

```
- Selecting: CODE=l241 and PRN=02
  grep l241 RO.obs|gawk '{if ($5==02) print $3,$15}'> ro.dat

- Ploting L1-L2
  graph.py -f  ro.dat --xl "time (H)"
   --yl "meters of L1-L2"  -t"RO: L1-L2: COSMIC #4 Antenna #1"
```

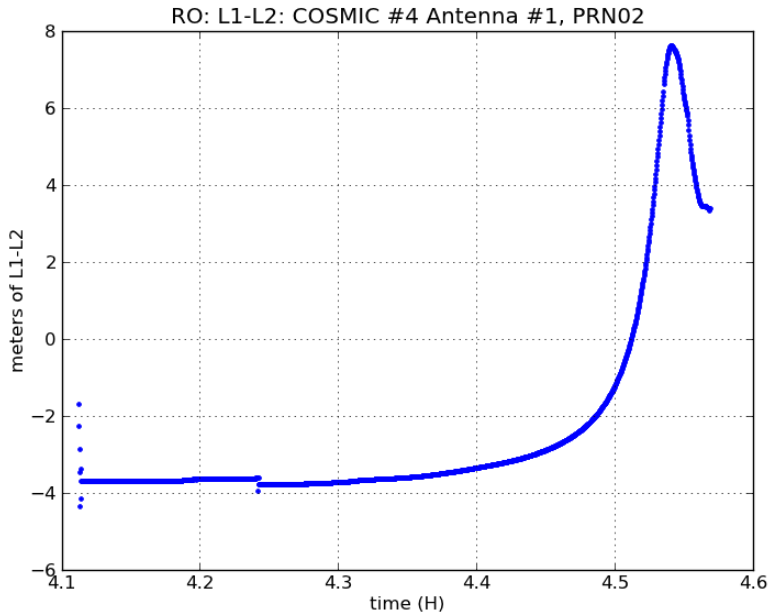


[*] This file has been generated from files (http://cosmic-io.cosmic.ucar.edu/cdaac):
podObs_2006.253.004.01.01_rnx, leoOrb_2006.253.004.01_2009.2650_sp3, igs13920.sp3

66

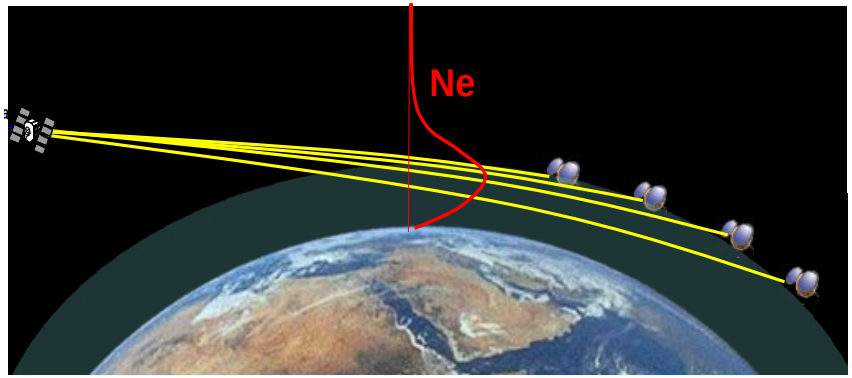
Ex. 2: STEC in a Radio Occultation (RO)

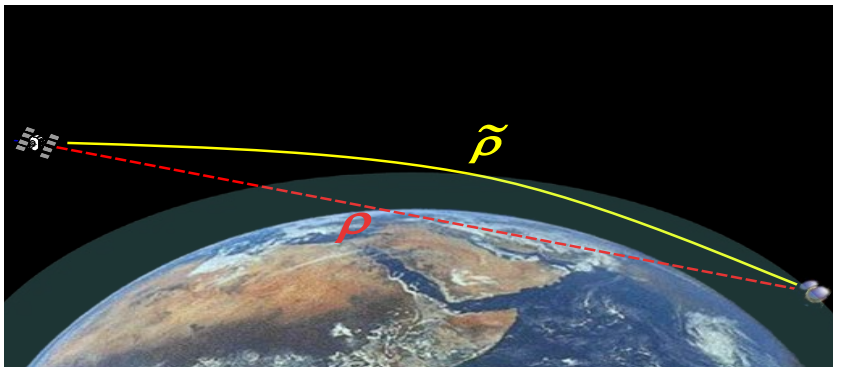
The previous plot shows only the variation of the Integrated Electron Content along the ray path (STEC).



More information can be retrieved from occultation measurements. For instance:

- Electron Density Profile of the Ionosphere (LWP1).
- Phase excess rate, which is related to the bending of ray (LWP2).





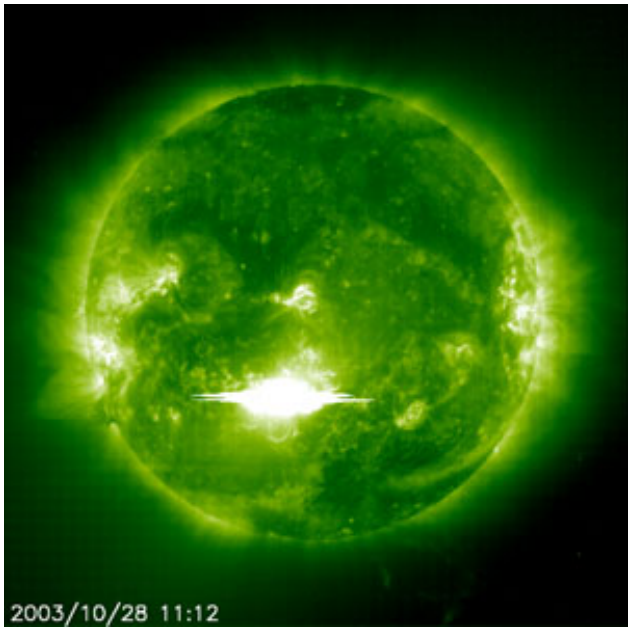
Given that session time is limited to 2h, participants who feel comfortable using gLAB, can skip part of the next basic exercises (Ex3..., Ex6) and jump to the Laboratory Work Projects (LWP).

There, if you prefer, you can jump to slide #87 and choose one from the four LWPs

Ex. 3: Solar Flare October 28, 2003

On October 28, 2003, an intense solar eruption (a Solar Flare) was detected around 11h UT in an active region which had grown one of the largest sunspots ever seen by the SOlar Helioscopic Observatory (SOHO). It appeared as a bright spike in the SOHO ultraviolet images.

This sudden enhancement of the solar radiation in the X-ray and extreme ultra-violet band produced a sudden increase in the ionospheric electron density on the daylight hemisphere, (see [R-3]).



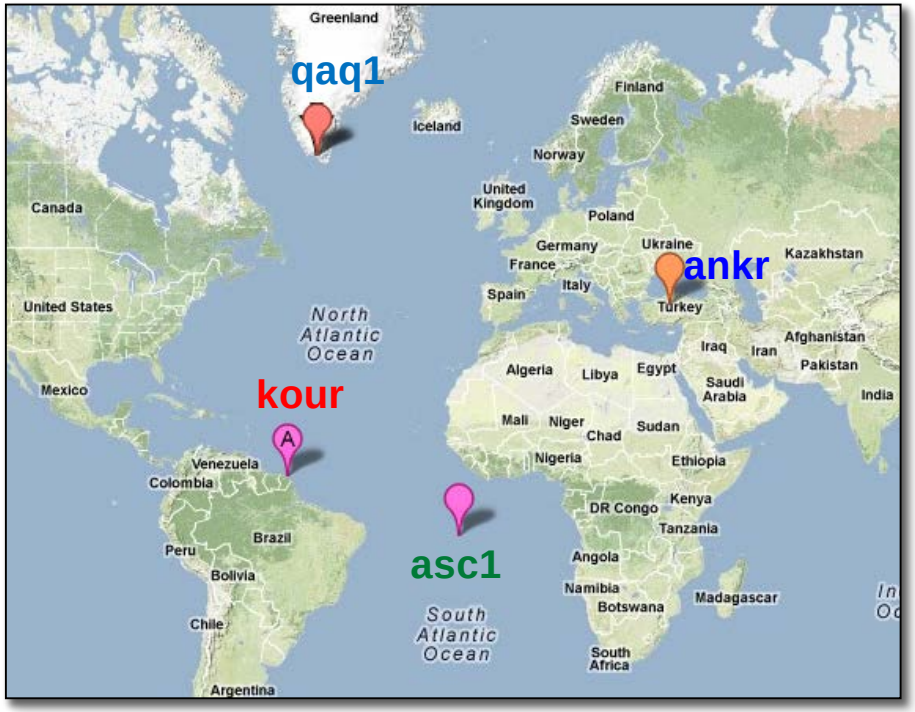
Ex. 3: Solar Flare October 28, 2003

Exercise: Analyze the effect of the Solar Flare on the Slant Total Electron Content (STEC) measurements of four permanent IGS receivers ankr, asc1, kour and qaq1, covering a wide range of longitude and latitude.

Data sets:

ankr3010.03o, asc13010.03o,

kour3010.03o, qaq13010.03o



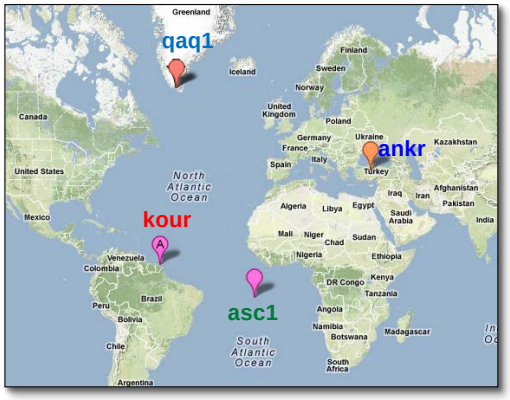
Ex. 3: Solar Flare October 28, 2003

Execute:

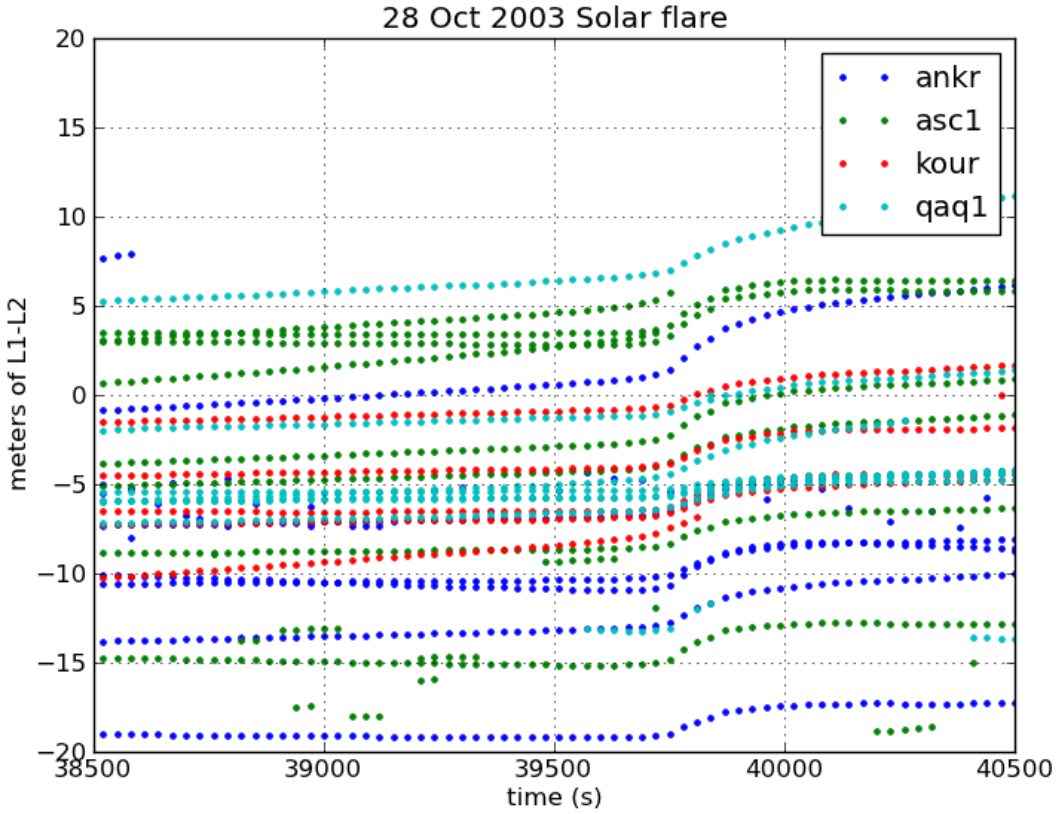
```
[Id YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2P L2P]
 1  2  3   4   5    6  7   8  9  10  11   xx  13  14  15 16 ]
```

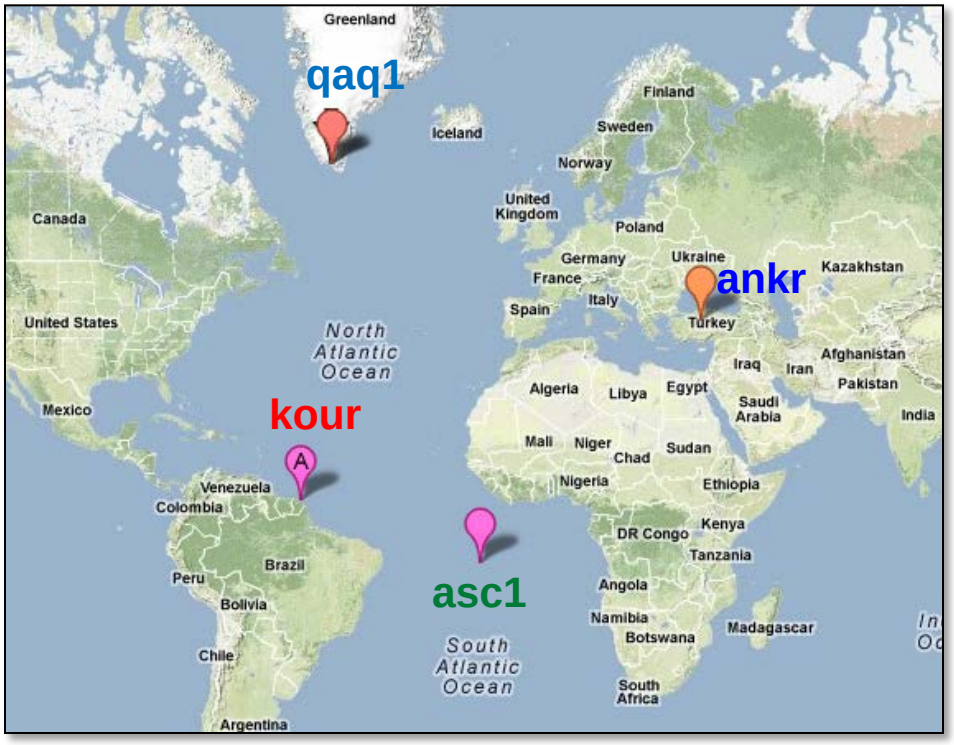
```
gLAB_linux -input:cfg meas.cfg -input:obs ankr3010.03o > ankr3010.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs asc13010.03o > asc13010.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs kour3010.03o > kour3010.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs qaq13010.03o > qaq13010.03.meas
```

```
graph.py -f ankr3010.03.meas -x4 -y'($14-$16)' --l "ankr"
         -f asc13010.03.meas -x4 -y'($14-$16)' --l "asc1"
         -f kour3010.03.meas -x4 -y'($14-$16)' --l "kour"
         -f qaq13010.03.meas -x4 -y'($14-$16)' --l "qaq1"
         --xl "time (s)" --yl "meters of L1-L2"
         --xn 38500 --xx 40500 --yn -20 --yx 20
         -t "28 Oct 2003 Solar flare"
```



Ex. 3: Solar Flare October 28, 2003

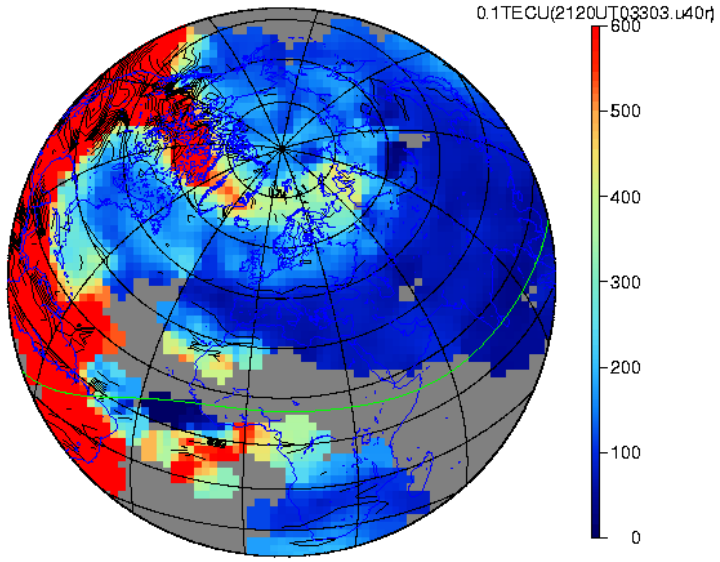




Ex. 4: Halloween storm: P2-P1 analysis

Associated with the Solar Flare analysed in the previous exercise, a Coronal Mass Ejection occurred, which sent a large particle cloud impacting the Earth's magnetosphere about 19 hours later, on October 29.

Subsequent impacts were still occurring several hours later. This material interacted with the Earth's magnetosphere and a Storm Enhancement Density (SED) appeared in North America and affected later the northern latitudes in Europe. Extra large gradients of TEC associated with this phenomenon were also produced, degrading the GPS positioning performance.



The TEC evolution in October 30, 2003 (i.e., Day 303 of year 2003) can be seen in the movie TEC 2003oct30 anim.gif.

Ex. 4: Halloween storm: P2-P1 analysis

The measurement files garl3010.03o, garl3020.03o, garl3030.03o, garl3040.03o, garl3050.03o, garl3060.03o were collected by the permanent receiver garl in Empire, Nevada, USA (ϕ= 40.42 deg, λ =-119:36 deg) from October 28 to November 2, 2003.

Using these files, plot the STEC for all satellites in view and discuss the range of such variations. Analyse, in particular, the satellite PRN 04 and calculate the maximum rate of STEC variation in mm=s of L1 delay. Add the elevation of satellite PRN 04 in the plot.

The associated broadcast navigation les are brdc3010.03n, brdc3020.03n, brdc3030.03n, brdc3040.03n, brdc3050.03n, brdc3060.03n.

Ex. 4: Halloween storm: P2-P1 analysis

Exercise: Depict the ionospheric delays for the different satellites in view from station amc2

- This is a simple exercise aimed to illustrate how to use gLAB to easily analyze GNSS measurements and their combinations.
- gLAB will used to read the RINEX measurements file and to generate a “text” with the measurements provided in a columnar format (more suitable to make plots).

- Using such “text” file, the STEC pattern for the different satellites in view during the storm is depicted from the geometry-free combination of codes *P2-P1.*

Note:

$$P_2 - P_1 = I + K_{21}$$

Ex. 4: Halloween storm: P2-P1 analysis

The next commands read a RINEX file and generate a text file (in columnar format) that allows to easily plot the measurements and their combinations:

1. **Using** the configuration file **meas.cfg**, READ the RINEX and generate the MEAS message with data format:

```
[Id YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2P L2P]
 1  2  3   4   5    6  7   8  9  10   11   xx  13  14  15 16 ]
```

Execute:

```
gLAB_linux -input:cfg meas.cfg -input:obs amc23030.03o -input:nav brdc3030.03n > amc23030.03.meas
```

2. **From** `meas.txt` **file,**

Compute the ionospheric combination of codes: ***PI=P2-P1.***

Generate the file **PI.txt** with the following content: **[PRN, hour, PI, elevation]**

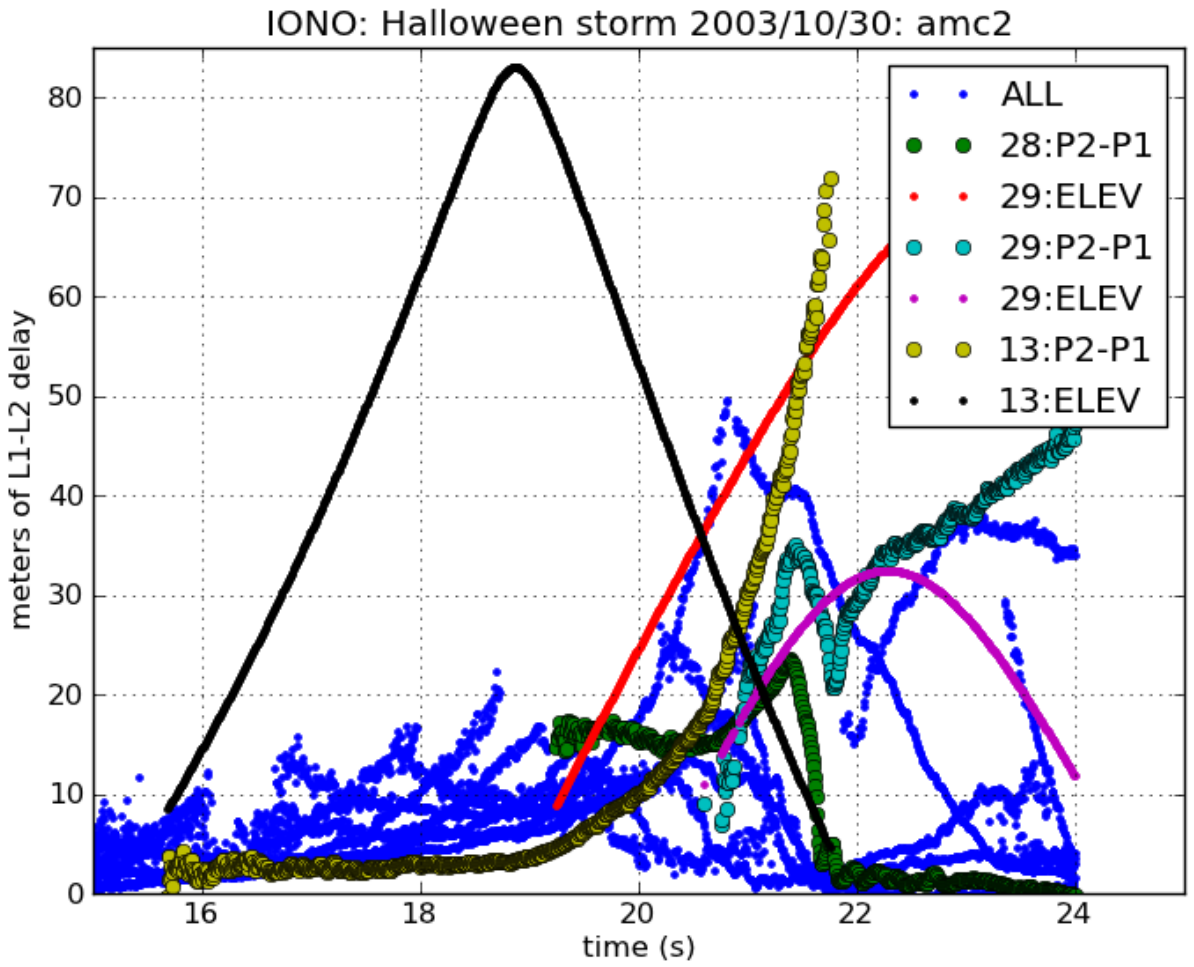
```
gawk '{print $6, $4/3600, $15-$13, $7}' amc23030.03.meas > PI.txt
```

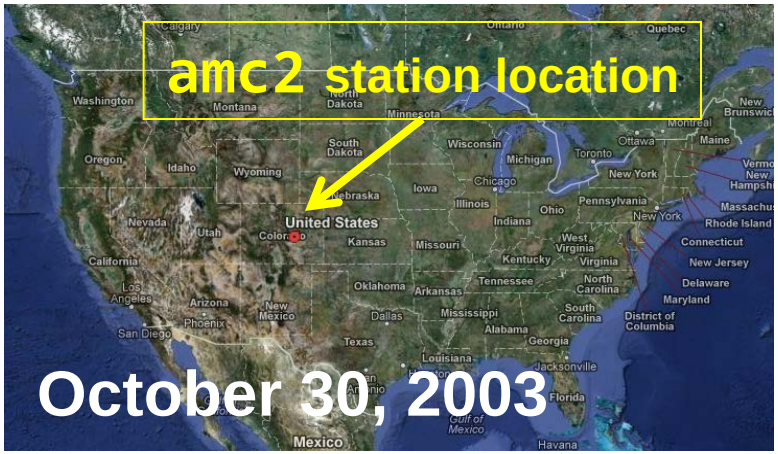
3. **From** `PI.txt` **file**,

Plot the ***PI=P2-P1*** for time interval [15 to 24].hours. Show in the same graph: 1) ALL satellites, 2) PRN 13, 28 and 29, and 3) The elevation of each satellite.(13, 28 and 29)

```
graph.py -f PI.txt -x2 -y3 --l "ALL"
   -f PI.txt -c'($1==28)' -x2 -y3 -so --l "28:P2-P1" -f PI.txt -c'($1==28)' -x2 -y4 --l "29:ELEV"
   -f PI.txt -c'($1==29)' -x2 -y3 -so --l "29:P2-P1" -f PI.txt -c'($1==29)' -x2 -y4 --l "13:ELEV"
   -f PI.txt -c'($1==13)' -x2 -y3 -so --l "13:P2-P1" -f PI.txt -c'($1==13)' -x2 -y4 --l "13:ELEV"
   --xn 15 --xx 25 --yn 0 --yx 85 --xl "time (s)" --yl "meters of L1-L2 delay"
```

Ex. 4: Halloween storm: P2-P1 analysis





Ex. 5: Halloween storm evolution

Exercise: Analyze the ionospheric delays for 6 consecutive days including the Halloween storm

- This is a simple exercise aimed to illustrate the ionospheric delays variation during the Halloween storm. A period of 6 consecutive days (from October 28 to November 2, 2003) are analyzed using measurements collected in the **"garl"** station in North America.

- The STEC variations are depicted from the geometry-free combination of codes *P2-P1.*

Note: $P_2 - P_1 = I + K_{21}$

Ex. 5: Halloween storm evolution

```
[Id YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2P L2P]
 1  2  3   4   5   6  7   8  9  10  11   xx  13  14  15 16 ]
```

1.- Read RINEX file:

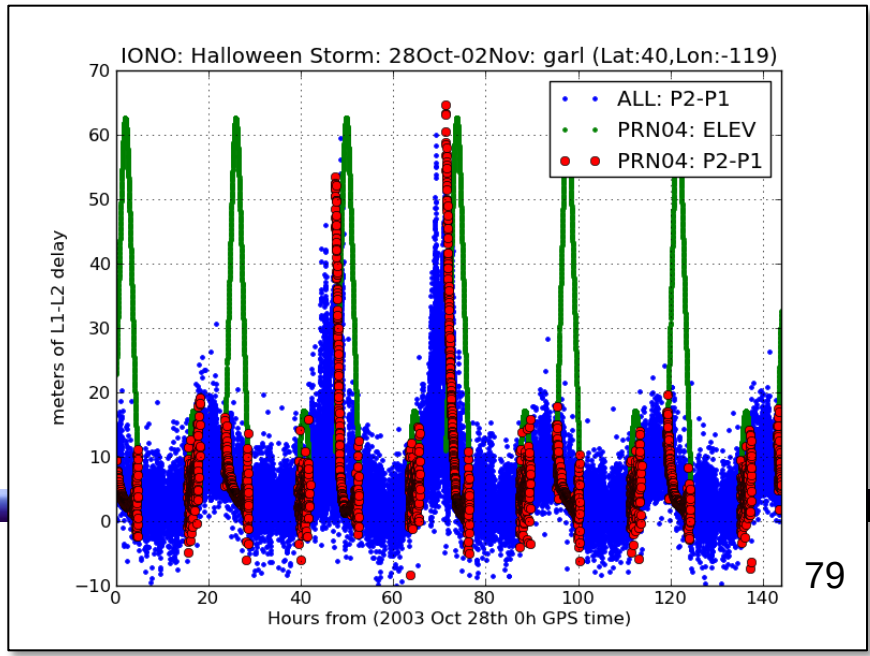
```
gLAB_linux -input:cfg meas.cfg -input:obs garl3010.03o -input:nav brdc3010.03n > garl3010.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs garl3020.03o -input:nav brdc3020.03n > garl3020.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs garl3030.03o -input:nav brdc3030.03n > garl3030.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs garl3040.03o -input:nav brdc3040.03n > garl3040.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs garl3050.03o -input:nav brdc3050.03n > garl3050.03.meas
gLAB_linux -input:cfg meas.cfg -input:obs garl3060.03o -input:nav brdc3060.03n > garl3060.03.meas
```

2.- Merge files and refer all the data to 0h of October 28th: Doy0301:

```
cat garl30?0.03.meas |gawk '{d=($3-301)*86400;$4=$4+d; print $6, $4/3600, $15-$13, $7}' > PI.txt
```

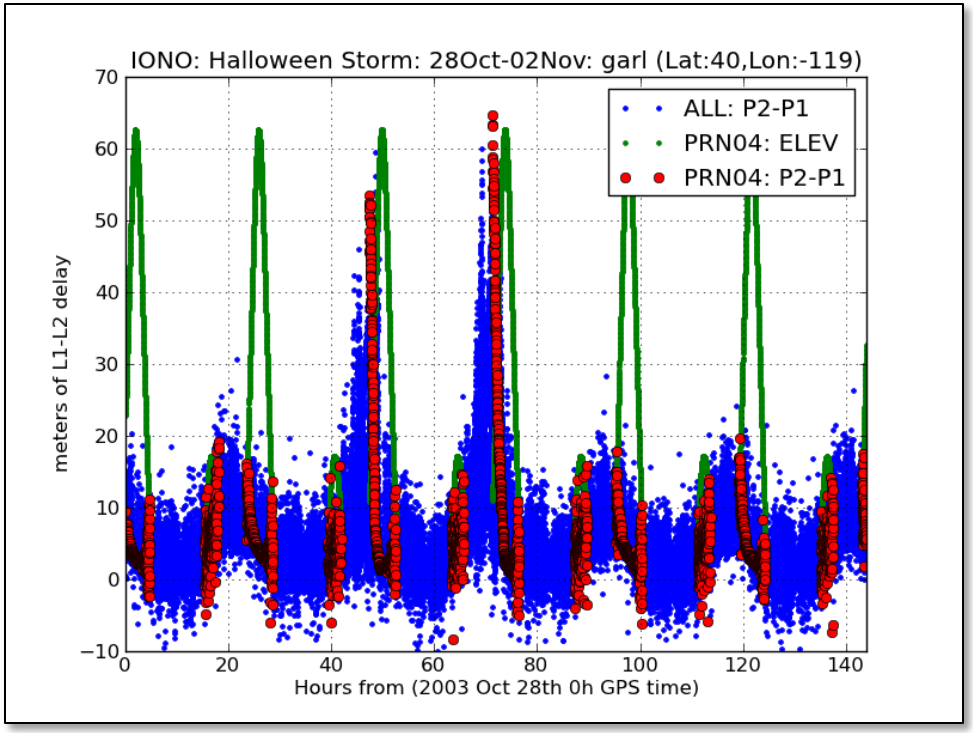
3.- Plot results:

```
graph.py -f PI.txt -x2 -y3 --l "ALL P2-P1"
  -f PI.txt -c'($1==04)' -x2 -y4 --l "PRN04: ELEV"
  -f PI.txt -c'($1==04)' -x2 -y3 -so --l "PRN04: P2-P1"
  --xn 0 --xx 144
```



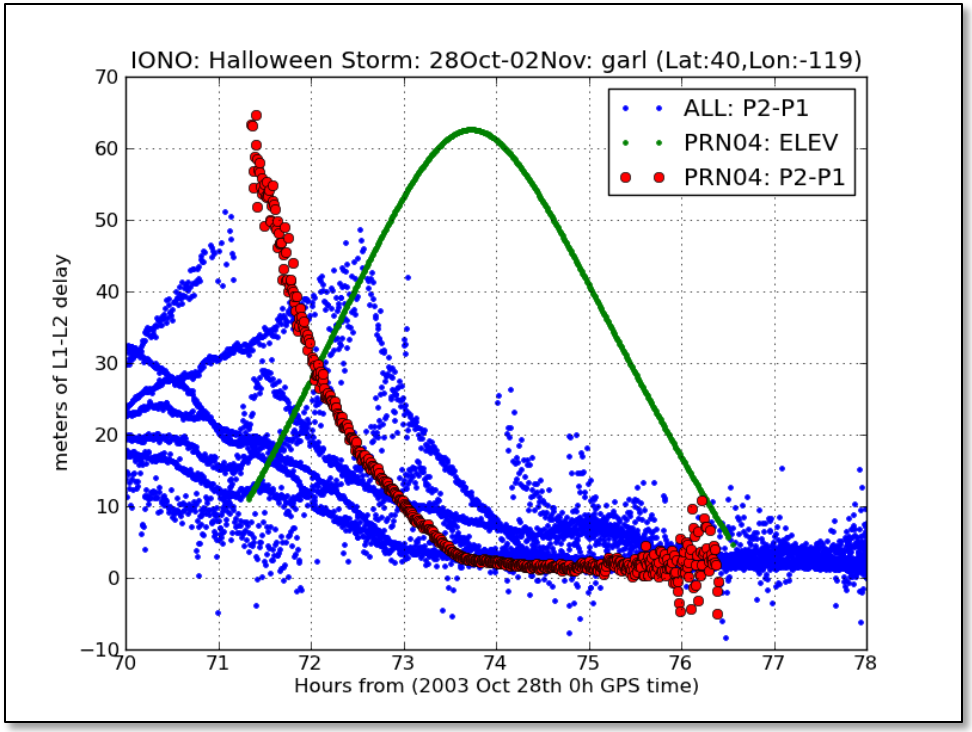
Ex. 5: Halloween storm evolution

```
graph.py -f PI.txt -x2 -y3 --l "ALL P2-P1"
  -f PI.txt -c'($1==04)' -x2 -y4 --l "04: EL"
  -f PI.txt -c'($1==04)' -x2 -y3 -so --l "04"
  --xn 0 --xx 144
```


IONO: Halloween Storm: 28Oct-02Nov: garl (Lat:40,Lon:-119)
ALL: P2-P1
PRN04: ELEV
PRN04: P2-P1
meters of L1-L2 delay
Hours from (2003 Oct 28th 0h GPS time)

Zoom at time interval: 70 to 78 h

```
graph.py -f PI.txt -x2 -y3 --l "ALL P2-P1"
  -f PI.txt -c'($1==04)' -x2 -y4 --l "04: EL"
  -f PI.txt -c'($1==04)' -x2 -y3 -so --l "04"
  --xn 70 --xx 78
```


IONO: Halloween Storm: 28Oct-02Nov: garl (Lat:40,Lon:-119)
ALL: P2-P1
PRN04: ELEV
PRN04: P2-P1
meters of L1-L2 delay
Hours from (2003 Oct 28th 0h GPS time)

Ex. 6: Travelling Ionospheric Disturb.

Travelling Ionospheric Disturbances (TIDs) are understood as plasma density fluctuations that propagate through the ionosphere at an open range of velocities and frequencies. The trend of such fluctuations can be seen from the geometry free combination of GPS carrier measurements $L_I = L_1 - L_2$.

Some authors distinguish between Large-Scale TIDs (LSTIDs) with a period greater than 1 hour and moving faster than *0,3 km/s*, and Medium- Scale TIDs (MSTIDs) with shorter periods (from 10 minutes to 1 hour) and moving slower (*0.05-0.3 km/s*). The LSTIDs seem to be related to geomagnetic disturbances (i.e., aurora, ionospheric storms, etc.). The origin of MSTIDs seems to be more related to meteorological phenomena such as neutral winds, eclipses, or solar terminator that produces Atmospheric Gravity Waves (AGW) being manifested as TIDs at ionospheric heights, due to the collision between neutral and ionised molecules.

Ex. 6: Travelling Ionospheric Disturb.

In [R4, 2006] a simple method to detect MSTIDs is proposed. It consists of detrending the geometry free combination of GPS carrier measurements from the diurnal variation and elevation angle dependences, applying the following equation:

$$\delta L_I(t) = L_I(t) - \left(L_I(t+\tau) - L_I(t-\tau) \right) / 2$$

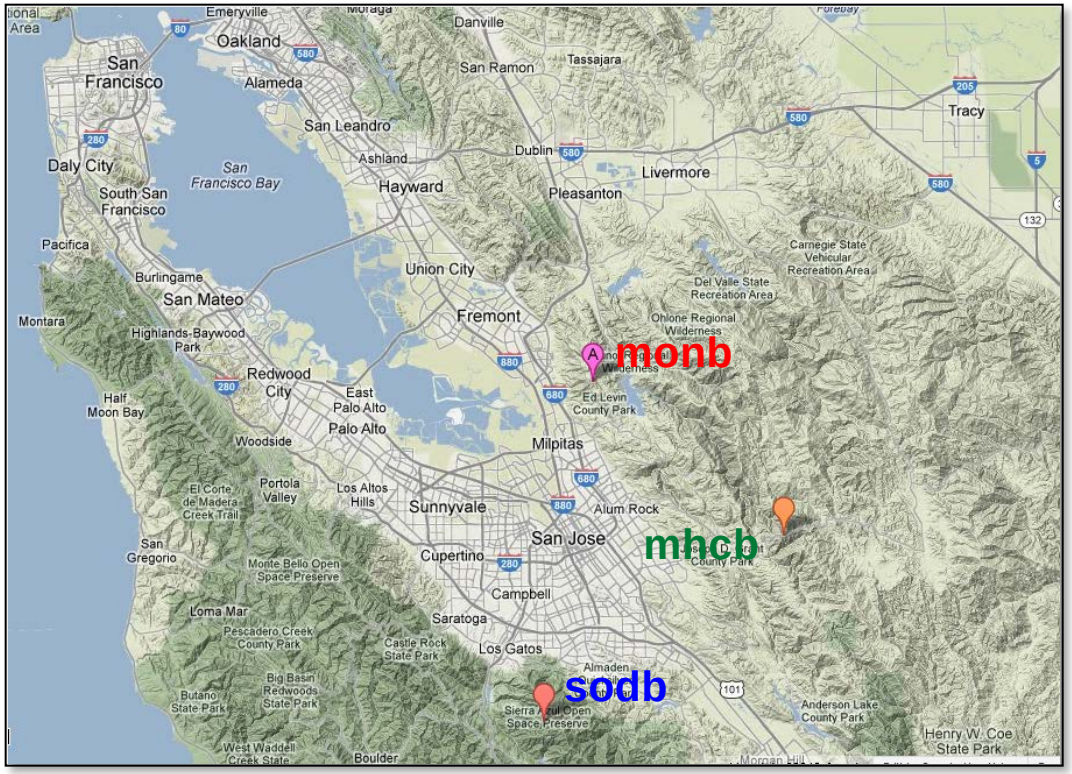
where a value of 300sec is suitable to keep enough variation of LI (i.e., STEC).

Using the previous equation, the detrending is done simply by subtracting from each value an average value of the previous and posterior measurements (i.e., the curvature of the LI temporal dependency). It must be pointed out that that this detrending procedure can be used in real time with a single receiver, so it is suitable for identifying these ionospheric perturbations in navigation applications.

Ex. 6: Travelling Ionospheric Disturb.

An example of MSTID propagation can be depicted as follows using the measurements of three stations SODB, MHCB and MONB, which are separated by a few tens of kilometres.

The target is to reproduce the figure 10 of the above mentioned paper [R4, 2006].



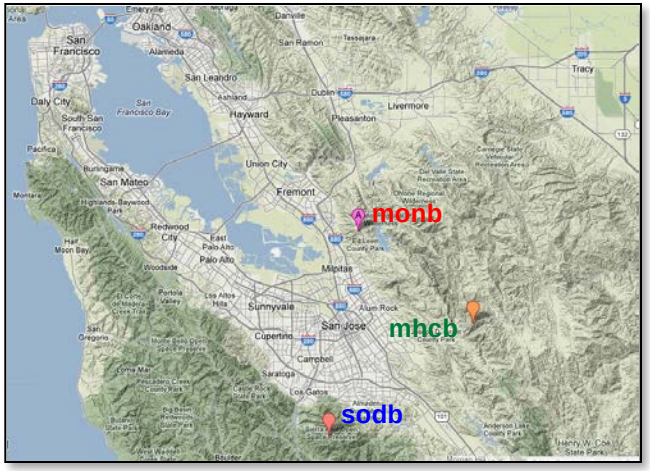
[R4, 2006] Hernández-Pajares, M; Juan, M.; Sanz, J., 2006].

Ex. 6: Travelling Ionospheric Disturb.

Exercise: Execute in a single line:

```
# a) Reading RINEX files:
gLAB_linux -input:cfg meas.cfg -input:obs mhcb2910.01o > mhcb.meas
gLAB_linux -input:cfg meas.cfg -input:obs monb2910.01o > monb.meas
gLAB_linux -input:cfg meas.cfg -input:obs sodb2910.01o > sodb.meas
```

```
# b) Selecting satellite PRN16:
gawk '{if ($6==14) print $0}' mhcb.meas > mhcb_14.meas
gawk '{if ($6==14) print $0}' monb.meas > monb_14.meas
gawk '{if ($6==14) print $0}' sodb.meas > sodb_14.meas
```

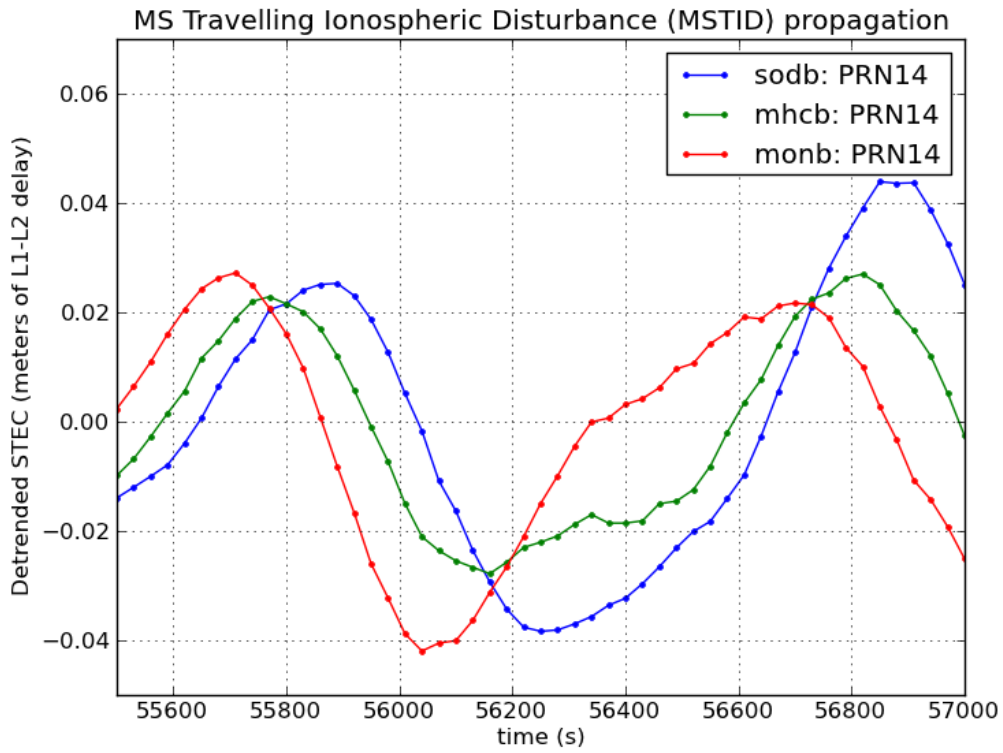


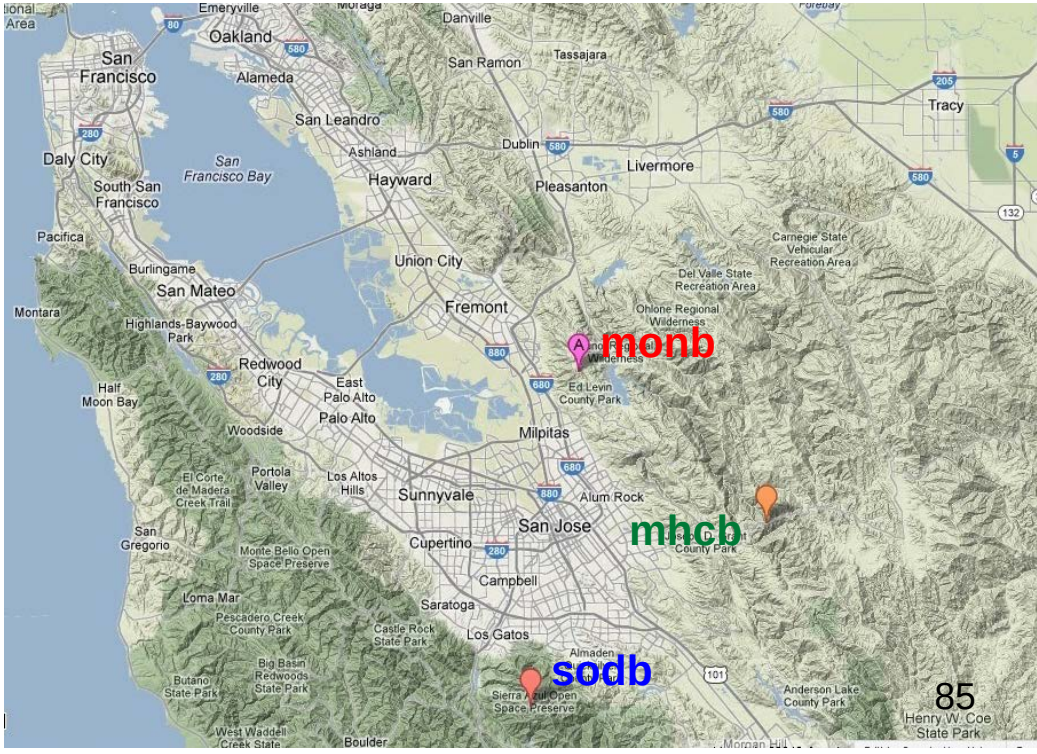

```
# c) Detrending on the geometry-free combination L1-L2:

gawk '{for (i=0;i<21;i++) {t[i]=t[i+1];l[i]=l[i+1]};t[21]=$4;l[21]=$14-$16;
      if (NR>21){tt=t[0]*t[10]*t[20];if (tt!=0) print t[10],(l[10]-(l[0]+l[20])/2)}}' mhcb_14.meas > mhcb_dLi.meas

gawk '{for (i=0;i<21;i++) {t[i]=t[i+1];l[i]=l[i+1]};t[21]=$4;l[21]=$14-$16;
      if (NR>21){tt=t[0]*t[10]*t[20];if (tt!=0) print t[10],(l[10]-(l[0]+l[20])/2)}}' monb_14.meas > monb_dLi.meas

gawk '{for (i=0;i<21;i++) {t[i]=t[i+1];l[i]=l[i+1]};t[21]=$4;l[21]=$14-$16;if (NR>21){tt=t[0]*t[10]*t[20];
      if (tt!=0) print t[10],(l[10]-(l[0]+l[20])/2)}}' sodb_14.meas > sodb_dLi.meas
```

Ex. 6: Travelling Ionospheric Disturb.

Execute in a single line:

```
graph.py -f sodb_dLi.meas -s.- --l "sodb: PRN14"
         -f mhcb_dLi.meas -s.- --l "mhcb: PRN14"
         -f monb_dLi.meas -s.- --l "monb: PRN14"
         --xn 55500 --xx 57000 --yn -0.05 --yx 0.07
         --xl "time (s)" --yl  "Detrended STEC (meters of L1-L2 delay)"
         -t "MS Travelling Ionospheric Disturbance (MSTID) propagation"
```





OVERVIEW

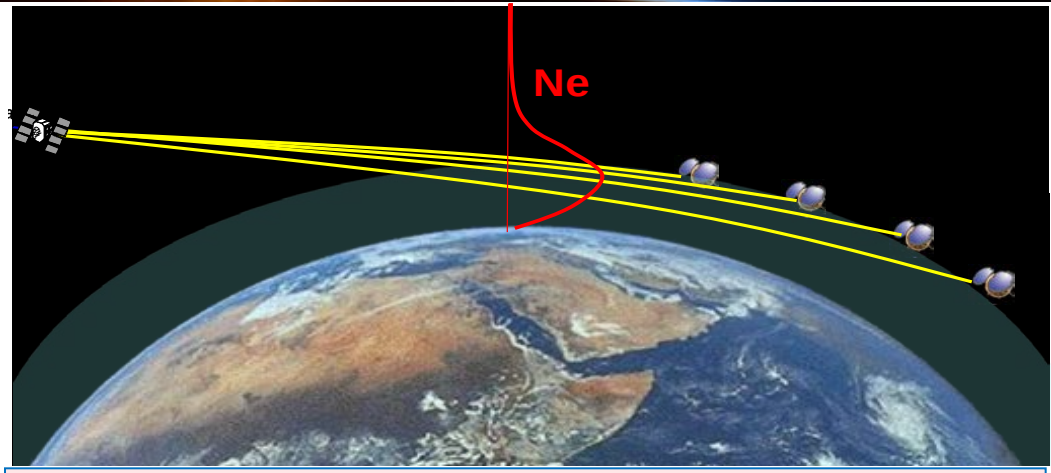
- Introduction
- The gLAB tool suite
- Examples of GNSS processing using gLAB
- Laboratory session organization

LABORATORY Session

- Starting up your laptop
- **Basic:** Introductory lab exercises: Iono & Posit, SF, storm,TIDs
- **Medium: Laboratory Work Projects: LWP1 to LWP4**
- **Advanced:** Homework

LWP1: Electron Density Profile from RO

In the previous Exercise #2 the variation of the Integrated Electron Content along the ray path (STEC) has been shown. From these integrated measurements during an occultation it is possible to retrieve the electron density profile (i.e., *Ne(h)*) of the ionosphere.

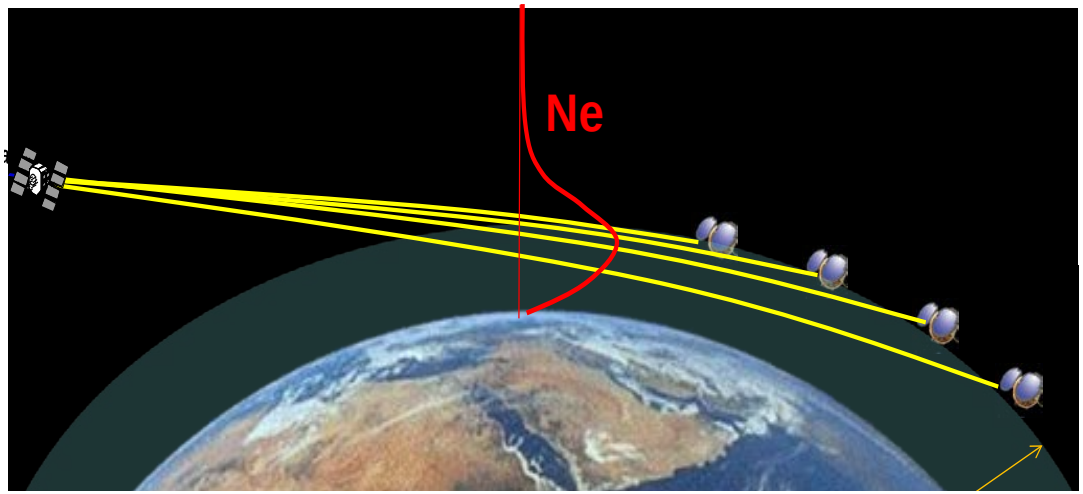


LWP1: Target

In this LWP we will retrieve the Ne(h) using a simple numerical algorithm which is equivalent to the Abel transform (see [R-6]).

LWP1: Electron Density Profile from RO

- The basic observable of this technique is the additional delay, due to the refractivity index, of a radio signal when passing through the atmosphere.
- This additional delay is proportional to the integrated refractivity, in such a way that we can obtain an estimation of the vertical refractivity profiles using observations at different elevation angles by solving an inverse problem.
- Traditionally, the solution of this inverse problem is obtained by using the **Abel inversion** algorithm assuming a refractivity index that only depends on the altitude (see [RD-6])



As it is know, *STEC* and *Ne* are related by:

$$STEC(p) = \int_{GPS}^{LEO} N_e \, dl$$

An equivalent expression, assuming spherical symmetry

$$STEC(p_n) \simeq 2\sum_{i=1}^{n} N_e(p_i)\, l_{i,n}$$

where ***p*** stands for the **impact parameter** (the closest point to the Earth centre along the optical ray path).

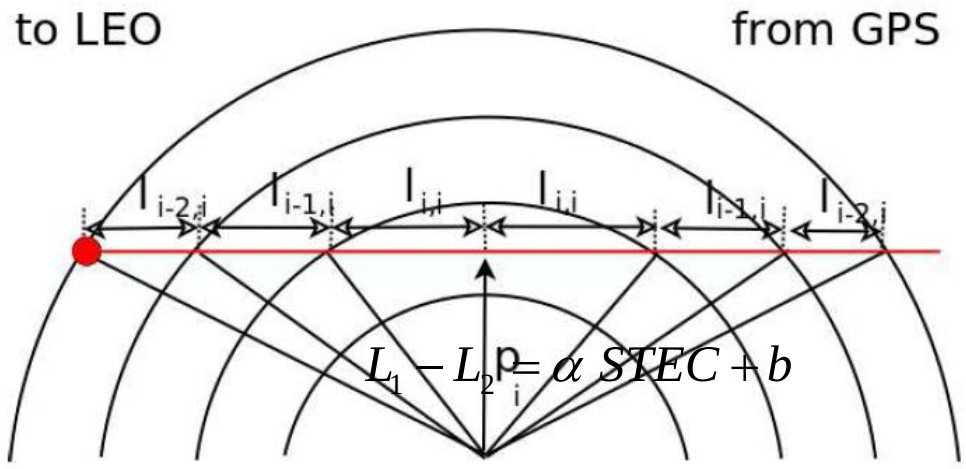
LWP1: Electron Density Profile from RO

Thence, starting from the outer ray ($p_1=r_{LEO}$), for a given ray *i*, where *i=1,…*, with impact parameter p_i, its STEC can be written in a discrete representation as:

$$STEC(p_i) = 2\,N_e(p_i)\,l_{i,i} + \sum_{j=1}^{j=i-1} N_e(p_j)\,l_{i,j}$$

where l_{ji} is the fraction of *i*th ray within the spherical layer *i*th (see [R-6]).

The previous equation defines a triangular linear equations system that can be solved recursively for the electron density *Ne(p).*



where ***p*** stands for the **impact parameter** (the closest point to the Earth centre along the optical ray path).

As measurements we use *L1-L2* carrier phases that are related with the STEC by:

$$L_1 - L_2 = \alpha\ STEC + b$$

where the bias term ***b*** is eliminated making differences to a reference in the arch data.

LWP1: Electron Density Profile from RO

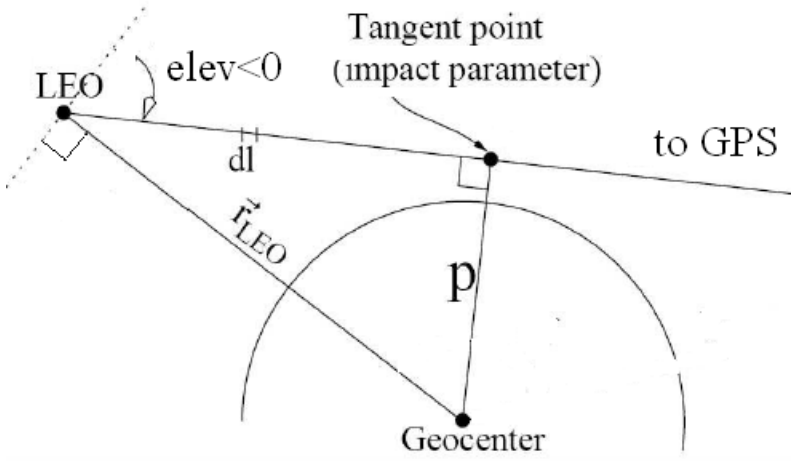
The program "`abel.perl`" implements the previous algorithm to estimate the *Ne(p)* profile from GPS L1-L2 carrier measurements.

- **The input data is `[p(n),L1-L2(n)]`**, with *p* in km and *L1-L2* in meters (of L1-L2 delay)
  where the impact parameter must be sorted from larger to lower value.
  ➔ Only measurements with negative elevation must be given (i.e., occultation).

- **The output data is: `[n,p(n),L1-L2(n),Ne(n)]`,**
  where Ne is given in e^-/m^3.

Note: the Impact parameters can be computed from the LEO elevation (elev) and its distance to Earth's centre (r_{LEO}) by (see figure):

$$p = r_{LEO}\cos(elev)$$



LWP1: Electron Density Profile from RO

Exercise:

The file “RO.obs” contains the following fields (see Ex.5):

```
                                  |<------ LEO ------>|<------- GPS ------->|
YY DoY HH.HH CODE PRN  elev  r_LEO AR_LEO DEC_LEO  r_GPS AR_GPS DEC_GPS   L1  L2   L1-L2 arc
                       (deg)  (km) (Deg)   (Deg)    (km)  (Deg)  (Deg)   (cycles)   (m)
 1   2    3     4    5    6     7     8       9       10     11     12     13  14    15   16
```

1.- Using the file **RO.obs**, select the measurements with negative elevations for GPS satellite PRN02, the LEO #4 and antenna #1, and generate the input file **[p(n),L1-L2(n)]** for program “**abel.perl**”

```
- Selecting: CODE=l241 and PRN=02 and negative elevations (ocult)
  grep l241 RO.obs|gawk '{if ($5==02 && $6<0) print $0}'> ro.tmp

- Generating the input file
  gawk '{printf "%9.5f %7.5f \n",$7*cos($6*3.14/180),$15}' ro.tmp > abl.tmp

- Sort the file by impact parameter:
  sort –nr –k+1 abl.tmp > abl.dat
```

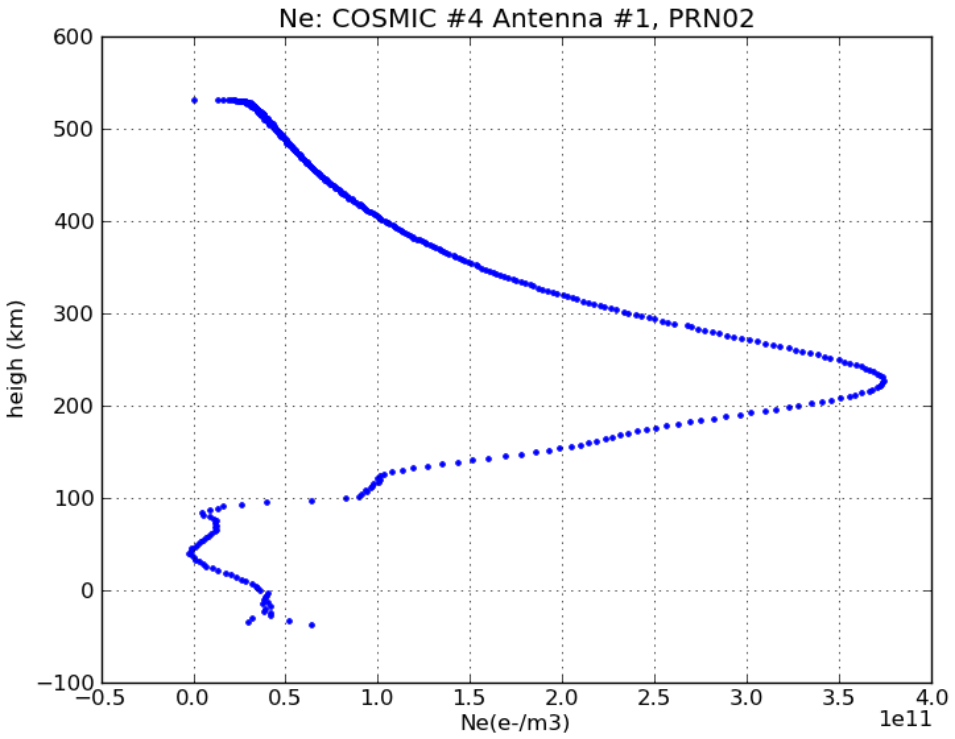
LWP1: Electron Density Profile from RO

2.- Run the program **"abel.perl"** over the generated file **"abl.dat"** to compute the electron density profile Ne(p):

```
- Sort the file by impact parameter:
  cat abl.dat| abel.perl > Ne.dat
```

3.- The output file **"abl.dat"** contains the fields **[n,p(n),L1-L2(n),Ne(n)]**
Plot the electron density profile Ne as a function the impact parameter p and as a function of height above Earth's

```
- Plot1: As a function of "p"
  graph.py -f Ne.dat -x4 -y2
       --xl "Ne(e-/m3)" --yl "p (km)"
- Plot2: As a function of "height"
  graph.py -f Ne.dat -x4 -y'($2-6370)'
       --xl "Ne(e-/m3)" --yl "h (km)"
```



LWP1: Electron Density Profile from RO

Questions

1. Taking into account the relationship between the electron density (N_e) and the critical frequency (f_p), i.e., minimum frequency for a signal not being reflected, [R-1]:

$$f_p = 8.98\sqrt{N_e} \quad (N_e \text{ in } \mathrm{e^-/m^3},\ f_p \text{ in Hz})$$

   Compute the minimum frequency of a signal to cross through the ionosphere.

   Answer:
   From previous plot, the N_e of the maximum is 3.7E+11 e^-/m^3. Thence

$$f_p = 8.98\sqrt{3.7\cdot 10^{11}} = \quad 5.46 MHz$$

2. Calculate the height where a signal with frequency *f=4* MHz will be reflected, according to the previous plot of N_e profile.

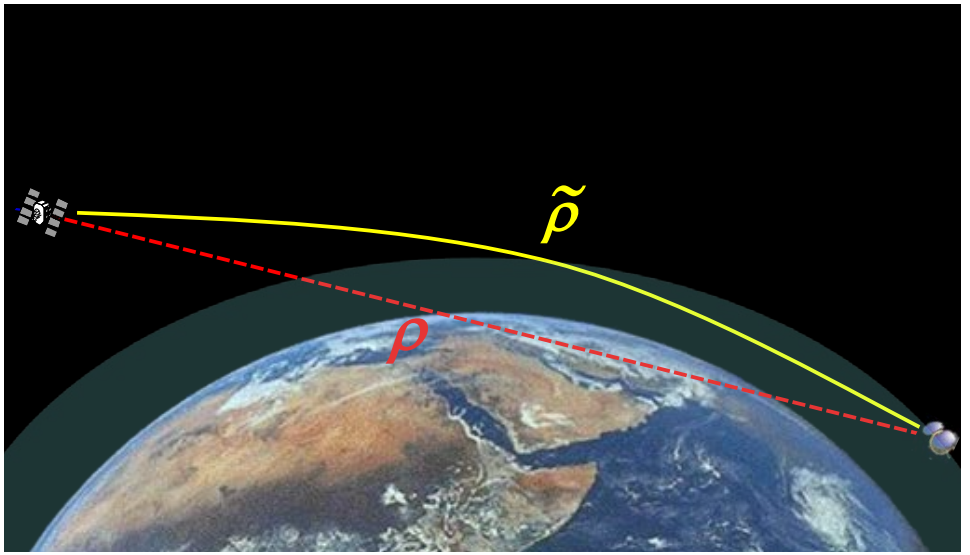
   Answer:

$$N_e = (f\ / 8.98)^2 = (4\cdot 10^6\ / 8.98)^2 = 1.98\cdot 10^{11} \Rightarrow \sim 150 \text{ km}$$

LWP2: Atmospheric Bending in RO

LWP2: Target

This LWP is focused in depicting and analysing the effect of the atmospheric bending in Radio Occultation measurements.



A simple procedure will be given to depict the phase excess rate due to the troposphere and ionosphere over L1, L2 and LC measurements.

Note: LC is the Ionosphere Free combination of carriers L1 and L2 is given by:

$$LC = \frac{f_1^2 L1 - f_2^2 L2}{f_1^2 - f_2^2}$$

LWP2: Atmospheric Bending in RO

Let L_1 be the carrier measurement at frequency f_1. A procedure to depict the L1 bending is given next:

$$L_1 = \rho^* + cdt_{rec}^{sat} + B_1; \quad \rho^* = \tilde{\rho} + T - \tilde{\alpha}_1 I$$

being ρ the Euclidean distance between GPS and LEO and B a constant bias along continuous phase arc

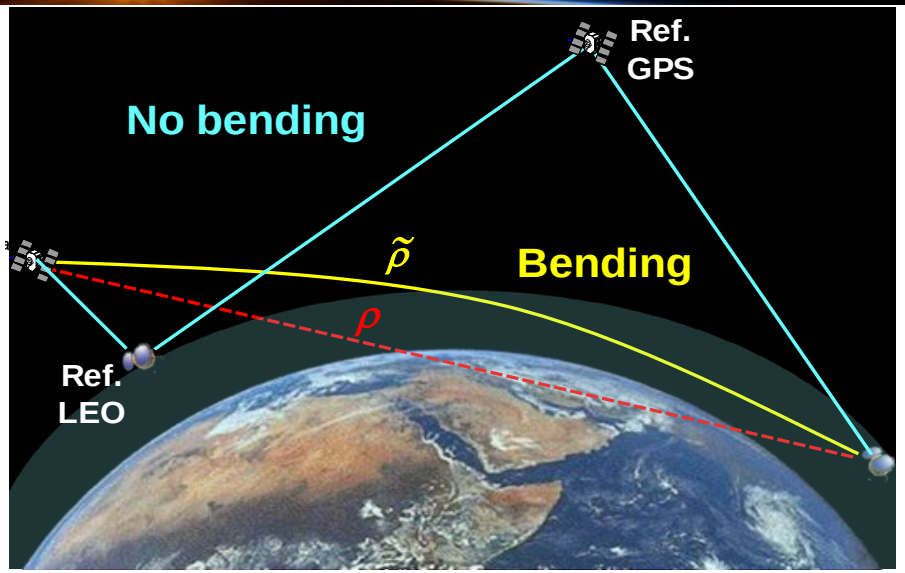
- **The bias B cancels, taking time differences of *L1.***
  Thence, from previous equation, it follows

$$\frac{\Delta\rho^*}{\Delta t} = \left(\frac{\Delta L_1}{\Delta t} - \frac{\Delta cdt_{rec}^{sat}}{\Delta t} \right)$$

- **And clocks cancel taking Double-Differences between pairs of LEO and GPS satellites:**

$$DD\frac{\Delta\rho^*}{\Delta t} = DD\frac{\Delta L_j}{\Delta t}$$

Assuming NO Bending in the other Sat-Sat measurements



Reference satellites (GPS, LEO) are taken **in NON-OCULTATION** .

$$\frac{\Delta\rho^*_{occult}}{\Delta t} - \frac{\Delta\rho_{occult}}{\Delta t} = DD\frac{\Delta L_j}{\Delta t} - DD\frac{\Delta\rho}{\Delta t} \neq 0$$

Note: LEO and GPS orbits are known at the level of few cm (~5cm), thus the Euclidean range can be calculated accurately and, thus, the range rate $\frac{\Delta\rho}{\Delta t}$

$$DD(\bullet) = \left[(\bullet)_{LEO}^{GPS} - (\bullet)_{LEO}^{GPS_{Ref}} \right] - \left[(\bullet)_{LEO_{Ref}}^{GPS} - (\bullet)_{LEO_{Ref}}^{GPS_{Ref}} \right]$$

LWP2: Atmospheric Bending in RO

Next expressions generalize previous results for L1, L2 and Lc measurements:

$$L_j = \rho^* + cdt_{rec}^{sat} + B_j; \quad \boxed{\rho^* = \tilde{\rho} + T - \tilde{\alpha}_j I}; \quad j = 1,2$$

$$L_C = \rho^{\odot} + cdt_{rec}^{sat} + B_C; \quad \boxed{\rho^{\odot} = \tilde{\rho} + T}$$

The differences in time to depict the bending

$$\frac{\Delta\rho^*}{\Delta t} = \frac{\Delta L_j}{\Delta t} - \frac{\Delta cdt_{rec}^{sat}}{\Delta t} \Rightarrow DD\frac{\Delta\rho^*}{\Delta t} = DD\frac{\Delta L_j}{\Delta t}$$

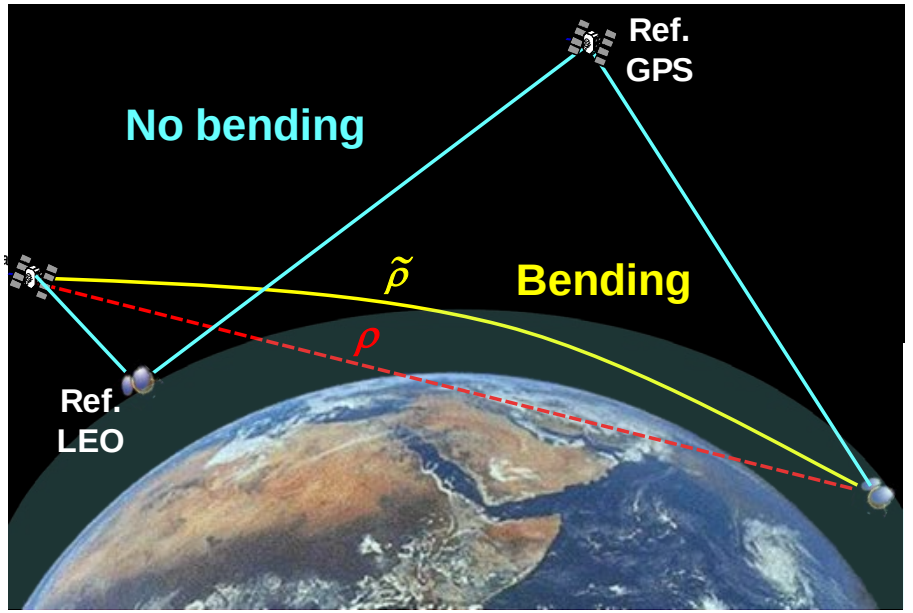
$$\frac{\Delta\rho^{\odot}}{\Delta t} = \frac{\Delta L_C}{\Delta t} - \frac{\Delta cdt_{rec}^{sat}}{\Delta t} \Rightarrow DD\frac{\Delta\rho^{\odot}}{\Delta t} = DD\frac{\Delta L_C}{\Delta t}$$

And the clock term cancels taking Double Differences between LEO and GPS satellites

$$\frac{\Delta\rho^*_{occult}}{\Delta t} - \frac{\Delta\rho_{occult}}{\Delta t} = DD\frac{\Delta L_j}{\Delta t} - DD\frac{\Delta\rho}{\Delta t} \neq 0 \quad ; \quad j = 1,2$$

$$\frac{\Delta\rho^{\odot}_{occult}}{\Delta t} - \frac{\Delta\rho^*_{occult}}{\Delta t} = DD\frac{\Delta L_C}{\Delta t} - DD\frac{\Delta\rho}{\Delta t} \neq 0$$

Carrier Excess Rate



Reference satellites (GPS, LEO) are taken **in NON-OCULTATION** .

Bending is assumed only for the GPS-LEO ray in occultation.

$$DD(\bullet) = \left[(\bullet)^{GPS}_{LEO} - (\bullet)^{GPS_{\text{Ref}}}_{LEO}\right] - \left[(\bullet)^{GPS}_{LEO_{\text{Ref}}} - (\bullet)^{GPS_{\text{Ref}}}_{LEO_{\text{Ref}}}\right]$$

LWP2: Atmospheric Bending in RO

Another possibility to remove the clock term, could be to subtract the LC combination from L1 (or L2). The result will provide the "discrepancy between L1 (or L2) and LC excess ray path.

That is:

$$\left.\begin{aligned} \frac{\Delta\rho^{*}_{occult}}{\Delta t} &= \frac{\Delta L_j}{\Delta t} - \frac{\Delta c dt^{sat}_{rec}}{\Delta t}; \quad j=1,2 \\ \frac{\Delta\rho^{\odot}_{occult}}{\Delta t} &= \frac{\Delta L_C}{\Delta t} - \frac{\Delta c dt^{sat}_{rec}}{\Delta t} \end{aligned}\right\} \Rightarrow \frac{\Delta\rho^{*}_{occult}}{\Delta t} - \frac{\Delta\rho^{\odot}_{occult}}{\Delta t} = \frac{\Delta L_j}{\Delta t} - \frac{\Delta L_C}{\Delta t}; \quad j=1,2$$

Notice that the Euclidian range rate is not needed to subtract as in the previous case, because it is cancelled when taking the difference between L1 (or L2) and Lc. Other delays can also be cancelled...

In the following exercises, we will plot the previous combinations and discuss the different contribution of the ionosphere and troposphere to the phase excess rate.

LWP2: Atmospheric Bending in RO

Exercise:

The program "`RO.perl`" uses the **"RO.obs"** as input data and computes the following combinations of RO measurements:

The output file:

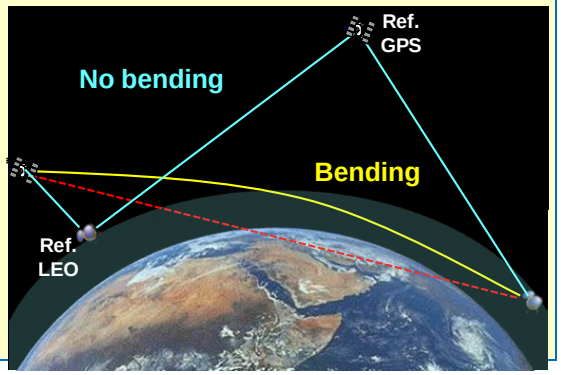
1	2	3	4	5	6	7	8	9	10	11	12	13	14
sec	CODE	PRN	p	dRho	dL1	dL2	dLc	d(L1-Lc)	d(L2-Lc)	DDdRho	DDdL1	DDdL2	DDLc
								(units m/s)					

where

- Rho is the Euclidean Distance between GPS and LEO
- d: means differences in time
- DD: means Double Differences between GPS and LEOs satellites.

  Note: the GPS **PRN13** and **LEO "I252"** are used as **reference satellites**.
  (the rays between these satellites are not in occultation).

The results are computed for the RO between **GPS PRN02** and **LEO "I241"** (the same occultation as in previous cases)



The aim of this exercise is to analyse the phase excess rate in the different combinations due to the bending of the ray.

LWP2: Atmospheric Bending in RO

1.- Run the program "RO.perl" over the file "RO.obs" and generate the combinations of measurements indicated in the previous table.

Note: the results are provided for the occultation associate to PRN=02 and "CODE=1241", that corresponds to LEO=4 and Antenna 1.
This is hard code in the program, but can be changed, as well.

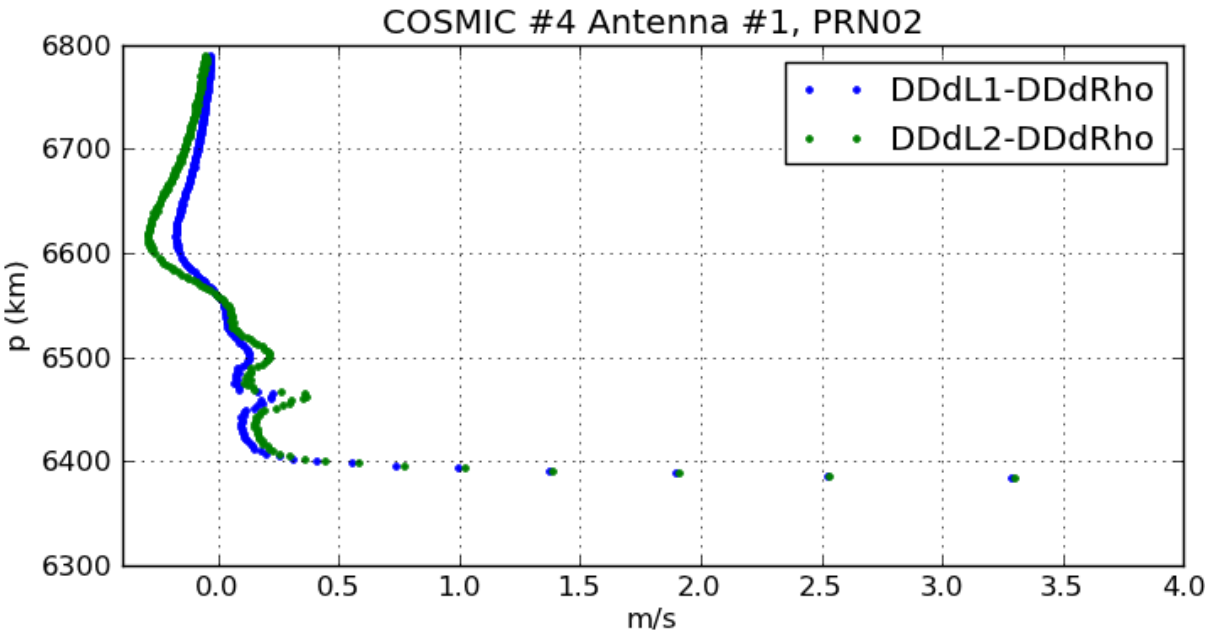
```
- Execute (the file RO.obs, must be available in the directory)

  RO.perl > bending.dat
```

2.- Discuss next plots:

LWP2: Atmospheric Bending in RO

P1.- Plot "DDdL1-DDdRho" and DDdL2-DDdRho as a function of time and discuss the results found

```
graph.py -f bending.dat -x'($12-$11)' -y4  -l "DDdL1-DDdRho"
         -f bending.dat -x'($13-$11)' -y4  -l "DDdL2-DDdRho"  --xn -0.4 --xx 4
```



Q1: Justify the discrepancy between the two plots.

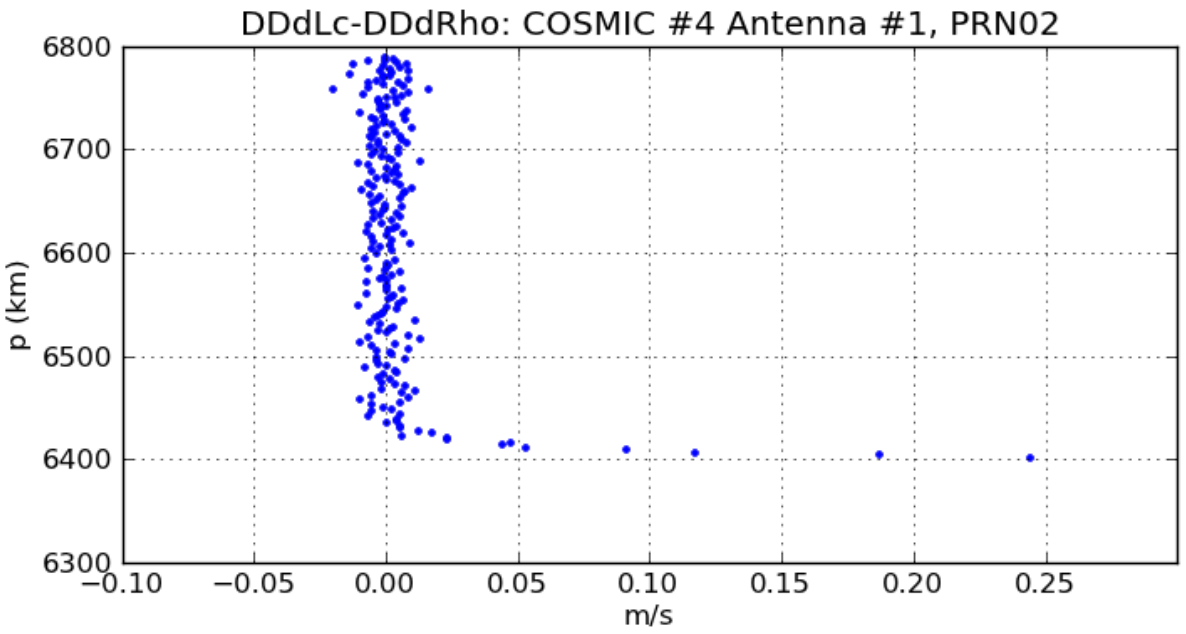
Answer 1:

- The curves in the plot show phase excess rate due the effect of both ionosphere and troposphere.
- As the bending in the ionosphere is a frequency dependent effect, the contribution is different for each signal (L1 and L2).

LWP2: Atmospheric Bending in RO

P2.- Plot DDdLc-DDdRho as a function of time. Discuss results.

```
graph.py -f bending.dat -x'($14-$11)' -y4 --xn -0.1 --xx 0.3 --xl "m_Lc/s"
         --yl "p (km)" -t"DDdLc-DDdRho: COSMIC #4 Antenna #1, PRN02"
```



Q2: Why there is no excess ray path for p> 6420 km?

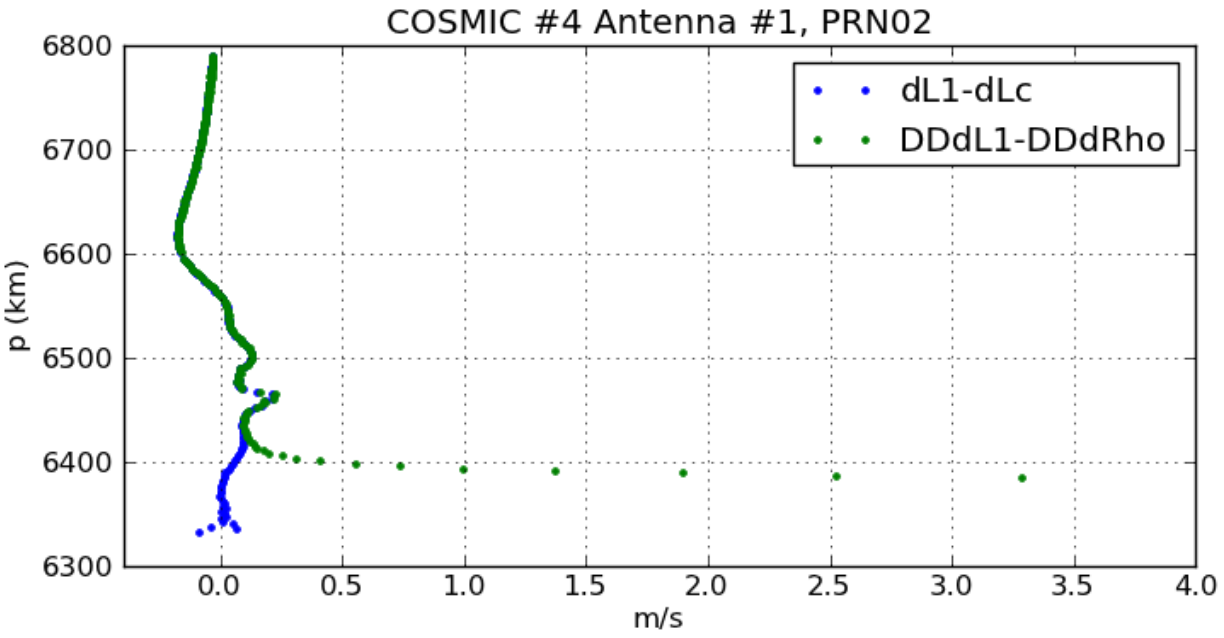
Answerer 2:

- The ionospheric bending effect on L1 and L2 is proportional to the inverse of squared frequencies and cancels in the ionosphere-free combination of carriers Lc.
- There is only bending effect in Lc due to the troposphere, which produces the path at the bottom of the figure.

LWP2: Atmospheric Bending in RO

P3.- Plot "dL1-dLc" and DDdL1-DDdRho as a function of time. Discuss results.

```
graph.py -f bending.dat –x9 -y4 -l "dL1-dLc"
         -f bending.dat -x'($12-$11)' –y4 -l "DDdL1-DDdRho"
          --xl "m_L1/s" --yl "p (km)" --xn -0.4 --xx 4 -y4
```



Q3: Justify the discrepancy between the two plots.

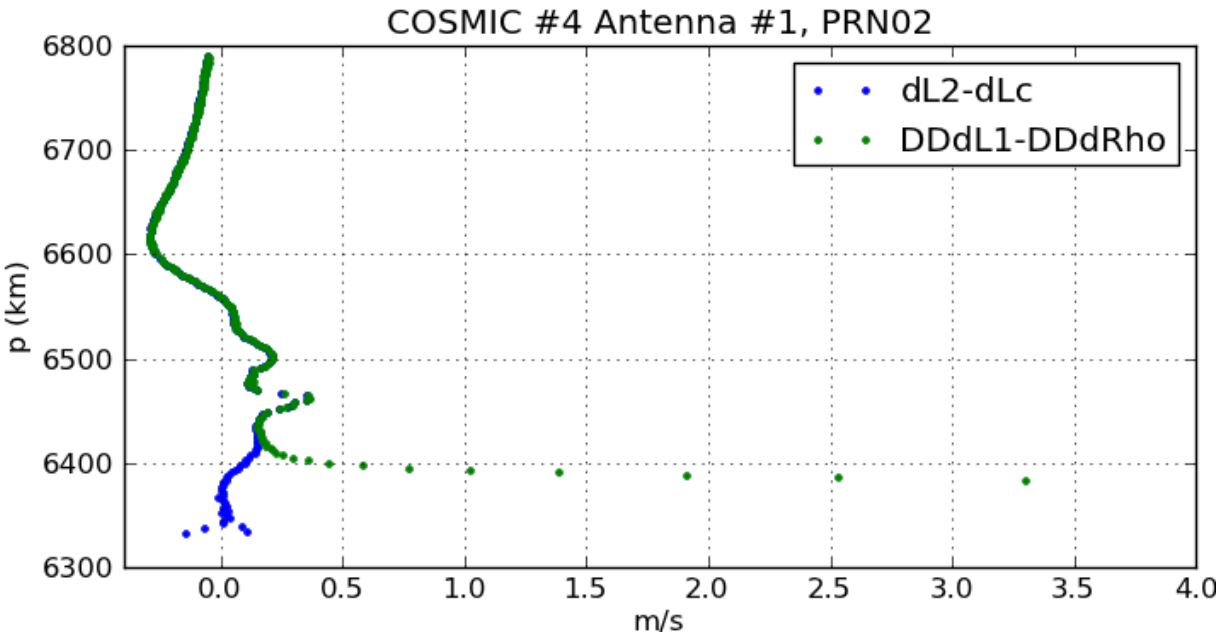
Answer 3:

- DDdL1-DDdRho accounts for the contribution of ionosphere and troposphere. The troposphere produces the large drift at the bottom.
- dL1-dLc cancels common effects in both signals, like troposphere and ionosphere. But, as there is no bending effect due to the ionosphere on Lc (see previous plot P2) , thence, the curves match for *p> 6420 km.*

LWP2: Atmospheric Bending in RO

P4.- Plot "dL2-dLc" and DDdL2-DDdRho as a function of time. Discuss results.

```
graph.py -f bending.dat –x10 -y4 -l "dL2-dLc"
         -f bending.dat -x'($13-$11)' –y4 -l "DDdL1-DDdRho"
          --xl "m_L2/s" --yl "p (km)" --xn -0.4 --xx 4 -y4
```



Q4: Justify the discrepancy between the two plots.

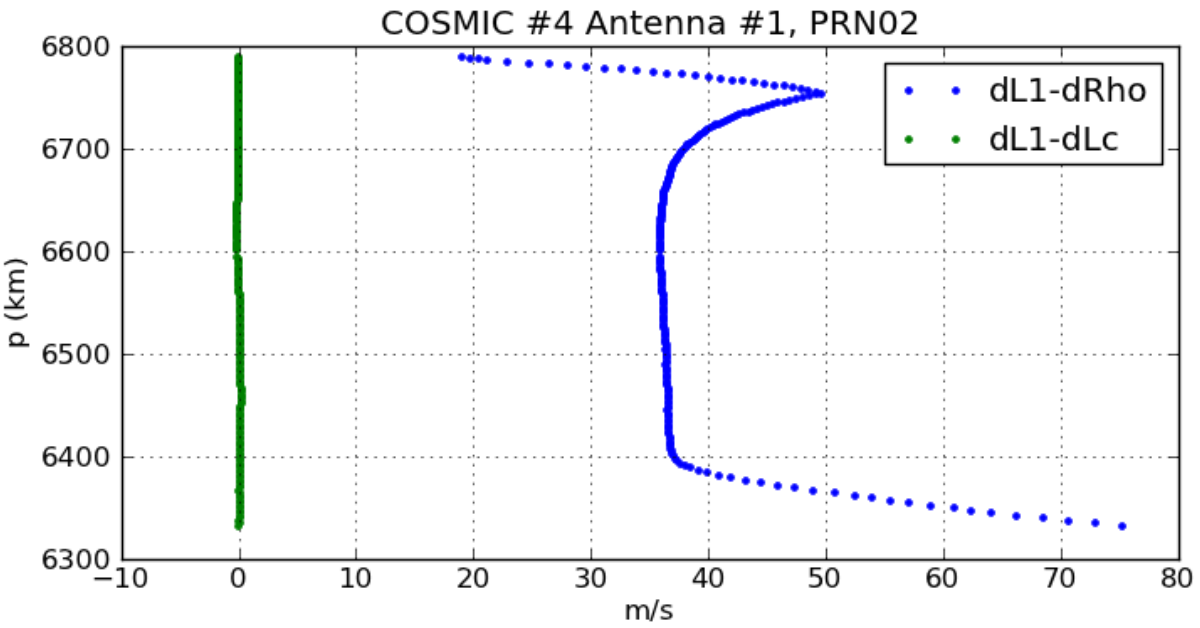
Answer 4:

- The same answer as in previous plot.

LWP2: Atmospheric Bending in RO

P5.- Plot "dL1-dRho" and dL1-dLc as a function of time. Discuss results.

```
graph.py -f bending.dat -x'($6-$5)' -y4 -l "dL1-dRho"
         -f bending.dat –x9 -y4 -l "dL1-dLc"
         --xl "m_L1/s" --yl "p (km)" -t"COSMIC #4 Antenna #1, PRN02"
```



Q5: Justify the discrepancy between the two plots.

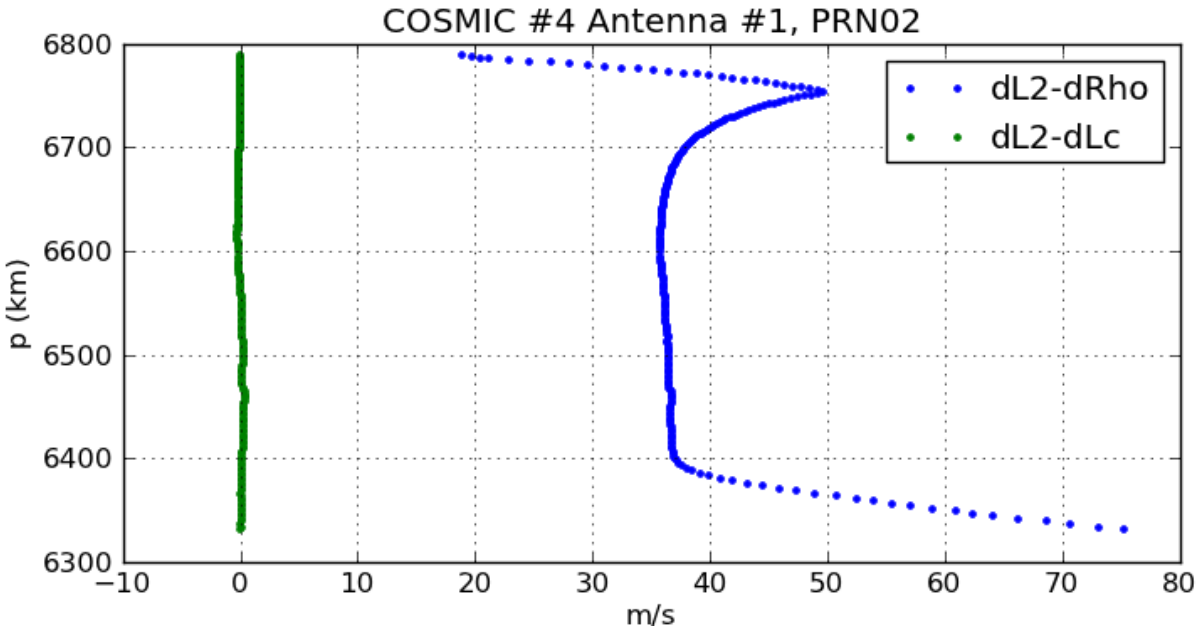
Answer 5:

- The large drift in dL1-dRho curve is due to the satellites (GPS and LEO) clock drift.
- These large clock variations do not allow to see the atmospheric bending effect.

LWP2: Atmospheric Bending in RO

P6.- Plot "dL2-dRho" and dL2-dLc as a function of time. Discuss results.

```
graph.py -f bending.dat -x'($7-$5)' -y4 -l "dL2-dRho"
         -f bending.dat –x10 -y4 -l "dL2-dLc"
         --xl "m_L2/s" --yl "p (km)" -t"COSMIC #4 Antenna #1, PRN02"
```

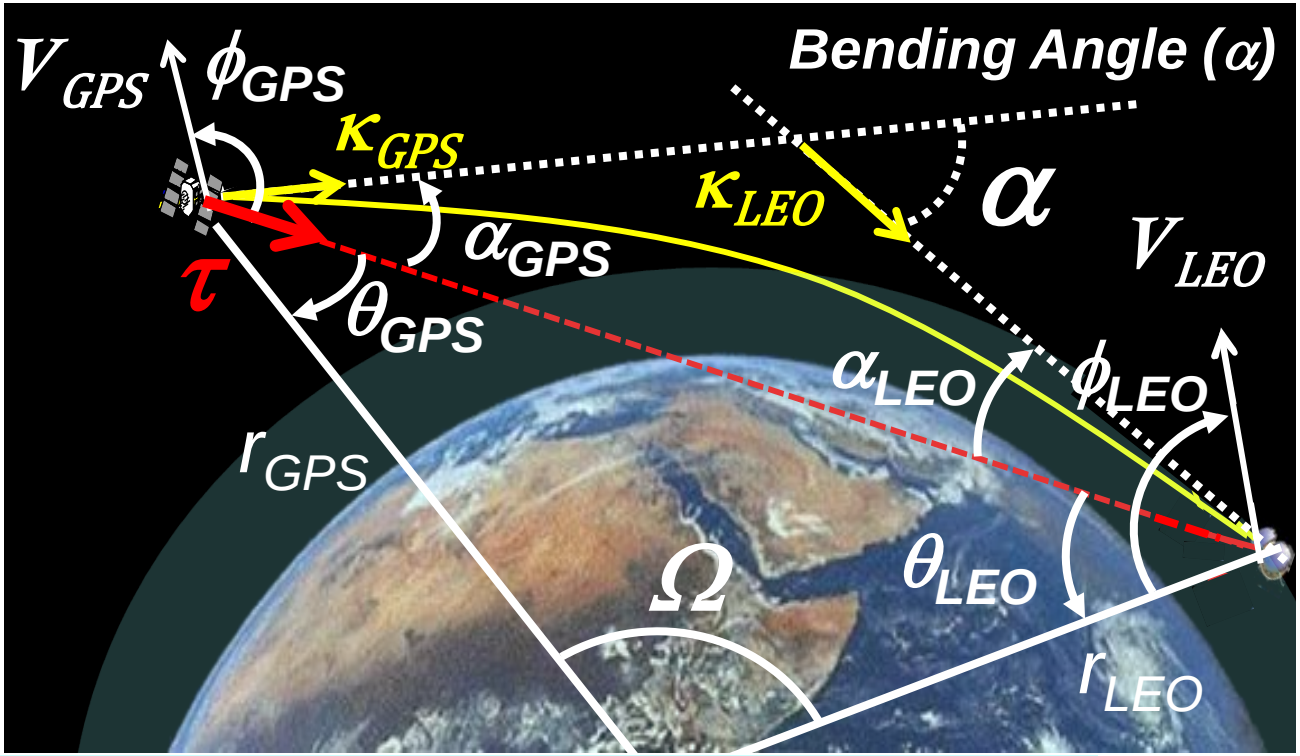


Q6: Justify the discrepancy between the two plots.

Answer 6:

- The same answer as in previous plot.

LWP2: Atmospheric Bending in RO

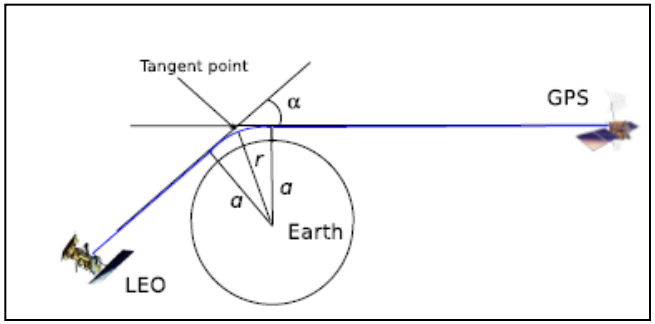


Derivation of bending angle $\alpha(a)$ from Excess Phase Rate (or Atmospheric Doppler Shift $\lambda\Delta f$)

$$\frac{\Delta\rho_{occult}}{\Delta t} = (\mathbf{v}_{GPS} - \mathbf{v}_{LEO})\cdot\boldsymbol{\tau}$$

$$\frac{\Delta\rho^{*}_{occult}}{\Delta t} = \mathbf{v}_{GPS}\cdot\mathbf{k}_{GPS} - \mathbf{v}_{LEO}\cdot\mathbf{k}_{LEO}$$

$$\lambda\Delta f = \frac{\Delta\rho^{*}_{occult}}{\Delta t} - \frac{\Delta\rho_{occult}}{\Delta t} = DD\frac{\Delta L_j}{\Delta t} - DD\frac{\Delta\rho}{\Delta t}$$



$$\lambda\Delta f = \mathbf{v}_{GPS}\cdot(\mathbf{k}_{GPS} - \boldsymbol{\tau}) - \mathbf{v}_{LEO}\cdot(\mathbf{k}_{LEO} - \boldsymbol{\tau})$$

$$n_{GPS}\, r_{GPS}\sin(\alpha_{GPS} + \theta_{GPS}) = n_{LEO}\, r_{LEO}\sin(\alpha_{LEO} + \theta_{LEO}) = a$$

$$\alpha = \alpha_{GPS} + \alpha_{LEO}$$

The Bending Angle $\alpha(a)$ can be derived iteratively from this equations system (see, [R-7])

LWP2: Atmospheric Bending in RO

Comments:

From phase excess rate measurements the bending angle can be estimated. From the bending angle, the variations of the refractivity can be computed, and from these one can then derive atmospheric quantities such as Pressure, Temperature and the partial pressure of water vapor, and electron density, among others.

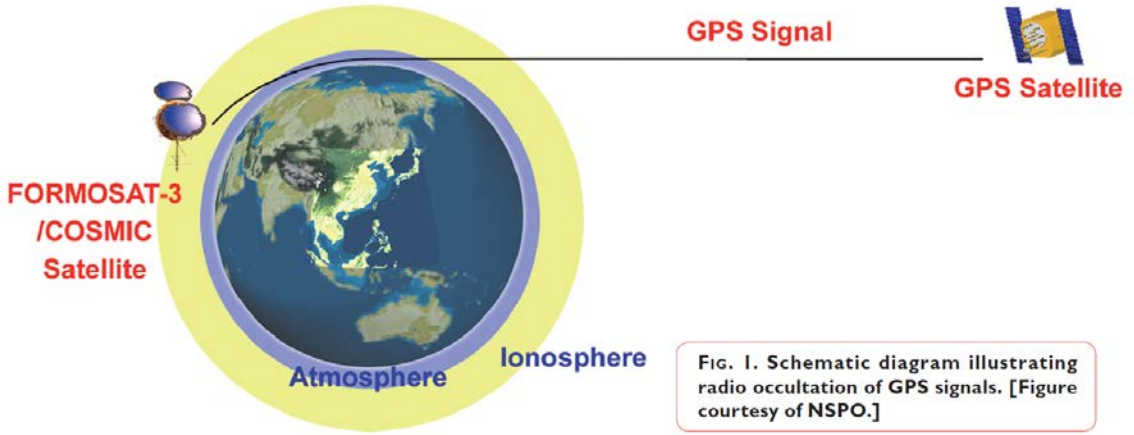
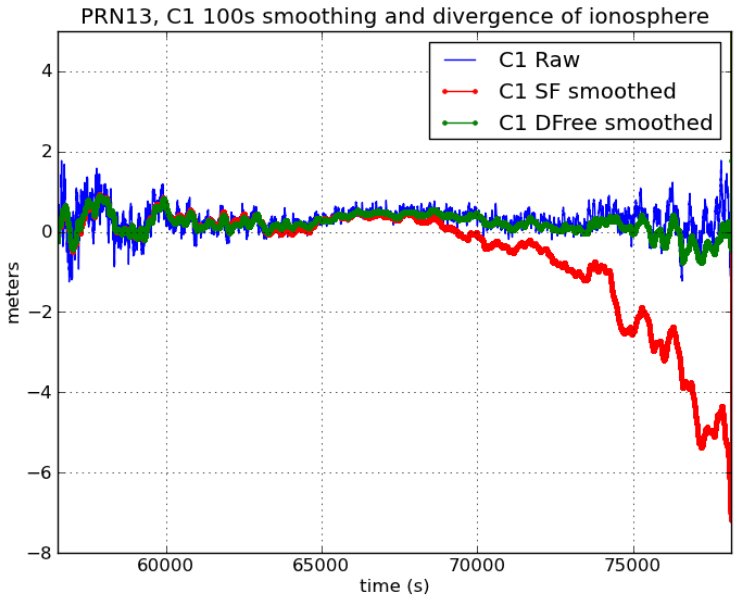


FIG. 1. Schematic diagram illustrating radio occultation of GPS signals. [Figure courtesy of NSPO.]

LWP3: Iono. Divergence on Smoothing

The target of LWP3 is to analyze the error induced by the divergence of the ionosphere (between code and carrier) into the Single-Frequency (SF) carrier smoothed code.



The Divergence Free (Dfree) and the Ionosphere Free (IFree) smoothed codes will be compared with the SF one.

This effect will be analyzed analytically and tested with single and double frequency GPS measurements under large ionospheric gradients.

LWP3: Iono. Divergence on Smoothing

The noisy code can be smoothed with the precise (but ambiguous) carrier measurements. This carrier smoothing can be done in real-time applying the Hatch filter.

The smoothing depends on the time smoothing constant or filter length. The more the filter length is used, the more smoothed the code is, but (with single frequency measurements) a higher code-carrier divergence error is induced by the ionosphere.

This is because the ionospheric refraction has opposite sign on code and carrier, being its effect twice on the difference of code and carrier. This double ionospheric refraction is propagated forward through the filter, producing a bias.

The error induced by the code-carrier divergence of the ionosphere on the single frequency smoothed codes is assessed in this exercise for different filter lengths.

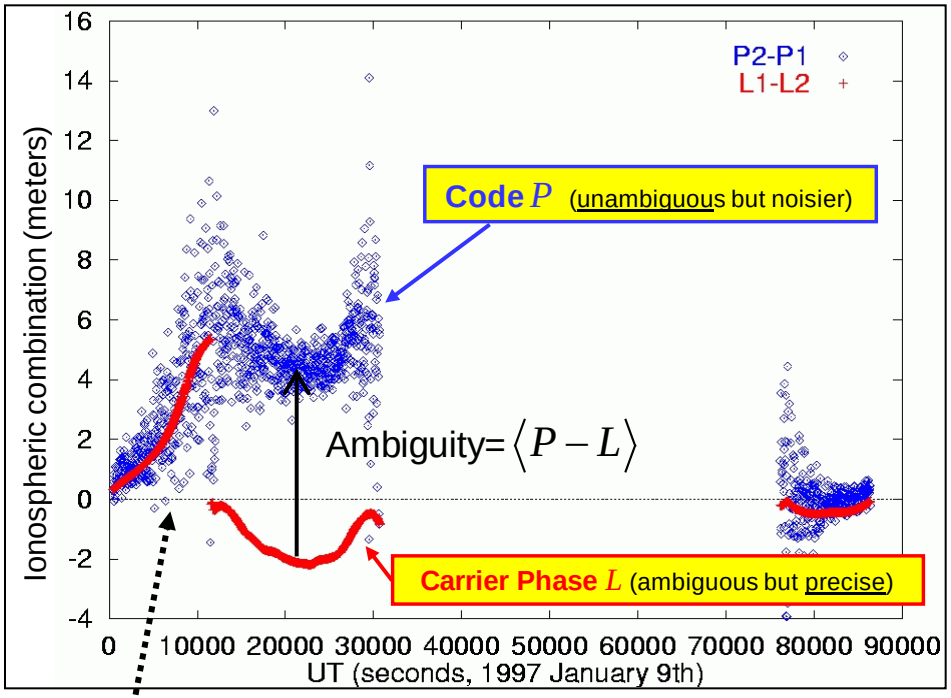
LWP3: Iono. Divergence on Smoothing

The noisy code P can be smoothed with the precise (but ambiguous) carrier L measurements. This carrier smoothing can be done in real-time applying the **Hatch filter**.

$$\hat{P}(k) = \frac{1}{n} P(k) + \frac{n-1}{n}\left(P(k-1) + L(k) - L(k-1)\right)$$

where $[n = k \text{ if } k < N]$, and $[n = N \text{ if } k \geq N]$.

The algorithm is initialised with: $\hat{P}(1) = P(1)$.



The previous algorithm can be interpreted as real-time alignment of carrier with code:

$$\hat{P}(k) = \frac{1}{n} P(k) + \frac{n-1}{n}\left(P(k-1) + L(k) - L(k-1)\right) = L(k) + \langle P - L \rangle_{(k)}$$

where

$$\langle P - L \rangle_{(k)} = \frac{1}{n}\left(P(k) - L(k)\right) + \frac{n-1}{n}\langle P - L \rangle_{(k-1)} \simeq \frac{1}{n}\sum\left(P(k) - L(k)\right)$$

LWP3: Iono. Divergence on Smoothing

Time varying ionosphere induces a bias in the single frequency smoothed code when it is averaged in the smoothing filter. This effect is analysed as follows:

Let:

$$P_1 = \rho + I_1 + \varepsilon_1$$
$$L_1 = \rho - I_1 + B_1 + \varsigma_1$$

Where ρ includes all non dispersive terms (geometric range, clock offsets, troposphere) and I_1 represents the frequency dependent terms (ionosphere and DCBs). B_1 Is the carrier ambiguity, which is constant along continuous carrier phase arcs and $\varepsilon_1, \varsigma_1$ account for code and carrier multipath and thermal noise.

thence,

$$P_1 - L_1 = 2I_1 - B + \varepsilon_1 \qquad \Rightarrow 2I_1 : \text{ Code-carrier divergence}$$

Note: the carrier noise ι_1 is neglected against code noise ε_1 .

Substituting $P_1 - L_1$ in Hatch filter equation (see the previous slide #110):

$$\hat{P}(k) = L(k) + \langle P - L \rangle_{(k)} = \rho(k) - I_1(k) + B_1 + \langle 2I_1 - B_1 \rangle_{(k)} =$$
$$= \rho(k) + I_1(k) + \underbrace{2\left(\langle I_1 \rangle_{(k)} - I_1(k)\right)}_{bias_I}$$

$$\Rightarrow \hat{P}_1 = \rho + I_1 + bias_I + \upsilon_1$$

where, being the ambiguity term B_1 a constant bias, thence $\langle B_1 \rangle = B_1$, and cancels in the previous expression

where υ_1 is the noise term after smoothing

LWP3: Iono. Divergence on Smoothing

Raw assessment of the induced bias on P_1 smoothed code by ionosphere:

- Let assume a simple model where the STEC vary linearly with time:

$$I_1(t) = I_{1_0} + I_1' \cdot t \quad \Rightarrow \quad \boxed{bias_I = 2\left(\langle I_1 \rangle_{(k)} - I_1(k)\right) = -2\tau I_1'}$$

where τ is the Hatch filter smoothing time constant (i.e., $\tau = N$ in previous eq.).

Exercise:

Proof the previous statement.

Solution:

Let be $f(t) \equiv I(t)$ *and* $y(t) \equiv \langle I \rangle_{(t)}$. *The averaging in the Hatch filter can be implemented as:*

$$y(t+\Delta T) = \frac{\tau - \Delta T}{\tau} y(t) + \frac{\Delta T}{\tau} f(t+\Delta T) \quad \Rightarrow \quad \frac{y(t+\Delta T) - y(t)}{\Delta T} + \frac{1}{\tau} y(t) = \frac{1}{\tau} f(t+\Delta T) \xrightarrow[\Delta T \to 0]{} \boxed{y' + \frac{1}{\tau} y = \frac{1}{\tau} f(t)}$$

Thence:

$$I_1(t) = I_{1_0} + I_1' \cdot t \quad \Rightarrow \quad \langle I_1 \rangle_{(t)} = I_1(t) - \tau I_1'\left(1 - e^{-t/\tau}\right) \Rightarrow \boxed{bias_I = 2\left(\langle I_1 \rangle_{(t)} - I_1(t)\right) \xrightarrow[t \to \infty]{} -2\tau I_1'}$$

LWP3: Iono. Divergence on Smoothing

- **Divergence Free smoothing (DFree):**

With 2-frequency measurements, the ionosphere can be removed from a combination of two carriers:

$$P_1 - L_1 - 2\alpha(L_1 - L_2) = B_{12} + \varepsilon_1 \quad \Rightarrow \quad \boxed{\hat{P}_1 = \rho + I_1 + \upsilon_{12}}$$

$$\alpha = \frac{f_2^2}{f_1^2 - f_2^2}$$

$$B_{12} = -B_1 - 2\alpha(B_1 - B_2)$$

➔**DFree** smoothed code is not affected by iono. temporal gradients, being the ionospheric delay the same as in the original code P_1 .

- **Ionosphere Free smoothing (IFree):**

Using both, code and carrier 2-frequency measurements, it is possible to remove the frequency dependent effects using the ionosphere-free combination P_C, L_C :

$$\begin{aligned} P_C &= \rho + \varepsilon_C \\ L_C &= \rho + B_C + \varsigma_C \end{aligned} \quad \Rightarrow \quad \boxed{\hat{P}_C = \rho + \upsilon_C}$$

$$P_C = \frac{f_1^2 P_1 - f_1^2 P_2}{f_1^2 - f_2^2}$$

$$L_C = \frac{f_1^2 L_1 - f_1^2 L_2}{f_1^2 - f_2^2}$$

➔**IFree** smoothed code is not affected by either spatial or temporal gradients, **but is 3-times noisier** than the DFree, or the in the Single Freq. smoothed code.

LWP3: Iono. Divergence on Smoothing

1.- Multipath and measurement noise assessment on raw code measurements:

The C1 code multipath and receiver noise can be depicted using the following combination (that removes all frequency dependent and not dependent terms):

$$M_{C_1} = C_1 - L_1 - 2\alpha(L_1 - L_2)$$

$$\alpha = \frac{f_2^2}{f_1^2 - f_2^2} = \frac{1}{\gamma - 1} = 1.545 \quad ; \quad \gamma = \left(\frac{77}{60}\right)^2$$

a) Generate the "meas" file for **PRN03**:

```
[Id YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2P L2P]
 1  2  3   4   5   6  7  8  9  10  11   12  13  14  15 16 ]
```

```
gLAB_linux -input:cfg meas.cfg -input:obs UPC33510.08O|gawk '{if ($6==03)print $0}'>upc3.meas
```

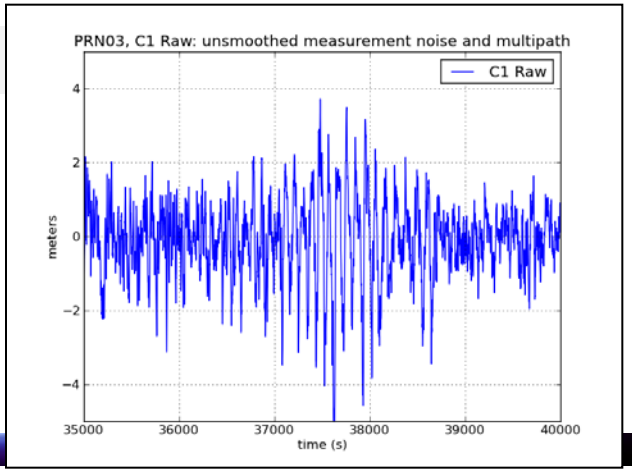
b) Using previous expression, compute the C1 multipath and code noise: :

```
gawk '{print $4,$11-$14-3.09*($14-$16)-21.3}' upc3.meas> upc3.C1
```

[*] results are Shifted by "-21.3" to remove the carrier ambiguity

c) Plot the raw (unsmoothed) measurements for PRN03:

```
graph.py -f upc3.C1 -s- --l "C1 Raw" --xn 35000 --xx 40000
         --yn -5 --yx 5  --xl "time (s)" --yl "meters"
         -t "PRN03, C1 Raw measurement noise and multipath"
```



LWP3: Iono. Divergence on Smoothing

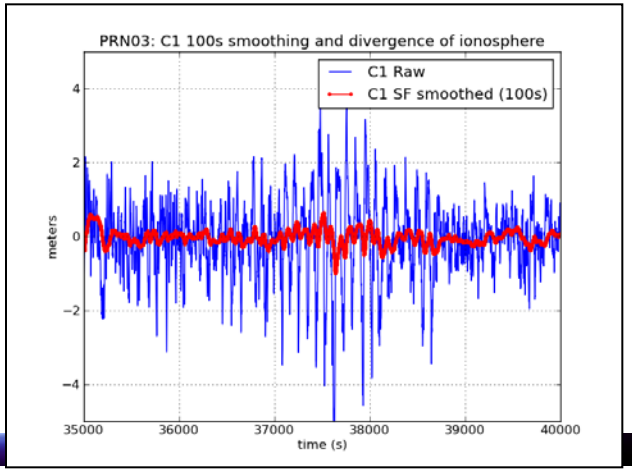
2. Apply the Hatch filter to smooth the code using a filter length of *N =100* sample (as the measurements are at *1Hz*,this means 100 seconds smoothing). Then, as in the previous case, depict the multipath and noise of the smoothed code.

a) Smoothing code (T=100sec):

```
gawk 'BEGIN{Ts=100}{if (NR>Ts){n=Ts}else{n=NR};
      C1s=$11/n+(n-1)/n*(C1s+($14-L1p));L1p=$14;
   print $4,C1s-$14-3.09*($14-$16)-21.3}' upc3.meas > upc3.C1s100
```

b) Plotting results and compare with the row C1.

```
graph.py -f upc3.C1 -s- --l "C1 Raw"
         -f upc3.C1s100 -s.- --cl r --l "C1 SF smoothed"
         --xn 35000 --xx 40000 --yn -5 --yx 5
         --xl "time (s)" --yl "meters"
         -t "PRN03: C1 100s smoothing and iono div."
```



LWP3: Iono. Divergence on Smoothing

3 . . Using 2-frequency carriers it is possible to generate a combination with the same ionospheric delay (the same sign) as the code to avoid the code-carrier divergence:

$$L_{1DFree} = L_1 + 2\alpha(L_1 - L_2) = \rho + I_1 + B + \zeta$$

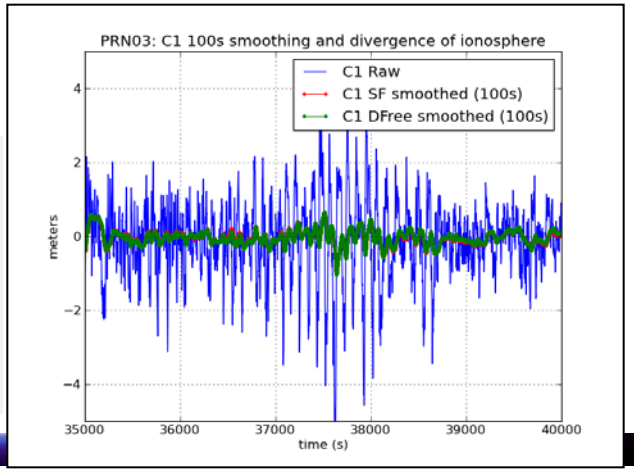
$$\alpha = \frac{f_2^2}{f_1^2 - f_2^2} = \frac{1}{\gamma - 1} = 1.545 \quad ; \quad \gamma = \left(\frac{77}{60}\right)^2$$

a) Apply the Hatch filter to compute the DFree smoothed code

```
gawk 'BEGIN{Ts=100}{if (NR>Ts){n=Ts}else{n=NR};
       C1f=$11; L1f=$14+2*1.55*($14-$16);
       C1fs=C1f/n+(n-1)/n*(C1fs+(L1f-L1p));L1p=L1f;
       print $4,C1fs-L1f-21.3}' upc3.meas  > upc3.C1DFs100
```

b) Plot results and compare with the row C1 code:

```
graph.py -f upc3.C1 -s- --l "C1 Raw"
  -f upc3.C1s100 -s.- --cl r --l "C1 SF smoothed (100s)"
  -f upc3.C1DFs100 -s.- --cl g --l "C1 DFree smooth(100s)"
        --xn 35000 --xx 40000 --yn -5 --yx 5
        --xl "time (s)" --yl "meters"
```



LWP3: Iono. Divergence on Smoothing

4 . Generate the ionosphere-free combinations of code and carrier measurements to compute the Ionosphere Free (IFree) smoothed code:

$$C_{IFree} \equiv P_C = \frac{\gamma P_1 - P_2}{\gamma - 1} \quad ; \quad L_{IFree} \equiv L_C = \frac{\gamma L_1 - L_2}{\gamma - 1} \qquad \gamma = \left(\frac{77}{60}\right)^2$$

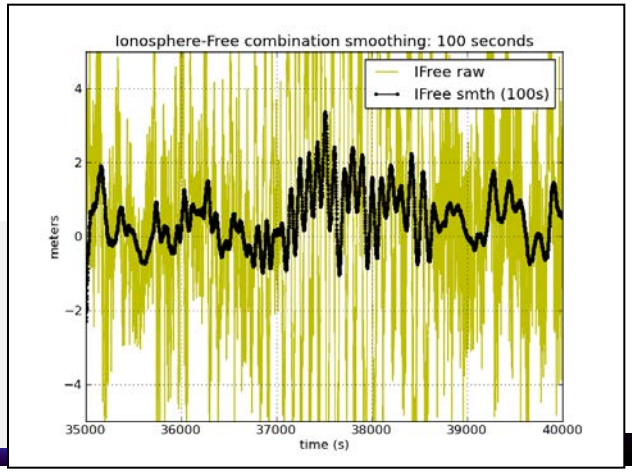
```
gawk 'BEGIN{g=(77/60)**2}{pc=(g*$13-$15)/(g-1); lc=(g*$14-$16)/(g-1);
                                        print  $4,pc-lc-3.5}' upc3.meas > upc3.PC
```

- Apply the Hatch filter to compute the IFree smoothed code

```
gawk 'BEGIN{g=(77/60)**2}{pc=(g*$13-$15)/(g-1);
     lc=(g*$14-$16)/(g-1); if (NR>100){n=100}else{n=NR};
               ps=1/n*pc+((n-1)/n*(ps+lc-lcp)); lcp=lc;
          print $4,ps-lc-3.5}' upc3.meas > upc3.PCs100
```

- Plot results and compare with the unsmoothed PC:

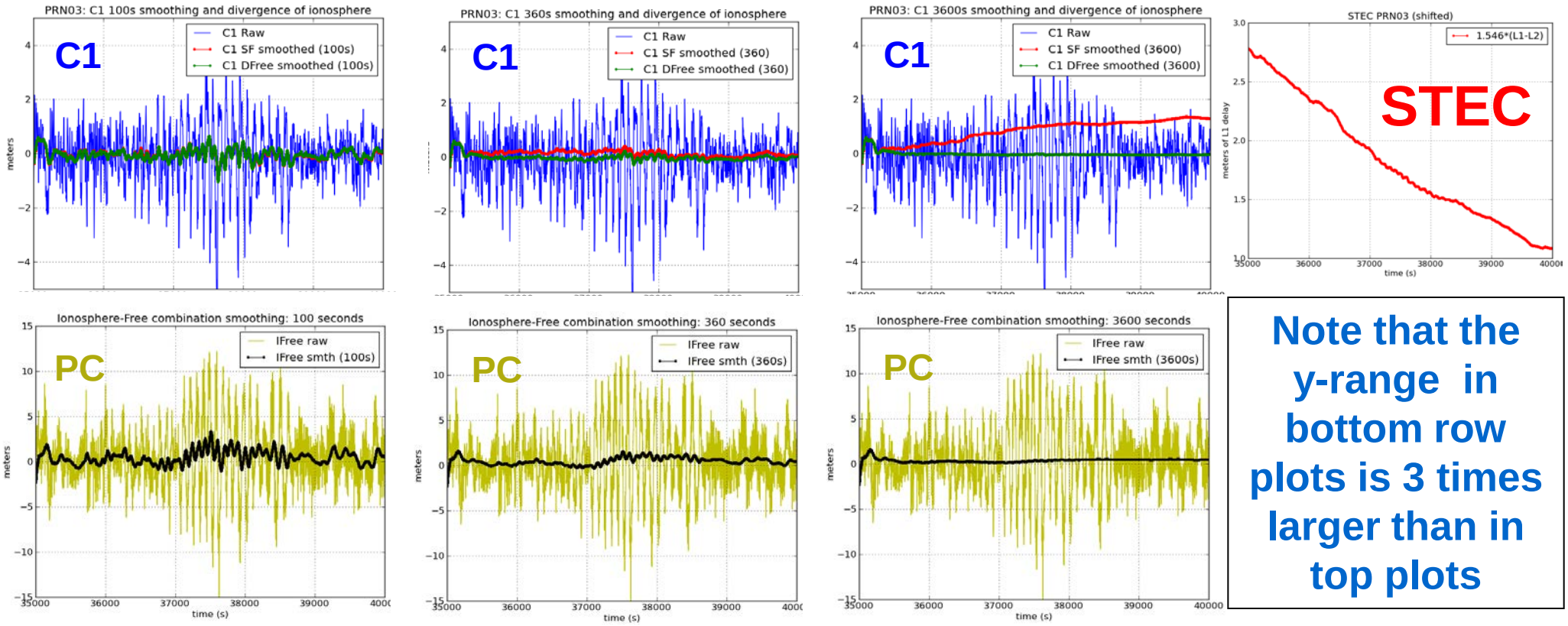
```
graph.py -f upc3.PC -s- --l "IFree raw"
         -f upc3.PCs100 -s.- --cl black --l "Ifree(100s)"
         --xn 35000 --xx 40000 --yn -5 --yx 5
         --xl "time (s)" --yl "meters"
```



LWP3: Iono. Divergence on Smoothing

5 . Repeat previous plots but using: *N=360*, *N=3600* and compare results. Plot also the ionospheric delay (from L1-L2) (see more details in [R-1]):

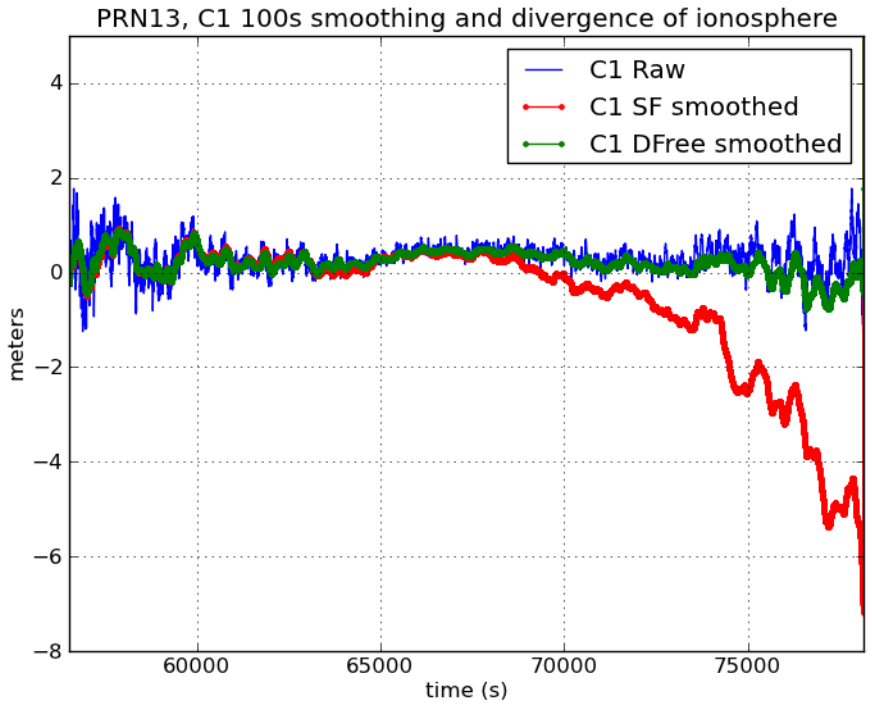
T=100s **T=360s** **T=3600s**

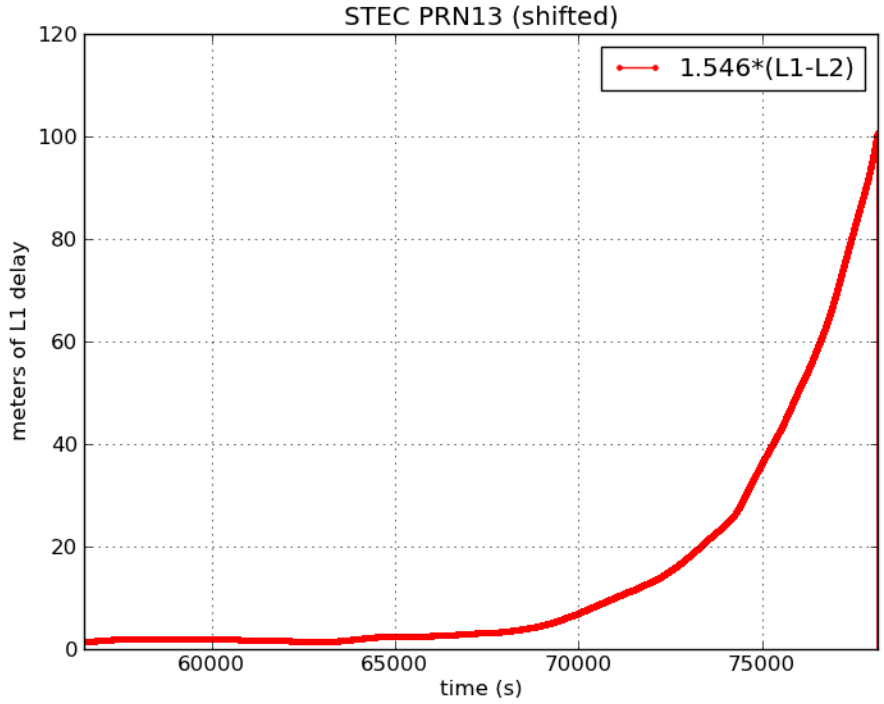


Note that the y-range in bottom row plots is 3 times larger than in top plots

LWP3: Iono. Divergence on Smoothing

Repeat the previous exercise using the RINEX file **`amc23030.03o_1Hz`** collected for the station `amc2` during the Halloween storm. Take *N=100* (i.e, filter smoothing time constant ***τ=100 sec***).

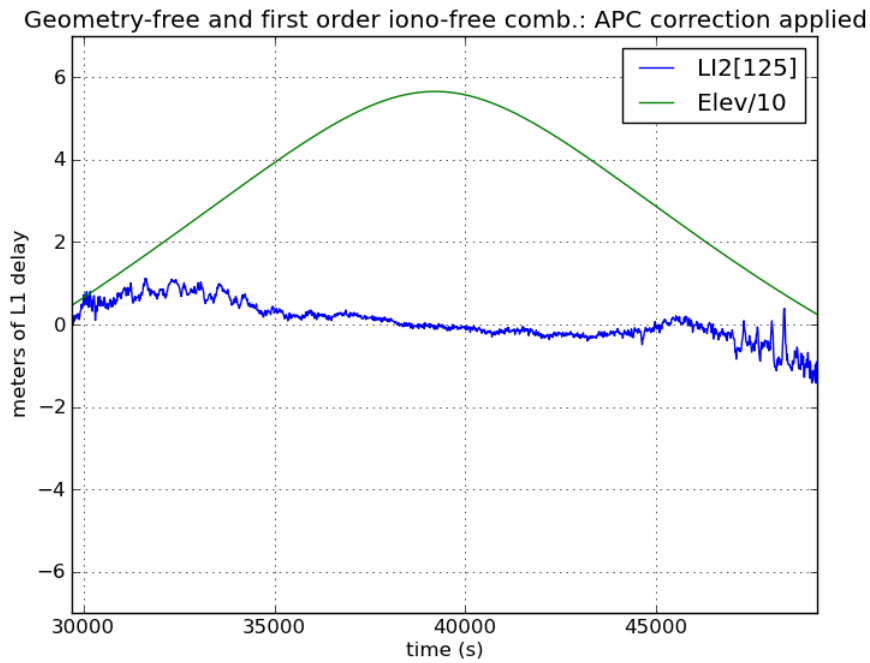




LWP4: Second order Ionospheric Effect

The aim of LWP4 is to build a combination of carriers measurements at three different frequencies to remove the geometry and the first order ionosphere effects.

Once this combination is obtained, its suitability to depict the second order ionospheric effects will be analyzed.



The assessment will be based on actual GPS measurements at frequencies L1, L2 and L5

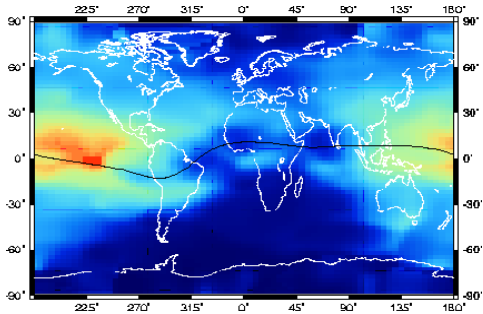
LWP4: Second order Ionospheric Effect

First order Ionospheric delay

As commented before, about the 99.9% of the ionospheric delay $I1$ depends on the inverse of squared frequency: where STEC is the number of electrons per area unit along ray path (STEC: Slant Total Electron Content).

$$I1 = \frac{40.3}{f^2} STEC$$

$$STEC = \int N_e ds$$



- Its effect on code and carrier is equal but with opposed sign: $I1_{carr} = -I1_{code}$

Second order Ionospheric delay

Previous expression comes from a simplification of the ionospheric delay derivation, where the dependence of the refraction index with the magnetic field $\boldsymbol{B}$ is neglected. If such dependence is taken into account, higher order terms appears (but, they represent less than 0.1% of total effect)

- The second order ionospheric term is given by: $I2_{code} = -\frac{7257c}{f^3} \int N_e B \cos\theta ds \quad ; \quad I2_{carr} = -\frac{1}{2} I2_{code}$
- In global geodetic computations, $I2$ mainly affects to the satellite clock estimates (cm level) and orbits (few mm), but the impact on receiver positions is smaller than1mm, (see [R-5] and [R-1]).

LWP4: Second order Ionospheric Effect

Second order Ionospheric delay combination

Question 1: Show that there is a unique linear combination of three carriers cancelling both geometry and (first order) ionospheric refraction. a) Apply results to GPS L1, L2 and L5 signals. b) Using file **`l5dt1260.09o`** depict such combination of carriers.

Hint:

Let $a_i L_i + a_j L_j + a_k L_k$ *be a linear combination of three carrier measurements at frequencies* f_i, f_j, f_k .

The coefficients a_i, a_j, a_k *, shall verify the conditions:*

$$\begin{cases} a_i + a_j + a_k = 0 & \leftarrow \text{geometry-free} \\ a_i + \beta_{ij}^2 a_j + \beta_{ik}^2 a_k = 0 & \leftarrow \text{1st-oder iono-free} \\ a_i + \beta_{ij}^3 a_j + \beta_{ik}^3 a_k = 1 & \leftarrow \text{2nd-order iono} \end{cases}$$

with

$$\beta_{ij} = f_i / f_j$$

Note:

The first equation cancels all non-frequency dependent effects (geometric range, clocks, troposphere…)

The second equation cancels all effects that depends of inverse squared frequency (1st-order: ionosphere and instrumental delays).

The last equation is to normalize the coefficients giving the combination in delay units at frequency f_i .

LWP4: Second order Ionospheric Effect

Answer to question 1a:

Show that there is a unique linear combination of three carriers cancelling both the geometry and the (first order) ionospheric refraction. Apply results to the L1, L2 and L5 signals.

Applying previous equations system to GPS signals $f_1 = 154\, f_0$, $f_2 = 120\, f_0$, $f_5 = 115\, f_0$.

$$\begin{cases} a_1 + a_2 + a_5 = 0 \\ a_1 + \beta_{12}^2 a_2 + \beta_{15}^2 a_5 = 0 \\ a_1 + \beta_{12}^3 a_j + \beta_{15}^3 a_5 = 1 \end{cases} \quad \textit{with} \quad \begin{matrix} \beta_{12} = 154/120 \\ \beta_{15} = 154/115 \end{matrix} \longrightarrow \quad \boxed{\begin{matrix} a_1 = 6.287 \\ a_2 = -34.084 \\ a_3 = 27.797 \end{matrix}}$$

Thence, the combination is: $\boxed{\mathrm{LI2} \equiv 6.287 L_1 - 34.084 L_2 + 27.797 L_5}$ (in delay units at f_1 frequency).

On the other hand, assuming the carriers L_i uncorrelated and with the same σ_L , the noise associated to this combination is given by: $\boxed{\sigma_{\mathrm{LI2}} = 44.4 \sigma_L}$

Note: As $I2_{code} = -\frac{1}{2} I2_{carr}$, the combination of codes is given by:

$$\boxed{\mathrm{PI2} \equiv -3.144 C_1 + 17.042 C_2 - 13.899 C_5 \,; \quad \sigma_{\mathrm{PI2}} = 22.2 \sigma_C}$$

LWP4: Second order Ionospheric Effect

Answer to question 1b:

Make a plot to depict the geometry-free and first-order ionosphere-free combination of GPS carrier phase measurements [L1,L2,L5].

Use files **`l5dt1260.09o`**, **`l5dt1260.09n`** [*] (and satellite PRN01).

1. **Using** the configuration file **`meas.cfg`**, READ the RINEX and generate the MEAS file with content:

```
[MEAS YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2C L2C C2P L2P C5X L5X ]
    1  2  3   4   5    6  7 8  9  10   11   12  13  14  15 16   17  18  19  20
```

```
gLAB_linux -input:cfg meas.cfg -input:obs l5dt1260.09o -input:nav l5dt1260.09n
                                                  -pre:dec 0| grep GPS > l5dt.meas
```

2. **From `l5dt9.meas` file, generate a file with the following content:**

```
[sec LI2  elev]
  1   2    3
```

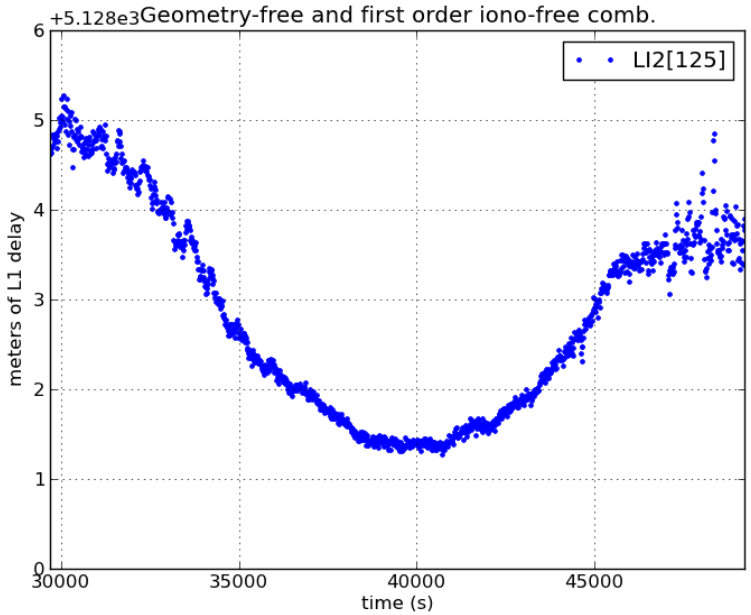
```
gawk '{if ($6==01) {print $4,6.287*$14-34.084*$18+27.797*$20,$7}}' l5dt.meas >
                                                                    LI2.dat
```

[*] Note, although the elevation is not needed for this exercise (and thence the broadcast orbit file **`l5dt1260.09n`**, it is computed because it will be useful for a further study).

LWP4: Second order Ionospheric Effect

3.- Plotting results:

```
graph.py -f LI2.dat -x1 -y2--l "LI2[125]"
         --xn 29700 --xx 49200  --yn 5128 --yx 5134
         --xl "time (s)" --yl "meters of L1 delay"
```



Discussion:

1. What is the order of magnitude of the second order ionospheric effect?
2. Is the pattern seen in the figure due to the 2nd order ionospheric effect or it is related to other phenomena?

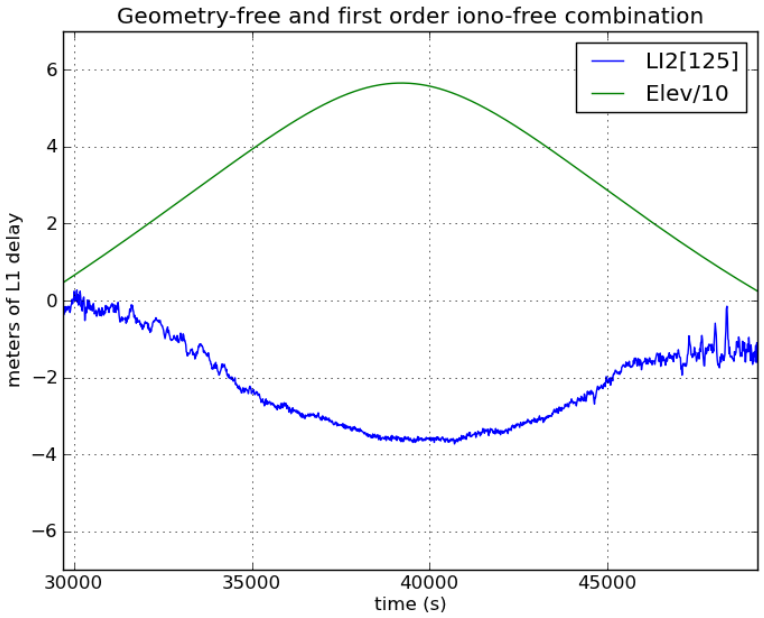
Hint:

Add the elevation in the previous plot and explore if the pattern could be related to the antenna phase centers of the different signals.

LWP4: Second order Ionospheric Effect

3.- Plotting results with the elevation added:

```
graph.py -f LI2.dat -x1 -y'($2-5133)' -s- --l "LI2[125]"
         -f LI2.dat -x1 -y'($3/10)' -s- --l "Elev/10" -s-
            --xn 29700 --xx 49200  --yn -7 --yx 7
            --xl "time (s)" --yl "meters of L1 delay"
```



Note:
The figure is shifted (by *5133m*) to align with the x-axis.
This bias is due to the carrier ambiguity (see HW1).

LWP4: Second order Ionospheric Effect

Answers to the previous discussion:

1. **What is the order of magnitude of the second order ionospheric effect?**
2. **Is the pattern seen in the figure due to the 2nd order ionospheric effect or it is related to other phenomena?**

The I2 effect on ground measurements is typically less than 2cm of L1 delay(see HW3 or [R-5]). Thence, the pattern must be related to another phenomena, as explained as follows:

- In the derivation of previous combination LI2, the antenna phase center (APC) correction for the GPS signals has not been taken into account. Indeed, as L1, L2 and L5 have different APCs, the geometric range for such signals is slightly different, producing an elevation dependent error if it is not modelled.
- In HW1 it is shown that, assuming only APC correction in the UP component, the APC effect can be removed from LI2 as:

$$\mathrm{LI2}+\left(a_i\Delta_{i_{UP}}+a_j\Delta_{j_{UP}}+a_k\Delta_{k_{UP}}\right)\sin\varepsilon$$

where a_i, a_j, a_k are the combination coefficients, $\Delta_{i_{UP}}, \Delta_{j_{UP}}, \Delta_{k_{UP}}$ are the antenna phase centres for the different signals and ε is the elevation of ray

LWP4: Second order Ionospheric Effect

Question 2: Using the following values for the APCs $\Delta_{1_{UP}} = 0.09,\ \Delta_{2_{UP}} = 0.12,\ \Delta_{5_{UP}} = 0.28$ (in meters, see HW1) plot the previous expression and discuss results.

Now the combination to plot is:

$$\text{LI2\_corr} \equiv 6.287(L_1 + 0.09\sin\varepsilon) - 34.084(L_2 + 0.12\sin\varepsilon) + 27.797(L_5 + 0.28\sin\varepsilon)$$

1.- Using previous file `l5dt.meas`, generate a file content:

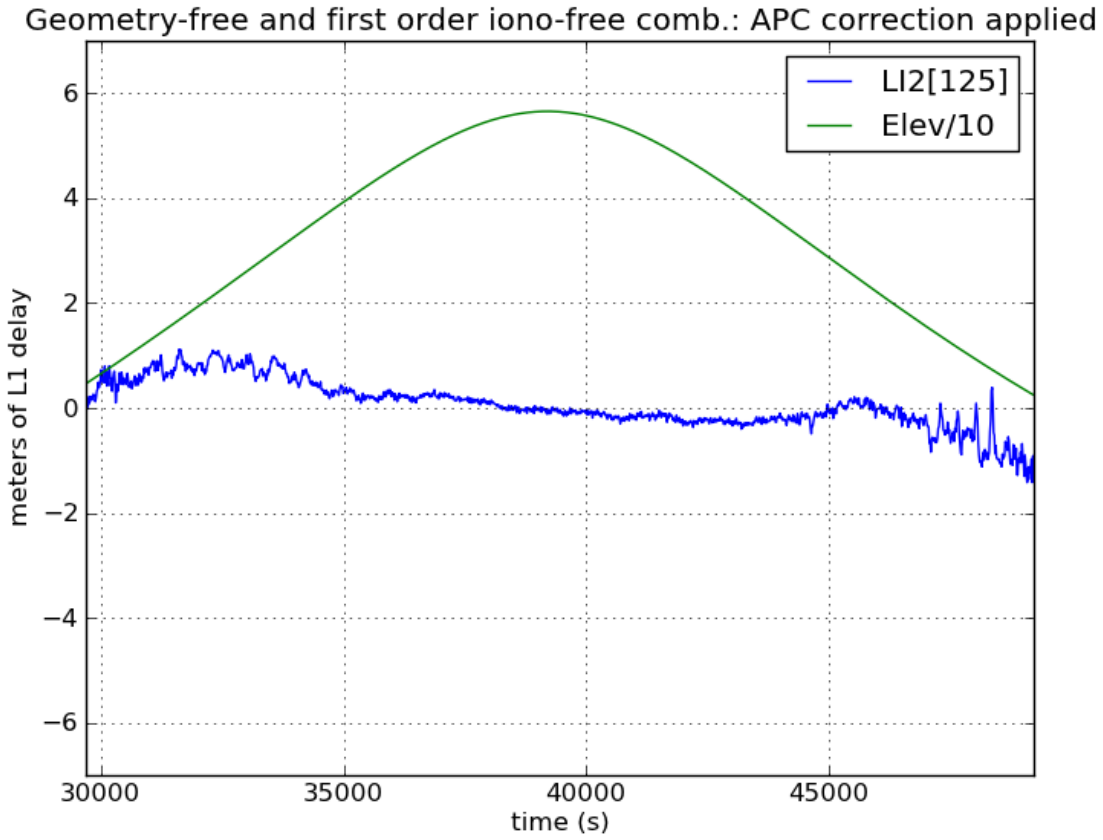
```
[sec LI2corr elev]
  1     2     3
```

```
gawk '{if ($6==01) {s=sin($7*3.14/180);
 print $4,6.287*($14+0.09*s)- 34.084*($18+0.12*s)+27.797*($20+0.28*s),$7}}'
                                                    l5dt.meas > LI2corr.dat
```

2.- Plot results:

```
raph.py -f LI2corr.dat -x1 -y'($2-5133)' -s- --l "LI2[125]"
        -f LI2.dat -x1 -y'($3/10)' --l "Elev/10" -s-
        --xn 29700 --xx 49200 --yn -7 --yx 7 --xl "time (s)" --yl “L1 meters"
```

LWP4: Second order Ionospheric Effect



Final questions:

1. Discuss if the second-order ionospheric effect can be depicted from GPS data.

   Hint:

   1. *The expected I2 effect on a ground receiver is less than 2cm in L1 delay (see HW3)*
   2. *The estimation noise of LI2 is* $\sigma_{\mathrm{LI2}} = 44.4\sigma_L$ *.Thence even in an ideal case without APC errors and no carrier multipath (take for instance* $\sigma_L \simeq 2mm$ *), the noise will be over the phenomena threshold.*

2.- The same question for Galileo data (see HW2).

OVERVIEW

- **Introduction**
- **The gLAB tool suite**
- **Examples of GNSS processing using gLAB**
- **Laboratory session organization**

LABORATORY Session

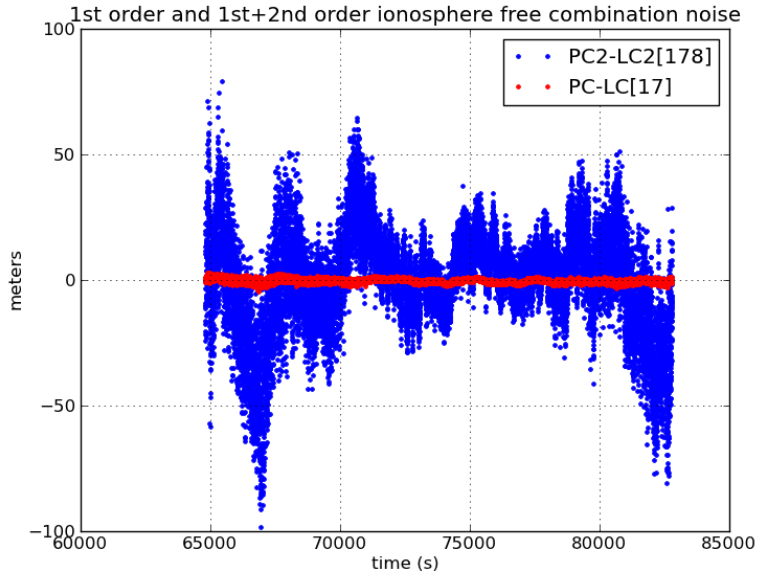
- **Starting up your laptop**
- **Basic:** Introductory lab exercises: Iono & Posit, SF, storm,TIDs
- **Medium:** Laboratory Work Projects: LWP1 to LWP4
- **Advanced:** Homework

Home Work

Aim

Different complementary questions (theoretical and experimental) related to the LW4 are asked in this homework section.

The aim is to analyze in depth the combinations of three frequency signals.



The assessment will be based in actual GPS measurements at frequencies L1, L2 and L5, as well as Galileo at E1, E5 and E5b frequencies

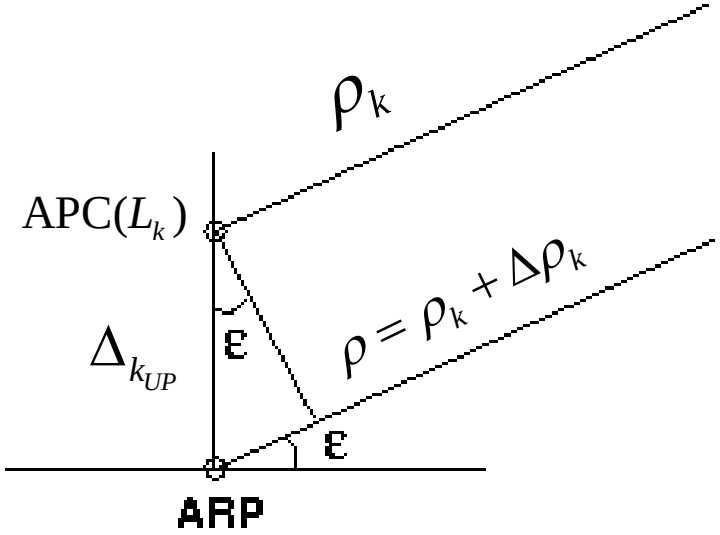
HW1: APC effect on the LI2 combination.

Question 1: Study the effect of the Antenna Phase Centre (APC) on the LI2 combination in order to analyze the elevation dependent pattern seen in previous of LWP2 and HW1 plots for the GPS signals (see [R-1]).

Answer :

GNSS signals at different frequencies (e.g., L1, L2, L5) have, in general, different APCs and they can produce an elevation dependent effect in the LI2 combination.

Indeed, referring the geometric range to a common reference (the Antenna Reference Point [ARP]) and assuming only APC in the UP component, it follows (see figure):



$$\rho = \rho_k + \Delta\rho_k \qquad \text{where:} \quad \Delta\rho_k = \Delta_{k_{UP}} \sin\varepsilon$$

Thence, the APC correction to apply to LI2 combination is given by:

$$\sum_k \alpha_k L_k + \underbrace{\sum_k \alpha_k \Delta_{k_{UP}} \sin\varepsilon}_{\text{APC correction term}} = bias$$

where the bias term is due to the carrier ambiguities.

Note: the satellite APC is not considered as the deviation angle from the direction pointing to the Earth centre is less than 14º.

HW1: APC effect on the LI2 combination.

Question 2: Knowing the L1 and L2 signals APCs, estimate the L5 APC.

a) The file `l5dt1260.09o` has been collected by a TRIMBLE NETR8 receiver with TRM59800.00 antenna. According the ANTEX file `igs05_1525.atx` the antenna phase centers of L1 and L2 are given by:

```
# TRM59800.00      NONE                    TYPE / SERIAL NO
#   G01                                    START OF FREQUENCY
#      0.37      0.86      90.02           NORTH / EAST / UP
#   G02                                    START OF FREQUENCY
#      0.09      0.01     119.89           NORTH / EAST / UP
```

Taking into account previous results, estimate the APC of L5 signal.

Note: Neglect the North/East components against the UP component.

According previous table ➔ $\Delta_{1_{UP}} = 0.09002m, \quad \Delta_{2_{UP}} = 0.11989m$

HW1: APC effect on the LI2 combination.

Answer to Question 2: (Knowing the L1 and L2 APCs, estimate the L5 APC.)

The APC of L5 signal, together with the carrier ambiguity (bias), can be estimated from carrier measurements along a continuous data arch (for the three carriers) as follows:

$$\sum_k \alpha_k \left(L_k + \Delta_{k_{UP}} \sin\varepsilon \right) = bias$$

$$\underbrace{\alpha_1 L_1(t) + \alpha_2 L_2(t) + \alpha_5 L_5(t) + (\alpha_1 \Delta_{1_{UP}} + \alpha_2 \Delta_{2_{UP}}) \sin\varepsilon(t)}_{y(t)} = bias - \left[\alpha_5 \sin\varepsilon(t)\right] \Delta_{5_{UP}}$$

$$\underbrace{\begin{bmatrix} y(t_1) \\ \vdots \\ y(t_n) \end{bmatrix}}_{\mathbf{y}} = \underbrace{\begin{bmatrix} 1 & -\alpha_5 \sin\varepsilon(t_1) \\ \vdots & \vdots \\ 1 & -\alpha_5 \sin\varepsilon(t_n) \end{bmatrix}}_{\mathbf{A}} \begin{bmatrix} bias \\ \Delta_{5_{UP}} \end{bmatrix} \quad \Rightarrow \quad \boxed{\begin{bmatrix} bias \\ \Delta_{5_{UP}} \end{bmatrix} = \left(\mathbf{A}^{\mathbf{T}}\mathbf{A}\right)^{-1}\mathbf{y}}$$

HW1: APC effect on the LI2 combination.

Numerical application to L1, L2 and L5 signals:

Applying the values $a_1 = 6.287, \quad a_2 = -34.084, \quad a_3 = 27.797, \quad \Delta_{1_{UP}} = 0.09002, \quad \Delta_{2_{UP}} = 0.11989$ to previous equation, it follows:

$$\underbrace{6.287L_1(t) - 34.084L_2(t) + 27.797L_5(t) - 43.505\sin\varepsilon(t)}_{y(t)} = bias - \left[27.797\sin\varepsilon(t)\right]\Delta_{5_{UP}}$$

$$\underbrace{\begin{bmatrix} y(t_1) \\ \vdots \\ y(t_n) \end{bmatrix}}_{\mathbf{y}} = \underbrace{\begin{bmatrix} 1 & -27.797\sin\varepsilon(t_1) \\ \vdots & \vdots \\ 1 & -27.797\sin\varepsilon(t_n) \end{bmatrix}}_{\mathbf{A}} \begin{bmatrix} bias \\ \Delta_{5_{UP}} \end{bmatrix} \rightarrow \begin{bmatrix} bias \\ \Delta_{5_{UP}} \end{bmatrix} = \left(\mathbf{A}^{\mathrm{T}}\mathbf{A}\right)^{-1}\mathbf{y} \Rightarrow$$

$$\Delta_{5_{UP}} = 0.283m$$
$$bias = 5133.1m$$

Using the L1, L2, L5 values of file l5dt1260.09o in the time interval 30000<t <49000 sec. (see details in the notepad).

HW1: APC effect on the LI2 combination.

b) Plot the LI2 combination corrected by the antenna phase center values: $\Delta_{1_{UP}} = 0.09,\ \Delta_{2_{UP}} = 0.12,\ \Delta_{5_{UP}} = 0.28$ (in meters)

Now the combination to plot is:

$$\text{LI2\_corr} \equiv 6.287(L_1 + 0.09\sin\varepsilon) - 34.084(L_2 + 0.12\sin\varepsilon) + 27.797(L_5 + 0.28\sin\varepsilon)$$

1.- Using previous file `l5dt.meas`, generate a file content:

```
[sec LI2corr elev]
  1     2      3
```

```
gawk '{if ($6==01) {s=sin($7*3.14/180); print $4,6.287*($14+0.09*s)-
     34.084*($18+0.12*s)+27.797*($20+0.28*s)-5133,$7}}' l5dt.meas > LI2c.dat
```

2.- Plot results:

```
graph.py -f LI2c.dat -x1 -y2 -s- --l "LI2[125]"
         -f LI2c.dat -x1 -y'($3/10)' -s- --l "Elev/10"
        --xn 29700 --xx 49200 --yn -7 --yx 7 --xl "time (s)" --yl "L1 meters"
```

HW1: APC effect on the LI2 combination.

HW2: Combinations of three-frequency measur.

This HP2 is an extension of previous LWP2 and it is devoted to analysing the three different combinations of three frequency signals (see [R-1]):

1. The first and second order ionosphere-free combination (LC2, PC2).
2. The geometry-free and second-order ionosphere-free combination (LI1, PI1).
3. The geometry-free and first-order ionosphere-free combination (LI2, PI2).

The target is to analyze the suitability (or not) of such combinations to provide:

- [LC2, PC2]: A measurement free from 1st and 2nd order ionospheric effects.
- [LI1, PI1]: A direct measurement of the 1st order ionosphere (free from 2nd order).
- [LI2, PI2]: A direct measurement of the 2nd order ionospheric effect.

The last case, i.e. LI2, PI2, has been already studied in the previous LWP2 for the GPS signals L1,L2,L5. This study will be extended here to the Galileo signals.

HW2: Combinations of three-frequency measur.

Preliminar: Combinations of three-frequency signals derivation:

Let L_i, L_j, L_k the carrier measurements at frequencies f_i, f_j, f_k , and $I1_i, I2_i$ the first and second order ionospheric effects at the frequency f_i (including instrumental delay terms). Show the following expressions, where ρ is the geometrical range plus all other non dispersive terms and the carrier ambiguity:

$$\begin{cases} L_i = \rho - I1_i + I2_i \\ L_j = \rho - \gamma_{ij} I1_i + \gamma_{ij}^{3/2} I2_i \\ L_k = \rho - \gamma_{ik} I1_i + \gamma_{ij}^{3/2} I2_i \end{cases} \qquad \text{with} \quad \gamma_{ij} = \left(f_i / f_j \right)^2$$

Consider the GPS carriers (L1, L2, L5). Show that

$$\begin{cases} \mathrm{LC2} = 7.08 L_1 - 26.130 L_2 + 20.050 L_5 \quad ; \quad \sigma_{\mathrm{LC2}} = 33.7 \sigma_L \\ \mathrm{LI1} = 12.368 L_1 - 60.215 L_2 + 47.847 L_5 \quad ; \quad \sigma_{\mathrm{LI1}} = 77.9 \sigma_L \\ \mathrm{LI2} = 6.287 L_1 - 34.084 L_2 + 27.797 L_5 \quad ; \quad \sigma_{\mathrm{LI2}} = 44.4 \sigma_L \end{cases}$$

Note:

$f_1 = 154\, f_0$, $f_2 = 120\, f_0$, $f_5 = 115\, f_0$.

being $\mathrm{LC2} \leftrightarrow \rho$; $\mathrm{LI1} \leftrightarrow I1_i$; $\mathrm{LI2} \leftrightarrow I2_i$. The carriers L_i are assumed uncorrelated and with the same σ_L

HW2: Combinations of three-frequency measur.

Note: The previous expressions correspond to:

- $[\rho]: \mathrm{LC2}$: *First order and Second order Ionosphere Free combination.*
- $[I1_i]: \mathrm{LI1}$: *Geometry-free and Second order Ionosphere Free combination.*
- $[I2_i]: \mathrm{LI2}$: *Geometry-free and First order Ionosphere Free combination.*

Hint:

Let $\mathbf{y} = \mathbf{A}\,\mathbf{x}$ *the previous equations system, where* $\mathbf{y} = [L_i, L_j, L_k]^T$, $\mathbf{x} = [\rho, I1_i, I2_i]^T$ *and* $\mathbf{A}$ *is the associated matrix, evaluated at the given frequencies. Thence, the coefficients of* $[\mathrm{LC2}, \mathrm{LI1}, \mathrm{LI2}]$ *are given by* $\mathbf{A}^{-1}$. *The sigmas are the square-root of diagonal elements of matrix* $(\mathbf{A}^T\mathbf{A})^{-1}$.

The same question for GPS codes (C1, C2, C5). Show that:

$$\begin{cases} C_1 = \rho - I1_1 - 2\,I2_1 \\ C_2 = \rho - \gamma_{12} I1_1 - 2\,\gamma_{12}^{3/2} I2_1 \\ C_5 = \rho - \gamma_{15} I1_1 - 2\,\gamma_{15}^{3/2} I2_1 \end{cases} \Longrightarrow \begin{cases} \mathrm{PC2} = 7.081C_1 - 26.130C_2 + 20.050C_5 \quad ; \quad \sigma_{\mathrm{PC2}} = 33.7\sigma_C \\ \mathrm{PI1} = -12.368C_1 + 60.215C_2 - 47.847C_5 \quad ; \quad \sigma_{\mathrm{PI1}} = 77.9\sigma_C \\ \mathrm{PI2} = -3.144C_1 + 17.042C_2 - 13.899C_5 \quad ; \quad \sigma_{\mathrm{PI2}} = 22.2\sigma_C \end{cases}$$

HW2: Combinations of three-frequency measur.

The same question for Galileo carriers (E1, E7, E8) and codes (C1, C7, C8). Show that:

$$\begin{cases} L_1 = \rho - I1_1 + I2_1 \\ L_7 = \rho - \gamma_{17} I1_1 + \gamma_{17}{}^{3/2} I2_1 \\ L_8 = \rho - \gamma_{18} I1_1 + \gamma_{18}{}^{3/2} I2_1 \end{cases} \Rightarrow \begin{cases} \mathrm{LC2} = 6.694 L_1 - 78.318 L_2 + 72.354 L_5 \quad ; \quad \sigma_{\mathrm{LC2}} = 106.8 \sigma_L \\ \mathrm{LI1} = 12.110 L_1 - 182.385 L_2 + 170.275 L_5 \quad ; \quad \sigma_{\mathrm{LI1}} = 249.8 \sigma_L \\ \mathrm{LI2} = 6.146 L_1 - 104.067 L_2 + 97.921 L_5 \quad ; \quad \sigma_{\mathrm{LI2}} = 143.0 \sigma_L \end{cases}$$

$$\begin{cases} C_1 = \rho - I1_1 - 2\, I2_1 \\ C_7 = \rho - \gamma_{17} I1_1 - 2\, \gamma_{17}{}^{3/2} I2_1 \\ C_8 = \rho - \gamma_{18} I1_1 - 2\, \gamma_{18}{}^{3/2} I2_1 \end{cases} \Rightarrow \begin{cases} \mathrm{PC2} = 6.964 C_1 - 78.318 C_7 + 72.354 C_8 \quad ; \quad \sigma_{\mathrm{PC2}} = 106.8 \sigma_C \\ \mathrm{PI1} = -12.110 C_1 + 182.385 C_7 - 170.275 C_8 \quad ; \quad \sigma_{\mathrm{PI1}} = 249.8 \sigma_C \\ \mathrm{PI2} = -3.073 C_1 + 52.033 C_7 - 48.960 C_8 \quad ; \quad \sigma_{\mathrm{PI2}} = 71.5 \sigma_C \end{cases}$$

Note:

$$f_1 \equiv f_{E1} = 154\, f_0\,, \quad f_7 \equiv f_{E5b} = 118\, f_0\,, \quad f_8 \equiv f_{E5} = 116.5\, f_0\,.$$

HW2: Combinations of three-frequency measur.

A) First order and Second order Iono-Free combination analysis

Questions: analyse the suitability of the combinations PC2 and LC2, obtained in the previous exercises, to navigate:

1. Calculate the theoretical noise of the (first order)-ionosphere-free combinations PC and LC and compare with the noise of first-order and second-order ionosphere- free combinations (LC2 and PC2) found in the previous exercise. Consider the Galileo signals [E1,E7] and [E1,E7,E8]. Which combinations are more suitable to navigate, the PC/LC or PC2/LC2?

2. Using files gien327sw.09o and orb15591.sp3, make a plot to compare the code noise of the first-order-ionosphere free combination of Galileo signals [E1,E7] and the first-order and second-order iono-free combination of signals [E1,E7,E8].

3. The same questions using files **`l5dt1260.09o, l5dt1260.09n`** for the GPS signals L1, L2, L5.

HW2: Combinations of three-frequency measur.

Answer to question A.1:

Calculate the theoretical noise of the (first-order) ionosphere-free combinations PC and LC and compare with the noise of first-order and second-order ionosphere- free combinations (LC2 and PC2)?

Assuming uncorrelated and with the same σ_P or σ_L :

$$PC_{[ij]} = \frac{\gamma_{ij} Pi - Pj}{\gamma_{ij} - 1} \quad \Rightarrow \quad \sigma_{PC[ij]} = \frac{\sqrt{\gamma_{ij}^2 + 1}}{\gamma_{ij} - 1}\sigma_P$$ .Idem : $\gamma_{ij} = \left(f_i / f_j \right)^2$

$$LC_{[ij]} = \frac{\gamma_{ij} Li - Lj}{\gamma_{ij} - 1} \quad \Rightarrow \quad \sigma_{LC[ij]} = \frac{\sqrt{\gamma_{ij}^2 + 1}}{\gamma_{ij} - 1}\sigma_L$$

Thence, for the Galileo signals [C1,C7] and [C1,C7,C8], it follows:

$$\sigma_{PC[17]} = 2.81\sigma_P \qquad \sigma_{\mathrm{PC2[178]}} = 106.8\sigma_C$$

$$\sigma_{LC[17]} = 2.81\sigma_L \qquad \sigma_{\mathrm{LC2[178]}} = 106.8\sigma_L$$

$$\gamma_{17} = \left(f_1 / f_7 \right)^2 = \left(154/118 \right)^2 = 1.703$$

Results show that the LC2 and PC2 are two orders of magnitude noisier than the original measurements. Thus, they are not suitable to navigate.

HW2: Combinations of three-frequency measur.

Answer to question A.2:

Make a plot to compare the code noise of the first-order ionosphere-free combination of Galileo signals [E1,E7] and the first-order and second-order ionosphere-free combination of Galileo signals [E1,E7,E8].

1. **Using the configuration file `meas.cfg`, READ the RINEX and generate the MEAS message with content:**

```
[MEAS YY Doy sec GAL PRN el Az N. list C1B L1B C1C L1C C7Q L7Q C8Q L8Q]
     1  2  3   4   5    6  7 8  9  10   11   12  13  14  15 16   17  18
```

Execute:

```
gLAB_linux -input:cfg meas.cfg -input:obs gien327sw.09o -input:sp3 orb15591.sp3> gien.meas
```

2. **From `gien327.09.meas` file, generate a file with the following content: (select the Galileo satellite PRN16, as well):**

```
[sec PC-LC PC2-LC2]
  1    2       3
```

```
gawk '{if ($5=="GAL" && $6==16){print $4,$11-1.42*($15-$11)-($12+1.42*($12-$16)),
              6.96*($11-$12)-78.32*($15-$16)+72.35*($17-$18)}}' gien.meas > gienPc2Lc2.dat
```

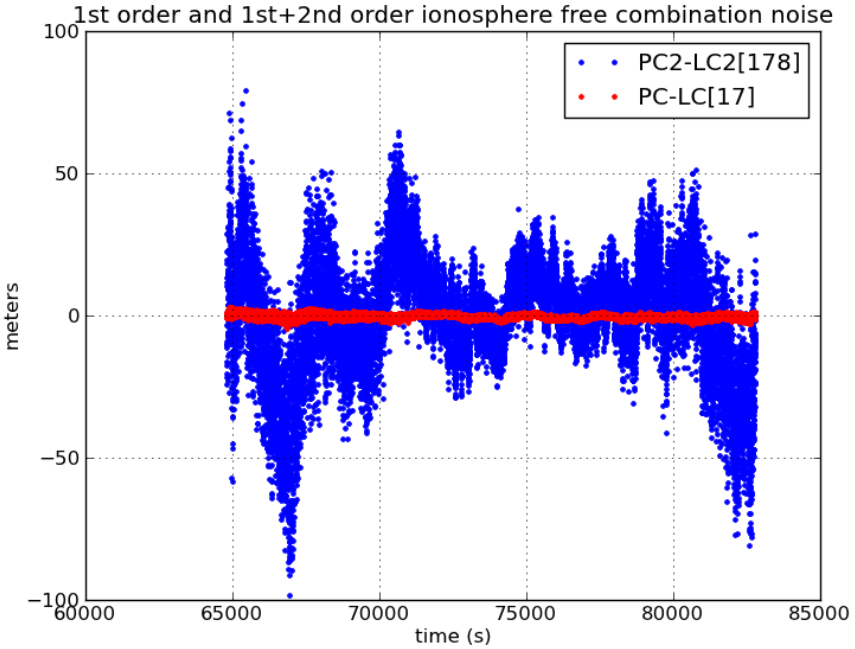
Note: The following expressions have been used to compute PC and LC

$$PC_{[ij]} = \frac{\gamma_{ij} Pi - Pj}{\gamma_{ij} - 1} = P_i - \frac{1}{\gamma_{ij} - 1}\left(P_j - P_i\right) \;\Rightarrow\; PC_{[17]} = P_1 - 1.42\left(P_7 - P_1\right) \quad ; \quad LC_{[ij]} = \frac{\gamma_{ij} Li - Lj}{\gamma_{ij} - 1} = P_i + \frac{1}{\gamma_{ij} - 1}\left(L_i - L_j\right) \;\Rightarrow\; LC_{[17]} = L_1 + 1.42\left(L_1 - L_7\right)$$

HW2: Combinations of three-frequency measur.

3.- Plotting results:

```
graph.py -f gienPc2Lc2.dat  -x1 -y3 --l "PC2-LC2[178]"
         -f gienPc2Lc2.dat  -x1 -y2 --l "PC-LC[17]"
         --cl r --yn -100 --yx 100 --xl "time (s)" --yl "meters"
```



As expected from the theoretical results, the measurement noise and mutipath are strongly amplified in the PC2 combination. Thence, it makes no sense to remove the second-order ionospheric effect (which is at the level of few centimetres) using this noisier combination.

Note:

The theoretical noise values found are:

$$\sigma_{PC[17]} = 2.81\sigma_C \; ; \sigma_{PC2[178]} = 106.8\sigma_C$$

HW2: Combinations of three-frequency measur.

Answer to Question A.3:

Repeat the previous exercise, for the GPS signals L1, L2, L5, using the files `l5dt1260.09o, l5dt1260.09n` (and satellite PRN01).

Resolution:

1. Using the configuration file `meas.cfg`, READ the RINEX and generate the MEAS file with content:

```
[MEAS YY Doy sec GPS PRN el Az N. list C1C L1C C1P L1P C2C L2C C2P L2P C5X L5X ]
    1  2  3   4   5    6  7 8  9  10   11   12  13  14  15 16   17  18  19  20
```

```
gLAB_linux -input:cfg meas.cfg -input:obs l5dt1260.09o -input:nav l5dt1260.09n
                                                    -pre:dec 0| grep GPS > l5dt.meas
```

2. From `l5dt126.09.meas` file, generate a file with the following content:

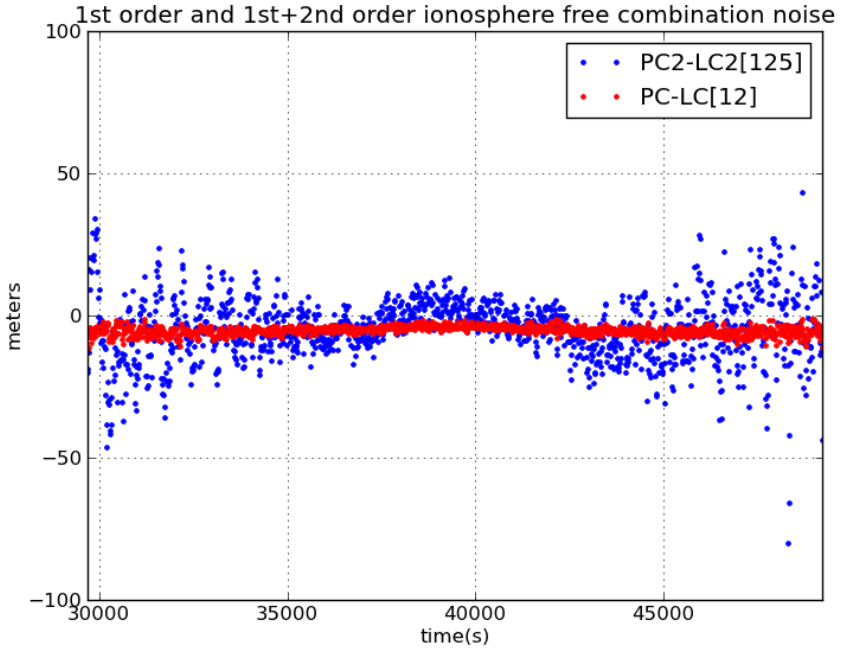
```
[sec PC-LC  PC2-LC2]
  1    2       3
```

```
gawk '{if ($6==01) {print $4,$13-1.55*($17-$13)-($14+1.55*($14-$18)),7.08*($13-$14)-
                        26.13*($17-$18)+20.05*($19-$20)}}' l5dt.meas > l5dtPc2Lc2.dat
```

HW2: Combinations of three-frequency measur.

3.- Plotting results:

```
graph.py -f l5dtPc2Lc2.dat -x1 -y'($3+5140)' --l "PC2-LC2[125]"
         -f l5dtPc2Lc2.dat -x1 -y2 --l "PC-LC[12] " --cl r
         --xn 29700 --xx 49200 --yn -100 --yx 100 --xl "time(s)" --yl "m"
```



Although the noise is lower than in previous case with the Galileo C1, C7 and C8 signals, it does not make sense to use the PC2 combination to navigate.

Note:

The theoretical noise values found are:

$$\sigma_{PC[12]} = 2.98\sigma_C \; ; \sigma_{PC2[125]} = 33.7\sigma_C$$

HW2: Combinations of three-frequency measur.

B) Geometry-free & Second-order Iono-Free combination analysis

Questions: analyse the suitability of the combinations PI1 and LI1, obtained in the previous exercises, to estimate the STEC:

1. Calculate the theoretical noise of the geometry-free combinations PI=P2-P1 and LI=L1-L2 and compare with the noise PI1 and LI1 combinations found in the previous exercise. Consider the Galileo signals [E1,E7] and [E1,E7,E8]. Which combinations are more suitable to navigate, the PI/LI or PI1/LI1?

2. Using files gien327sw.09o and orb15591.sp3, make a plot to compare the code noise of the geometry-free combination of Galileo signals [E1,E7] and the geometry-free and first-order ionosphere-free combination of signals [E1,E7,E8].

3. The same questions using files **`l5dt1260.09o, l5dt1260.09n`** for the GPS signals L1, L2, L5.

HW2: Combinations of three-frequency measur.

Answer to questions:

Question B.1: Measurement noise:

$$PI_{[ij]} = P_j - P_i \quad \Rightarrow \quad \sigma_{PI[ij]} = \sqrt{2}\sigma_P$$
$$LI_{[ij]} = P_i - L_j \quad \Rightarrow \quad \sigma_{LI[ij]} = \sqrt{2}\sigma_L$$

From previous results, seen at the beginning of this exercise.

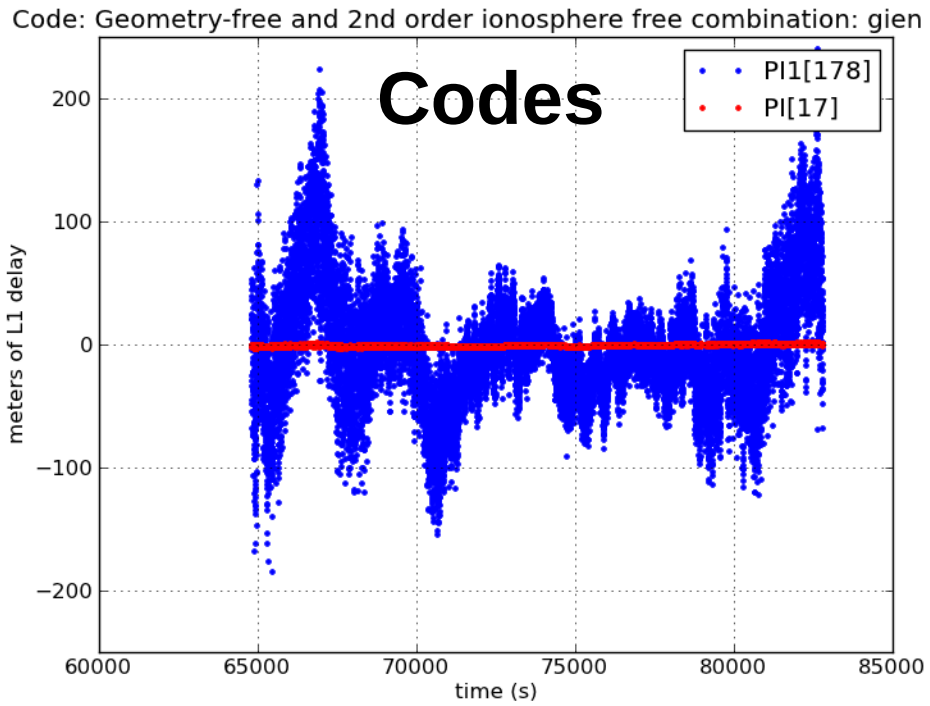
GAL: E1, E7, E8	GPS: L1, L2, L5
$\sigma_{PI_{[17]}} = \sqrt{2}\sigma_C$	$\sigma_{PI_{[12]}} = \sqrt{2}\sigma_C$
$\sigma_{LI_{[17]}} = \sqrt{2}\sigma_L$	$\sigma_{LI_{[12]}} = \sqrt{2}\sigma_L$
$\sigma_{\mathrm{PI1}_{[178]}} = 249.8\sigma_C$	$\sigma_{\mathrm{PI1}_{[125]}} = 77.9\sigma_C$
$\sigma_{\mathrm{LI1}_{[178]}} = 249.8\sigma_L$	$\sigma_{\mathrm{LI1}_{[125]}} = 77.9\sigma_L$

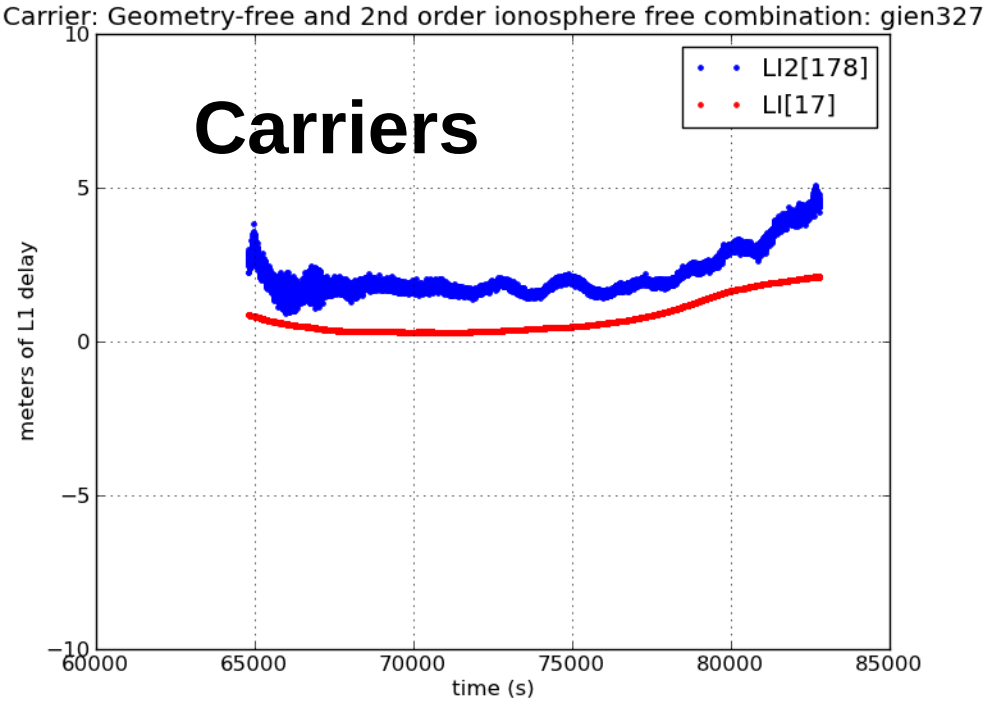
Thence, the measurement noise is strongly amplified in these combinations as in the previous case.

HW2: Combinations of three-frequency measur.

Question B.2: LI1, PI1 Plots: Following a similar procedure as in previous cases (see detailed instructions in the notepad):

Galileo: E1, E7, E8 signals

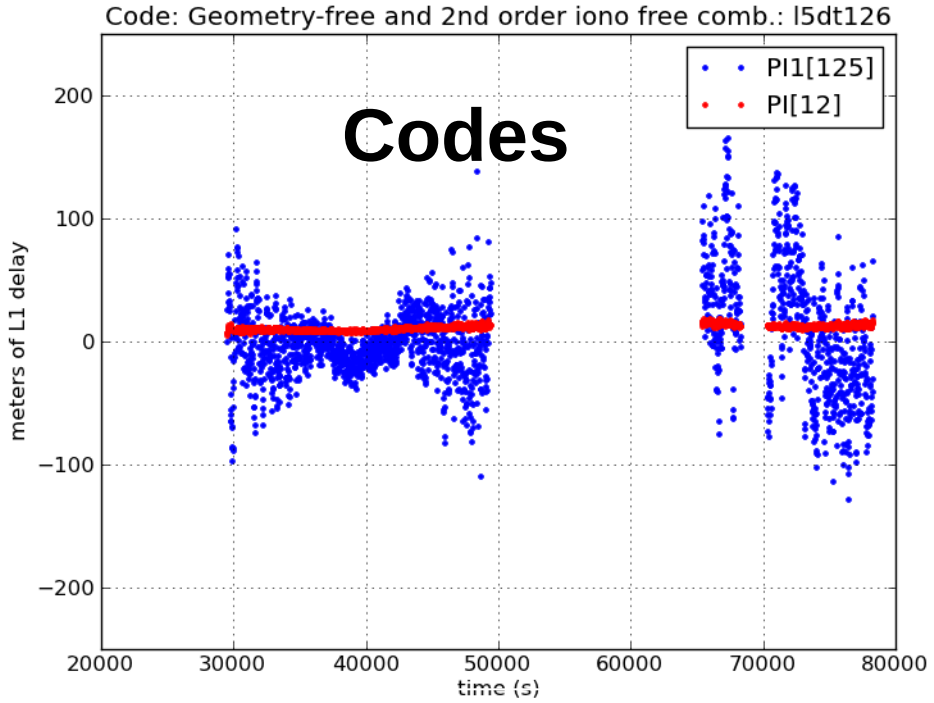


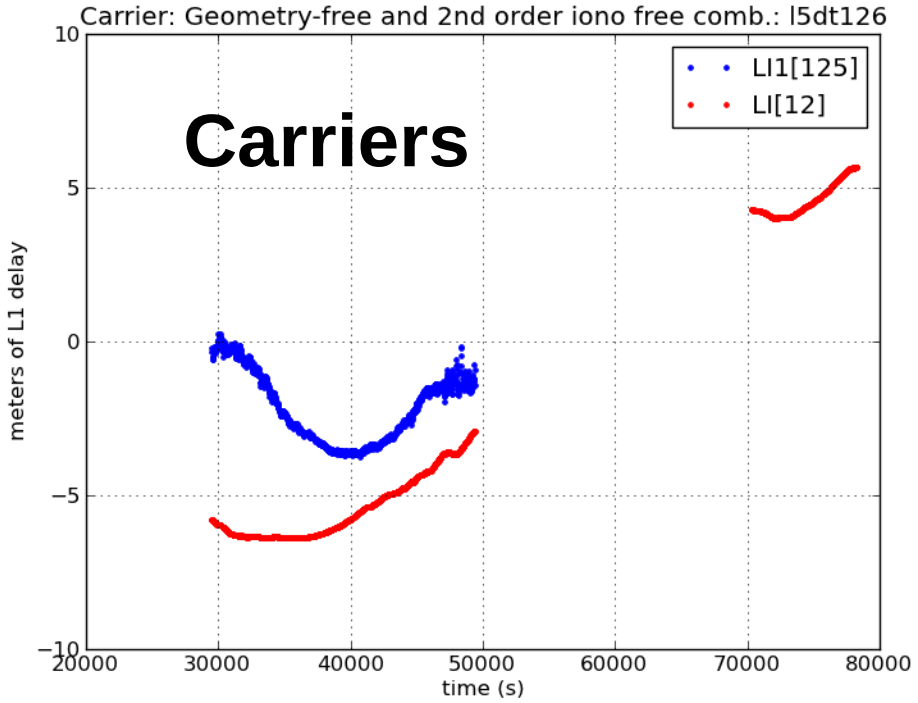


HW2: Combinations of three-frequency measur.

Question B.3: LI1, PI1 Plots: Following a similar procedure as in previous cases (see detailed instructions in the notepad): :

GPS: L1, L2, L5 signals





Why does this pattern appear in LI1/PI1? (see exercise HW1)

HW2: Combinations of three-frequency measur.

C) Geometry-Free & First-order Iono-Free combination analysis

Questions: analyse the suitability of the combinations PI2 and LI2, obtained in the previous exercises, to estimate the second-order ionosphere effect.

1. Make a plot to show the "geometry-free and first-order ionosphere-free combination (LI2) of Galileo carrier phase measurements [E1,E7,E8]. Use the files gien327sw.09o and orb15591.sp3 (and satellite PRN16). Discuss the results taking into account the theoretical noise figures found at the beginning of this exercise.

2. The same question for GPS carrier phase measurements [L1,L2,L5]. Use the files l5dt1260.09o, l5dt1260.09n (and satellite PRN01).

3. Discuss if the second-order ionospheric effect can be depicted from Galileo or GPS data.

HW2: Combinations of three-frequency measur.

Answer to questions:

Question C.1: Measurement noise:

From previous results, seen at the beginning of this exercise.

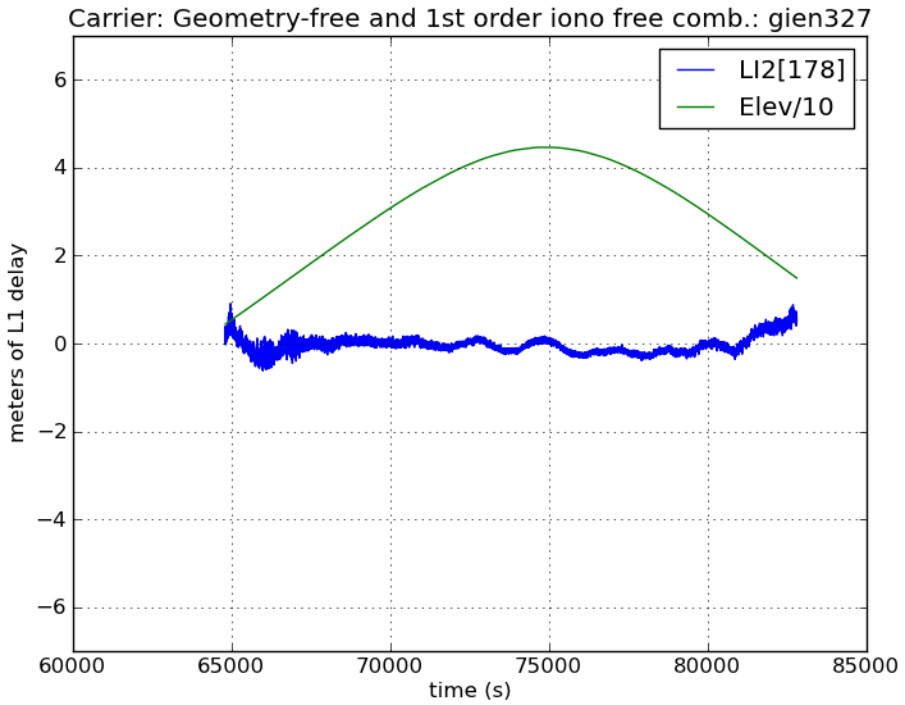
GAL: E1, E7, E8	GPS: L1, L2, L5
$\sigma_{\mathrm{PI2}_{[178]}} = 71.5\sigma_C$	$\sigma_{\mathrm{PI2}_{[125]}} = 22.2\sigma_C$
$\sigma_{\mathrm{LI2}_{[178]}} = 143.0\sigma_L$	$\sigma_{\mathrm{LI2}_{[125]}} = 44.4\sigma_L$

Thence, the measurement noise is strongly amplified in these combinations as in the previous case.

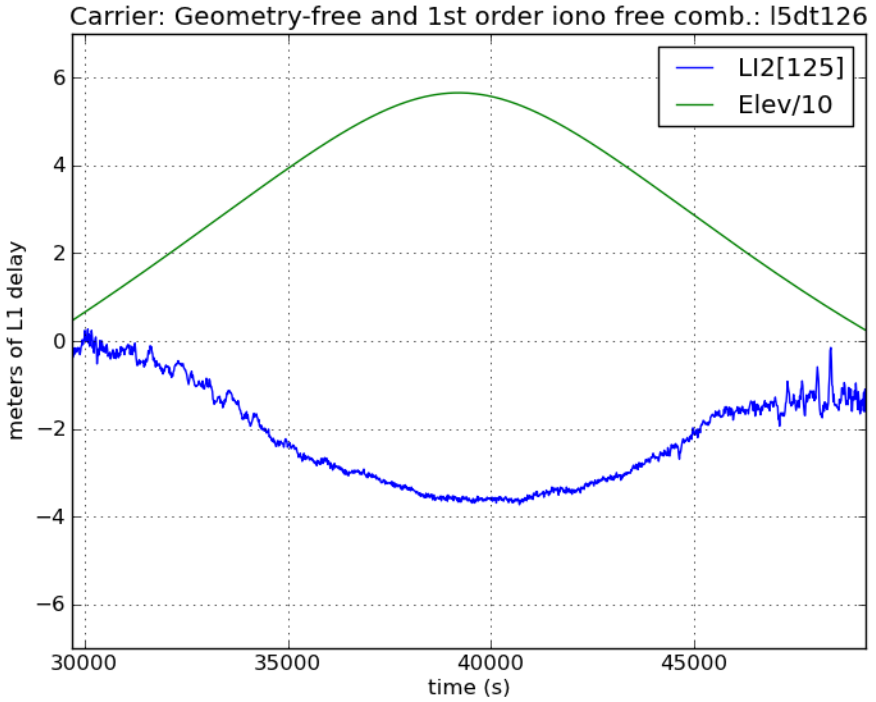
HW2: Combinations of three-frequency measur.

Questions C.2 and C3 : LI2 Plots: Following a similar procedure as in previous cases (see detailed instructions in the notepad):

Galileo: E1, E7, E8 signals



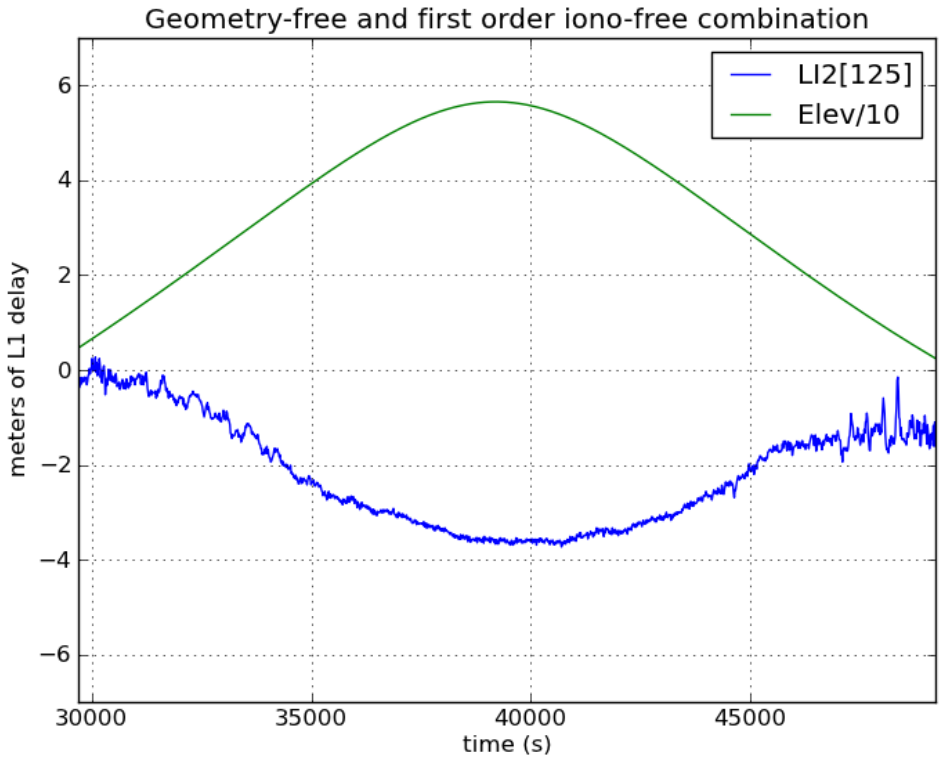
GPS: L1, L2, L5 signals



HW2: Combinations of three-frequency measur.

Comment 1:

In previous plot of GPS LI2 combination a clear pattern of about 2m appears (see this plot generation in LWP2).



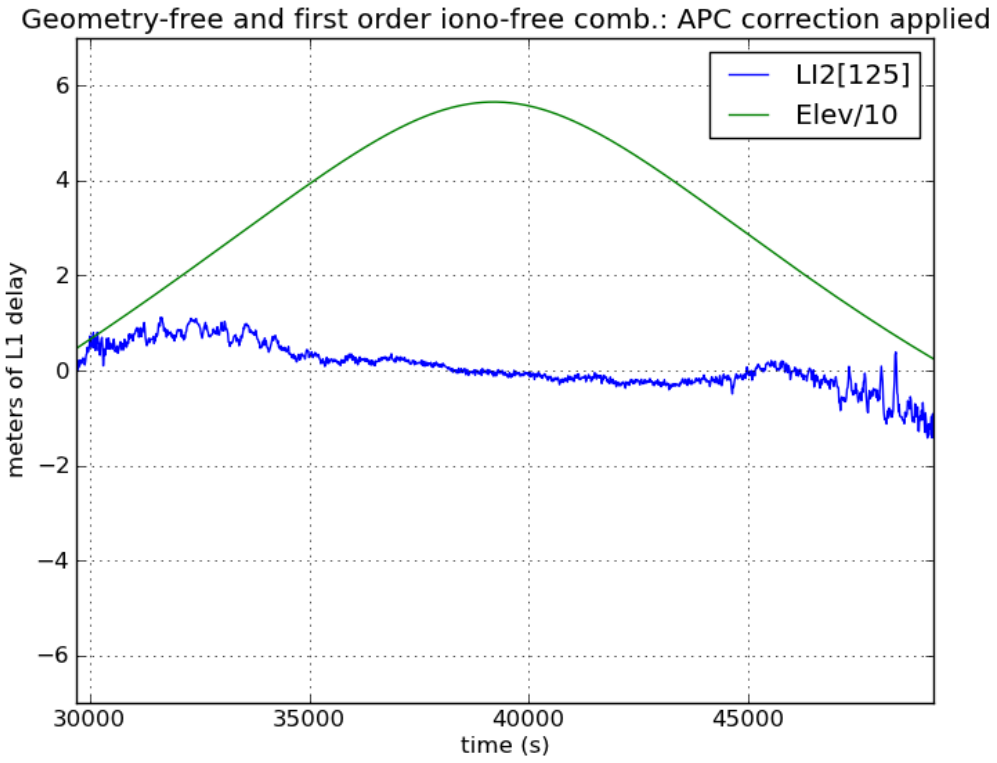
This pattern is an elevation dependent effect due to the different Antenna Phase Centres (APC) of the L1, L2, L5 signals.

The study of this effect was done in the previous Home Work exercise (HW1).

HW2: Combinations of three-frequency measur.

Comment 2:

After removing the error due to the APCs, the following plot is found (see this plot generation in exercise LWP2).



Nevertheless, the noise in the combination (in both cases, GPS and Galileo) is over the expected value for the 2nd order ionospheric effect (which is less than 2cm, see HW3 or [R-5]).

HW3: Theoretical exercises on 2nd order iono

Question 1:

Show that the second-order ionospheric delay on the L1 carrier produced by *10 TECU* of STEC is less than *2 millimetres*. Which values would reach I2 in the Halloween Ionospheric Storm (October 30, 2003) analyzed in exercise 3?.

Hint:

Consider the next expression where a single thin ionospheric layer approximation has been taken for the second term:

$$I2_{L1} = -\frac{7257c}{2f_1^3}\int_{rec}^{sat} N_e B\cos\theta ds \simeq -\frac{7427cB_0\cos\theta}{2f_1^3}STEC$$

Where c is the light speed, B is the module of the earth magnetic field and o is the angle between B and the propagation direction. Units are in the International System (SI).

The value $B_0 \simeq 4\cdot 10^{-5} Tesla$ *can be taken for magnetic field module at the pierce point of the satellite-receiver ray with the ionospheric layer, the Ionospheric Pierce Point (IPP), (assumed at about* $400\ km$ *in height).*

Note: $f_1 = 1575.420\cdot 10^6 Hz;\quad c = 2.99792458\cdot 10^8 m/s,\quad 1\,TECU = 10^{16} e^-/m^2$

HW3: Theoretical exercises on 2nd order iono

Question 2:

Assuming that the STEC can be estimated from smoothed code PI, after removing the DCBs [1], with an accuracy better than 5 TECUs, and assuming a negligible error in the magnetic field B value [2], show that the second order I2 effect can be calculated from the expression given in previous question 1 with an error less than 1 millimetre of delay in the L1 carrier.

Note:

[1] The DCBs can be obtained from the IONEX files available at the IGS site

`ftp://cddis.gsfc.nasa.gov/gps/products/ionex/`

[2] The subroutines International Geomagnetic Reference Field (IGRF) could be used as well to compute the magnetic field.

HW3: Theoretical exercises on 2nd order iono

Question 3:

Taking into account the previous results of HW2 and HW3, and thinking of high accuracy geodetic positioning, discuss what is more suitable to remove this effect on the (first-order) ionosphere-free combination LC: To use a model or to remove this effect from a linear combination of three frequency signals?

Question 4:

The previous expressions give the I2 effect in L1 delay units. Show the following relation between the I2 delay in the L1 carrier and in the (first order) ionosphere-free combination LC[12] :

$$I2_{LC_{[12]}} = \frac{-\gamma_{12}}{1+\sqrt{\gamma_{12}}} I2_{L1}$$

$$\gamma_{ij} = \left(f_i / f_j \right)^2$$

Thank you for your attention

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